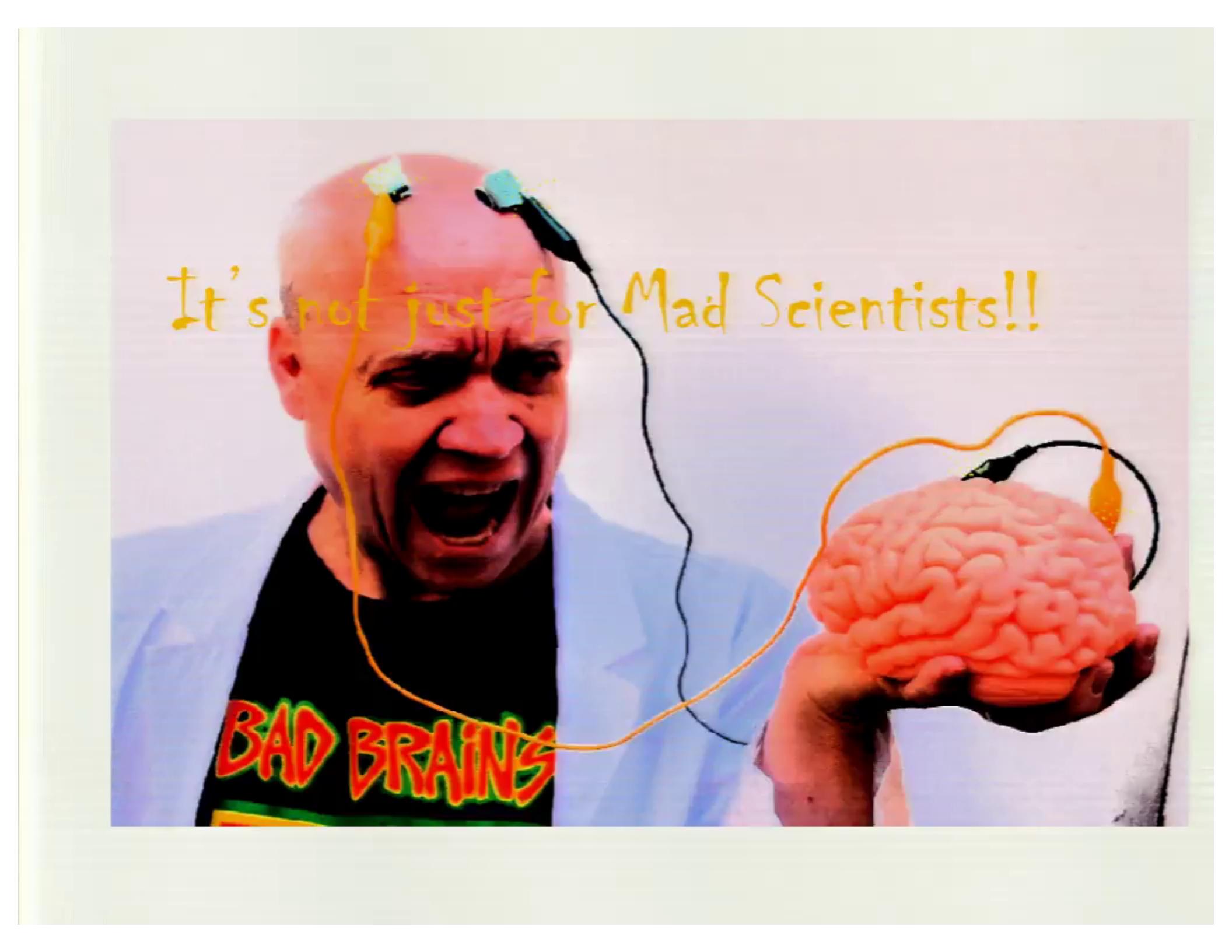


# Brain Control

Jeff Moehlis

Department of Mechanical Engineering

UC Santa Barbara

A photograph of a man screaming with a brain connected to his head by wires, and a hand holding a brain with a wire attached.

It's not just for Mad Scientists!!

BAD BRAINS

# Outline / Inspiration

## Parkinson's Disease

- **model:** population of neural oscillators
- **goal:** desynchronize neural activity
- **reduction:** based on isochrons
- **two control methods:** chaotic desync, optimal phase resetting



# Outline / Inspiration

## Parkinson's Disease

- **model:** population of neural oscillators
- **goal:** desynchronize neural activity
- **reduction:** based on isochrons
- **two control methods:** chaotic desync, optimal phase resetting



## Cardiac Arrhythmias

- **model:** excitable cells
- **alternans goal:** stabilize unstable periodic orbit
- **reduction:** based on isostables
- **fibrillation goal:** eliminate spirals



# Outline / Inspiration from Snowbird

- DS01 - Peter Tass talk
  - Complex Phase Resetting Techniques for Desynchronization
- DS05 - meeting with Eric Shea-Brown during break
  - collaboration: Optimal Inputs for Phase Models of Spiking Neurons, 2006
- DS05 - Danny Forger talk
  - Stochastic Stimulation of the Mammalian Circadian Clock
- DS07 - co-organized MS “Mathematics of PD”, w/ Jon Rubin
  - also co-organized related MS's in DS11, DS13
- DS11 - Tay Netoff talk
  - Using PRC's to Understand How Antiepileptic Drugs and Deep Brain Stimulation Prevent Seizures
- DSXX - talks by Bard Ermentrout, Steve Schiff,...
- DS13 – meeting with Flavio Fenton and Elizabeth Cherry during break



# Parkinson's disease



- affects 1,000,000 people in the US
- estimated cost: \$25 billion/year
- symptoms
  - tremors
  - postural instability
  - bradykinesia – slowness of movement
  - rigidity
- one hypothesis  
associated with pathological synchronization of neural activity in motor control region
- treatment
  - drugs
  - Deep Brain Stimulation



# Deep Brain Stimulation



Video:

Andrew Johnson (Auckland, New Zealand)  
diagnosed with early onset PD at age 35

blog: <http://youngandshaky.com>

video: <http://www.youtube.com/watch?v=uBh2LxTW0s0>

# Deep Brain Stimulation



<http://www.youtube.com/watch?v=uBh2LxTW0s0>



## Control Objective:

- find electrical stimulus which leads to desynchronization of neural activity using minimal power

**DESYNC**



# Isochrons

$$\frac{d\mathbf{x}}{dt} = \mathbf{F}(\mathbf{x}), \quad \mathbf{x} \in \mathbb{R}^n, \quad (n \geq 2)$$

stable hyperbolic periodic orbit  $\mathbf{x}^\gamma(t)$ , period  $T$

isochron:

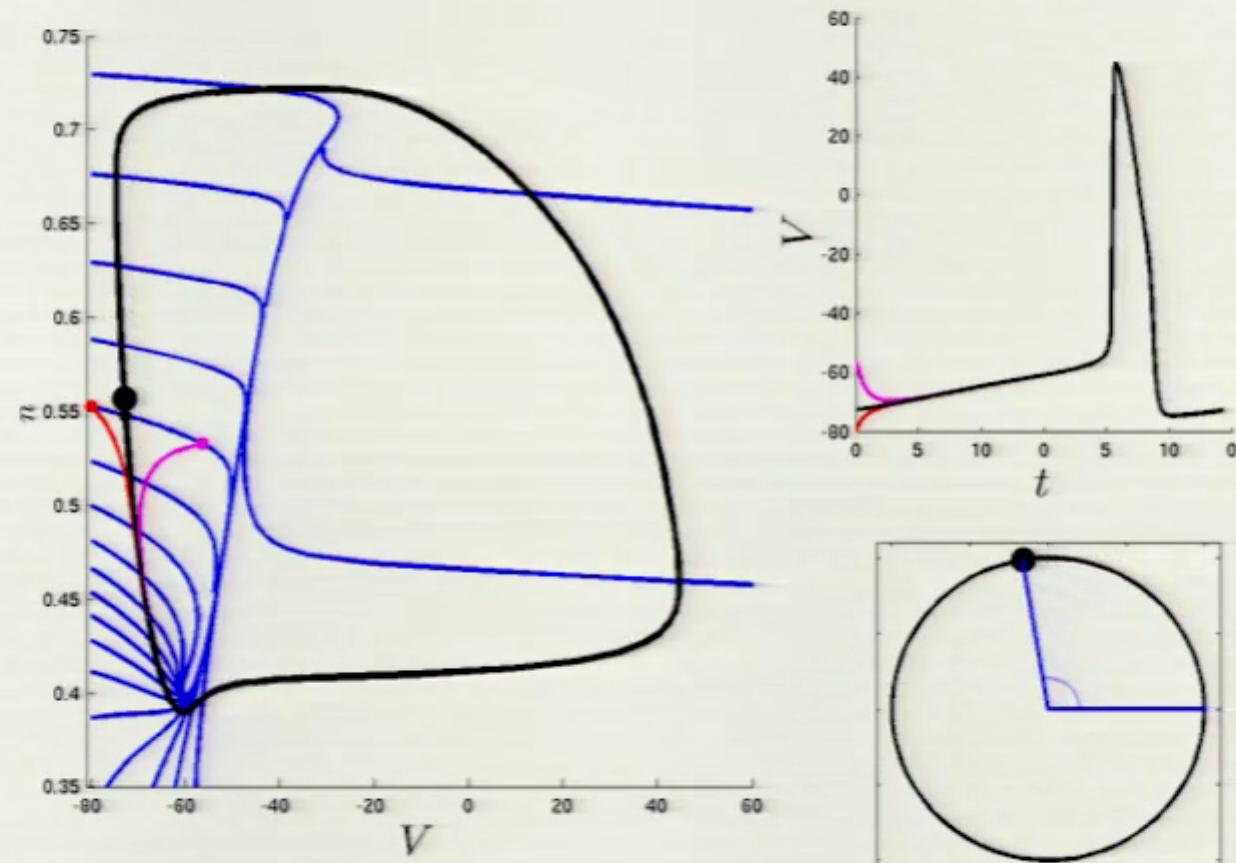
- a set of initial conditions that share the same asymptotic convergence to a periodic orbit
- a level set of phase variable  $\theta(\mathbf{x})$

on and off periodic orbit:

$$\frac{d\theta}{dt} = \frac{2\pi}{T} \equiv \omega$$



# Initial Conditions on Same Isochron



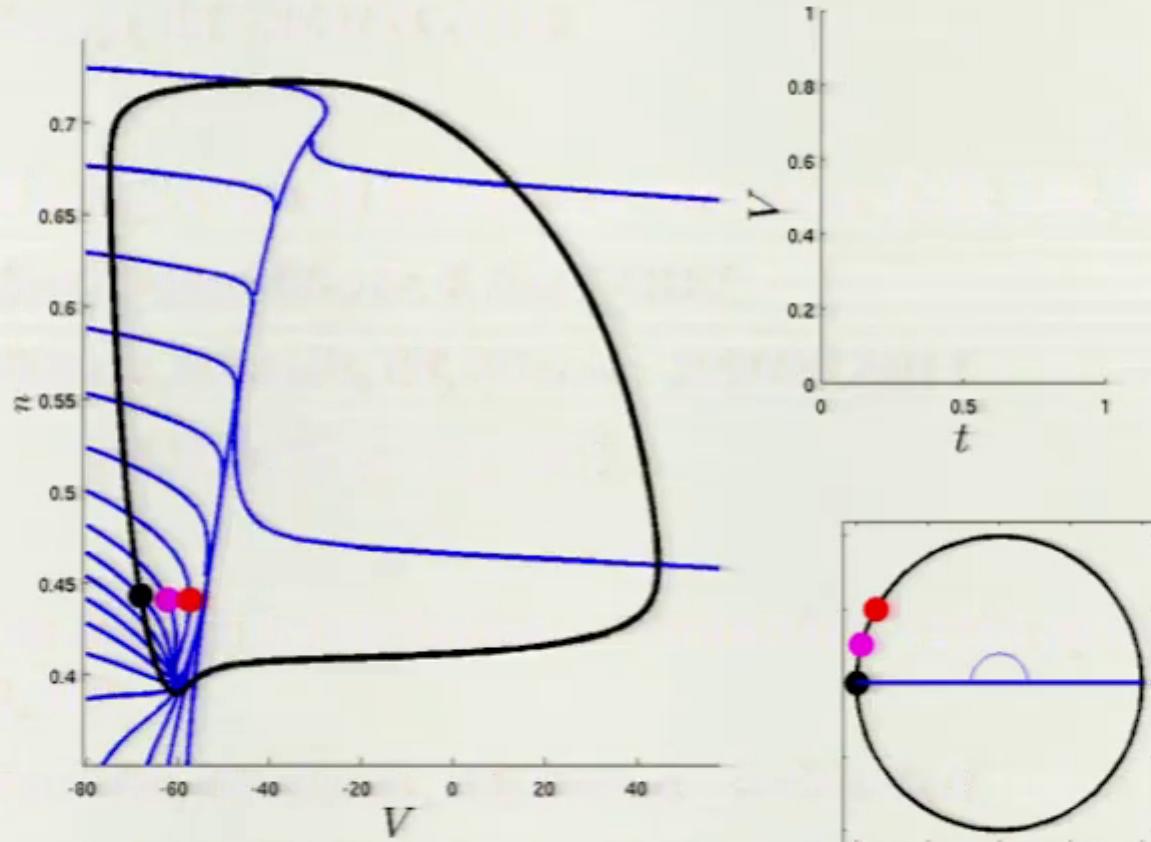
# Computation of Isochrons – Some New Methods



- **Continuation of a two point boundary value problem (2D)**
  - Osinga, M - *SIADS* 2010
- **Spectral properties of Koopman operator (2D, 3D, 4D,...)**
  - Mauroy and Mezic, *Chaos* 2012
  - Mauroy, Rhoads, M, Mezic – *SIADS* 2014
    - (3D bursting neurons)
- **Hamilton-Jacobi formulation of boundary value problem (2D, 3D, 4D,...)**
  - Detrixhe, Doubeck, M, Gibou – submitted
    - (3D mixed mode oscillations, 4D Hodgkin-Huxley model)

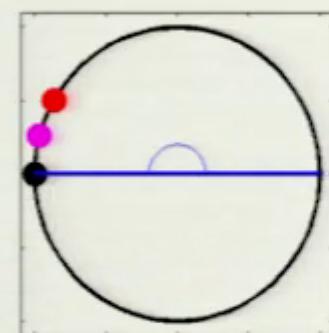
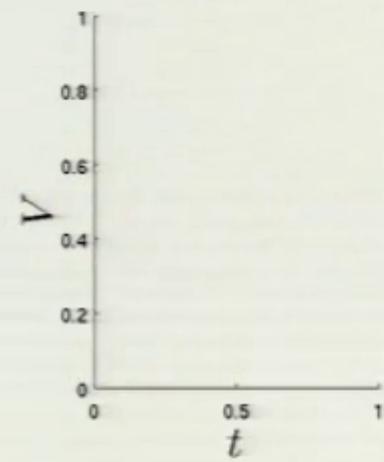
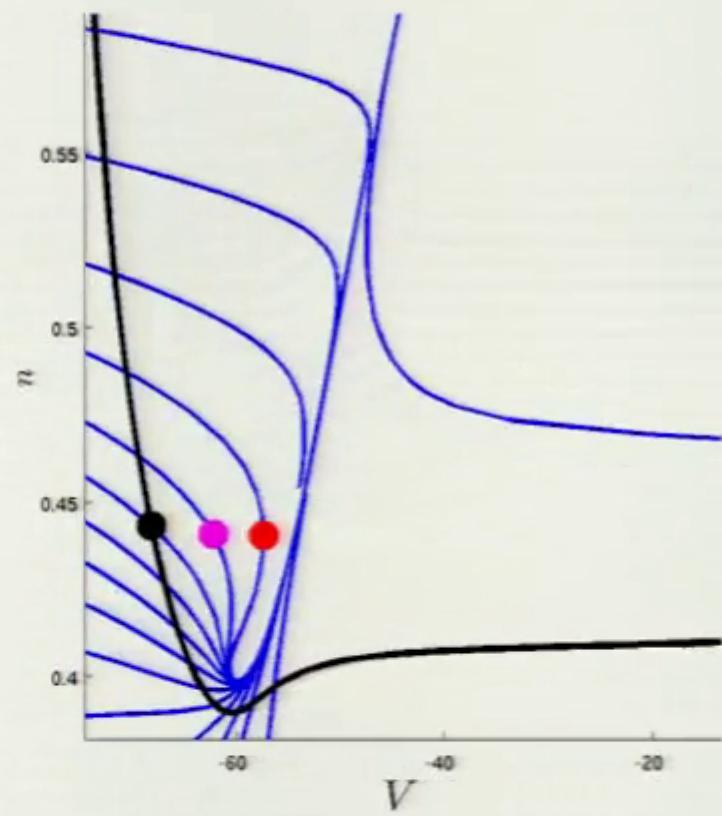


# Initial Conditions on Different Isochrons



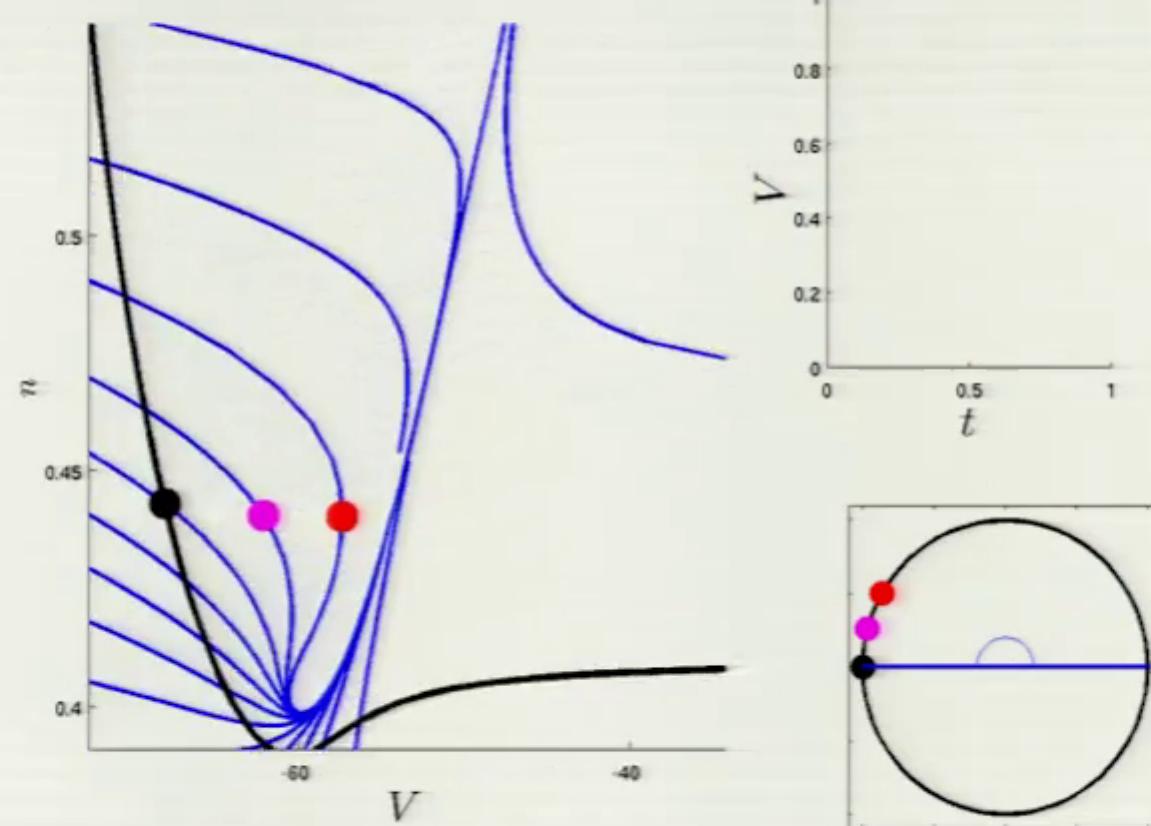


# Initial Conditions on Different Isochrons



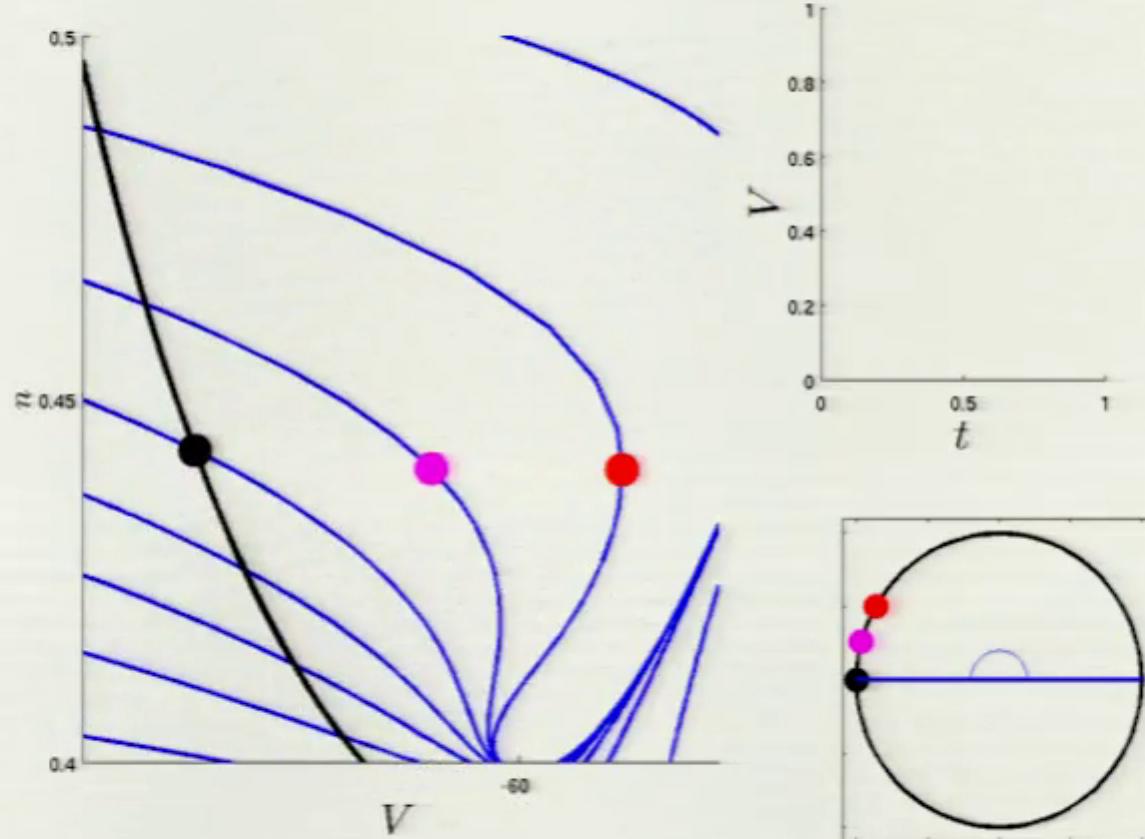


# Initial Conditions on Different Isochrons



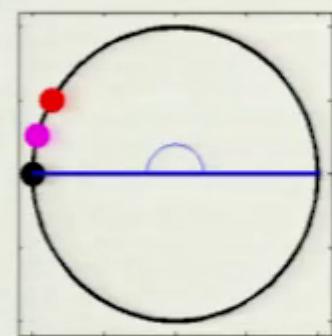
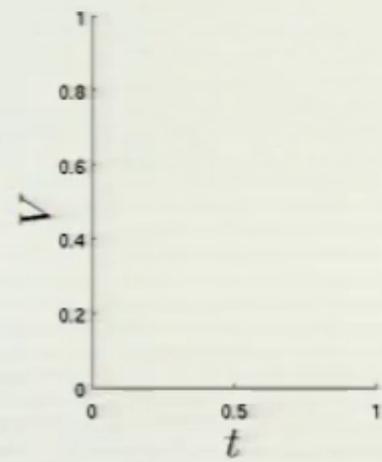
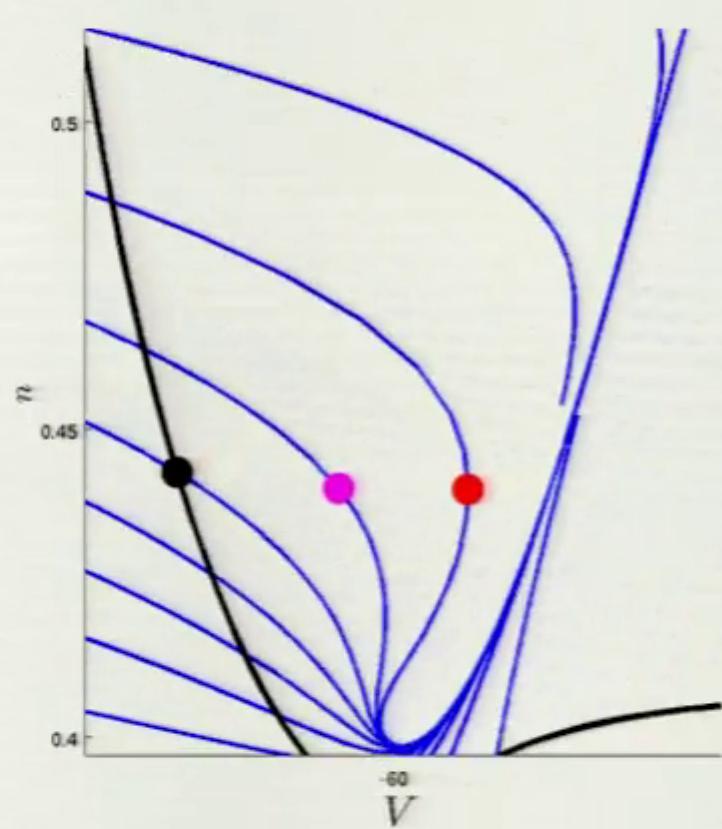


# Initial Conditions on Different Isochrons



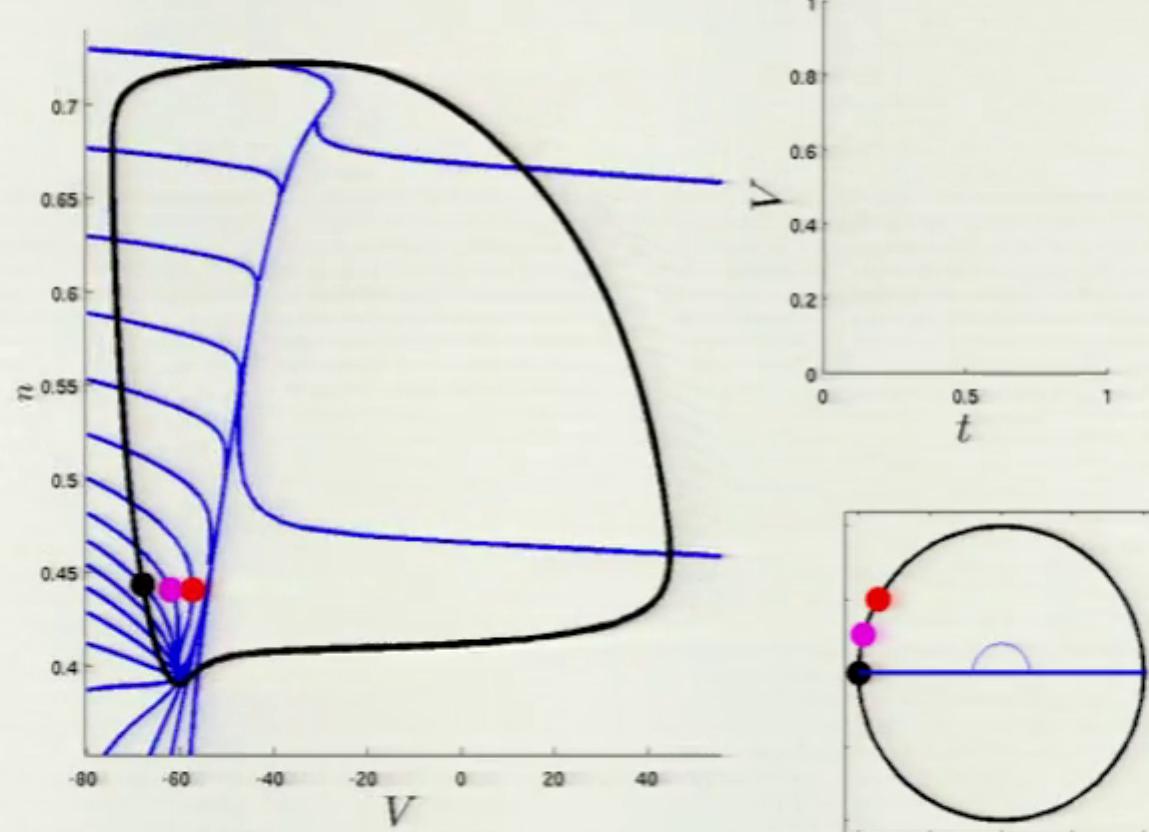


# Initial Conditions on Different Isochrons



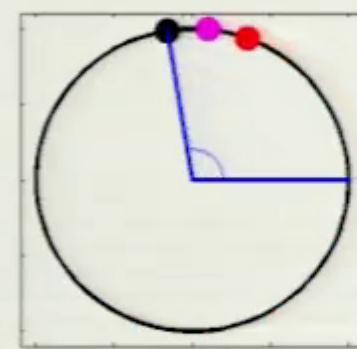
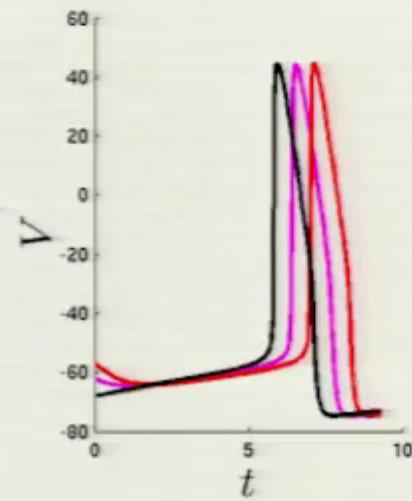
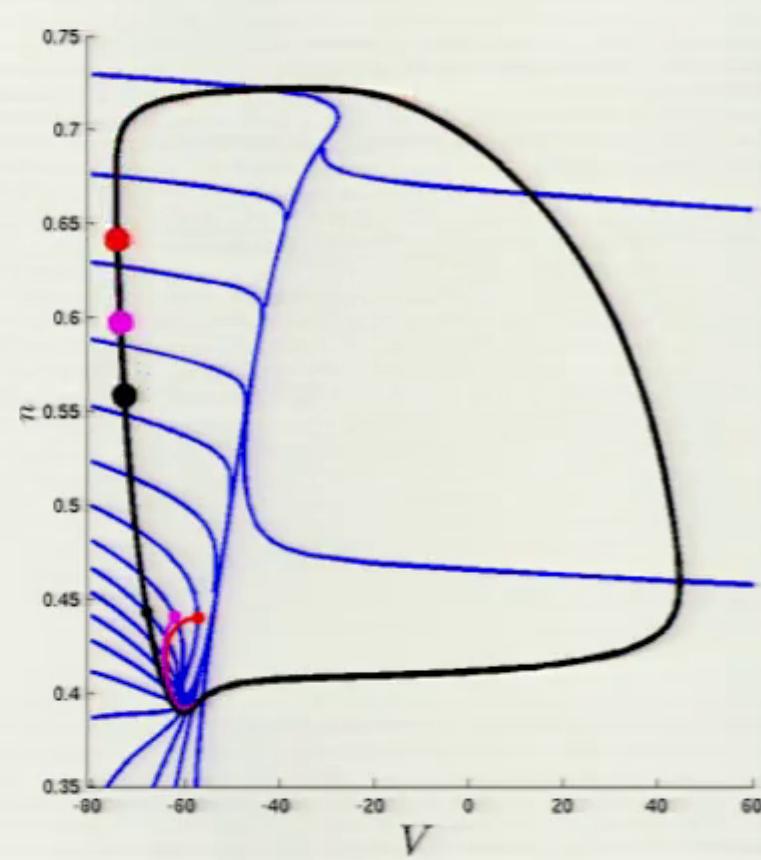


# Initial Conditions on Different Isochrons



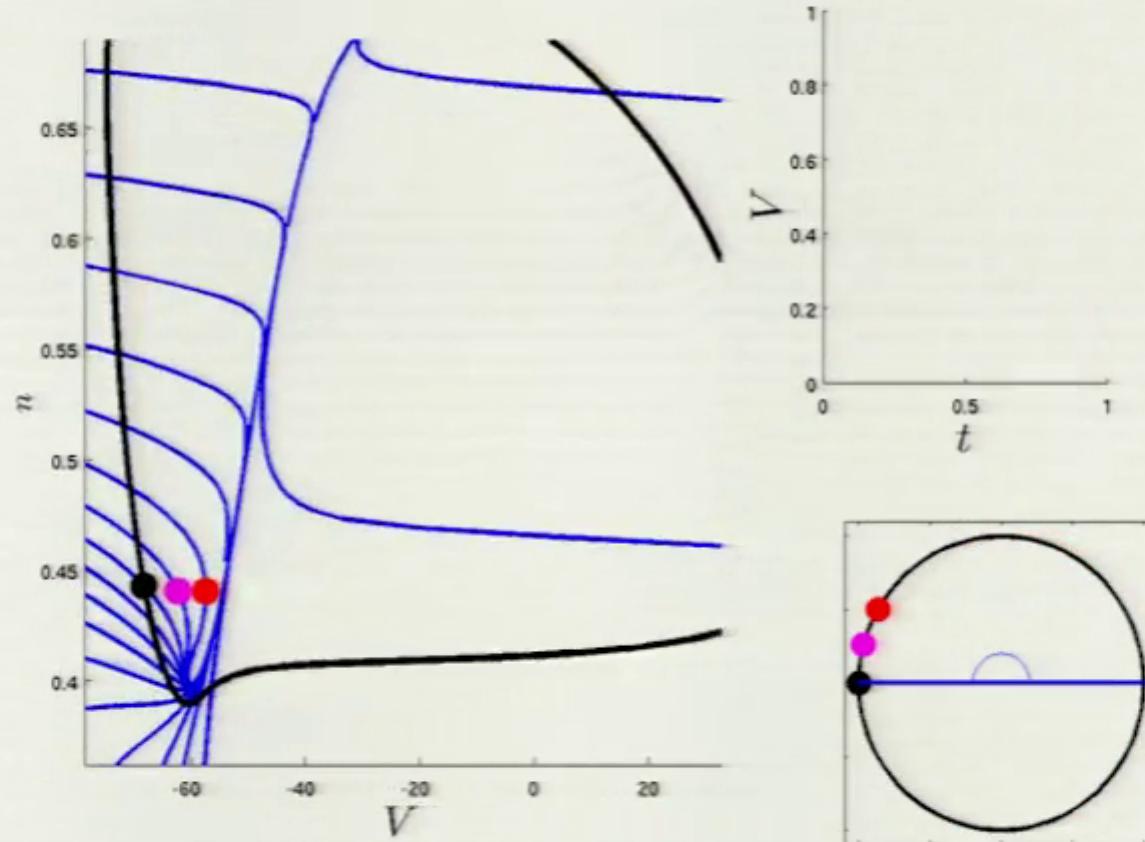


# Initial Conditions on Different Isochrons



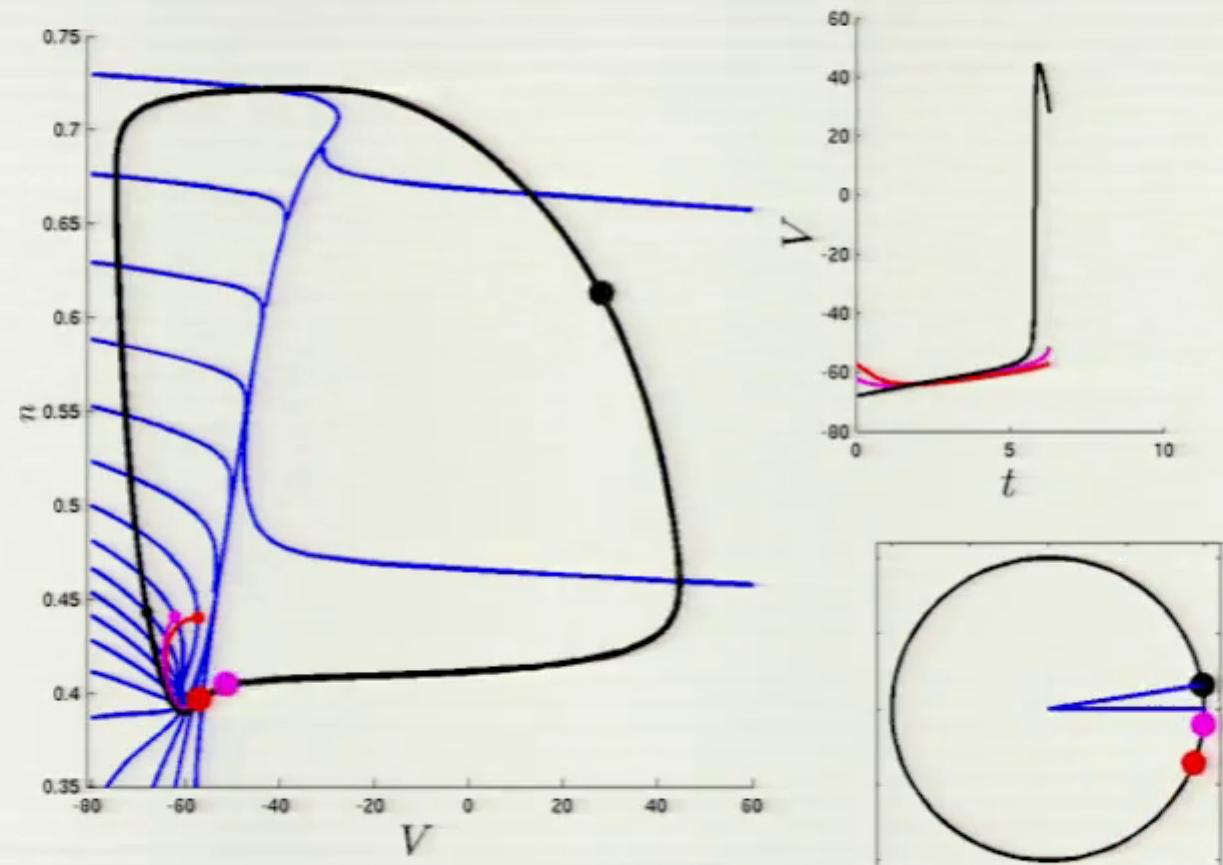


# Initial Conditions on Different Isochrons





# Initial Conditions on Different Isochrons



# Optimal Chaotic Desync



Phase model:

$$\frac{d\theta_i}{dt} = \omega + Z(\theta_i)u(t), \quad i = 1, 2,$$

where  $Z(\theta)$  is phase response curve,  $u(t)$  is input current.

Let  $\phi \equiv |\theta_2 - \theta_1|$ :

$$\frac{d\phi}{dt} = Z'(\theta)u(t)\phi + \mathcal{O}(\phi^2),$$

$$\Rightarrow \phi(t) \sim e^{\Lambda(t)t}, \quad \Lambda(\tau) = \frac{\log(\phi(\tau))}{\tau} = \frac{\int_a^{a+\tau} Z'(\theta(s))u(s)ds}{\tau}.$$

Here  $\Lambda(\tau)$  is the Lyapunov exponent for time  $\tau$ .



# Optimal Chaotic Desync

Phase model:

$$\frac{d\theta_i}{dt} = \omega + Z(\theta_i)u(t), \quad i = 1, 2,$$

where  $Z(\theta)$  is phase response curve,  $u(t)$  is input current.

Let  $\phi \equiv |\theta_2 - \theta_1|$ :

$$\frac{d\phi}{dt} = Z'(\theta)u(t)\phi + \mathcal{O}(\phi^2),$$

$$\Rightarrow \boxed{\phi(t) \sim e^{\Lambda(t)t}, \quad \Lambda(\tau) = \frac{\log(\phi(\tau))}{\tau} = \frac{\int_a^{a+\tau} Z'(\theta(s))u(s)ds}{\tau}}.$$

Here  $\Lambda(\tau)$  is the Lyapunov exponent for time  $\tau$ .



# Optimal Chaotic Desync

Use calculus of variations to minimize (with  $\beta > 0$ )

$$\mathcal{C}[u(t)] = \int_0^{t_1} \left\{ u(t)^2 - \beta Z'(\theta)u(t) + \lambda \left( \frac{d\theta}{dt} - \omega - Z(\theta)u(t) \right) \right\} dt$$

This gives the two point boundary value problem

$$\dot{\theta} = Z(\theta)[\beta Z'(\theta) + \lambda Z(\theta)]/2 + \omega$$

$$\dot{\lambda} = -[\beta Z'(\theta) + \lambda Z(\theta)][\beta Z''(\theta) + \lambda Z'(\theta)]/2$$

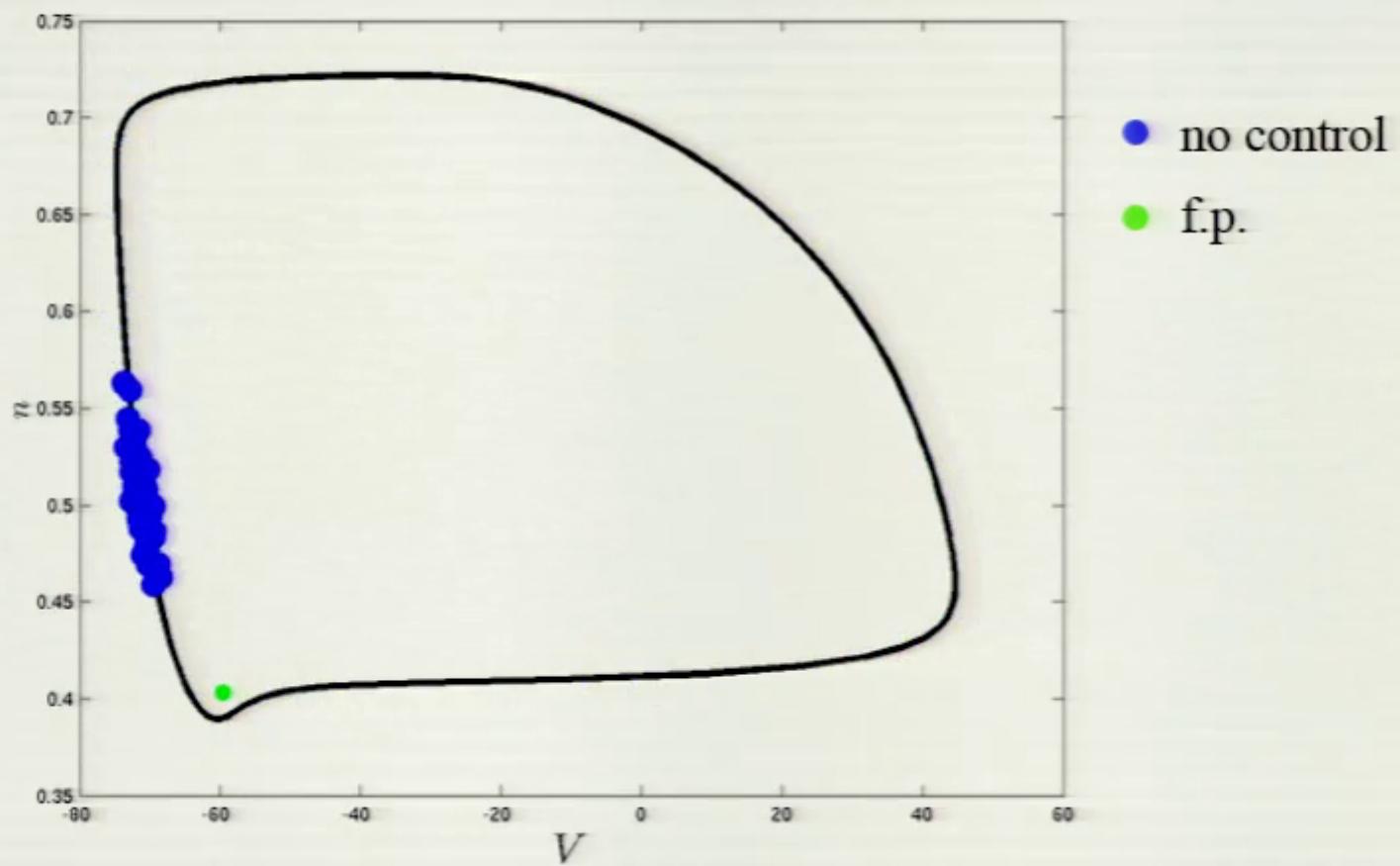
$$\theta(0) = 0, \quad \theta(t_1) = \omega t_1$$

$$u(t) = [\beta Z'(\theta) + \lambda Z(\theta)]/2$$

If average voltage exceeds threshold, apply this  $u(t)$

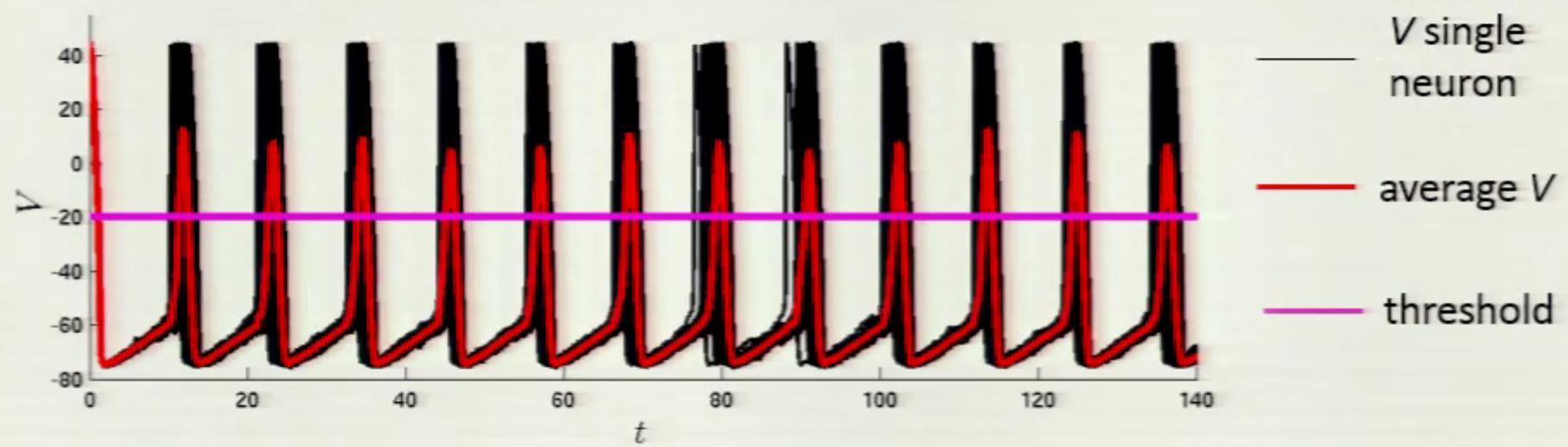


# Coupled, Noisy Neurons – No Control



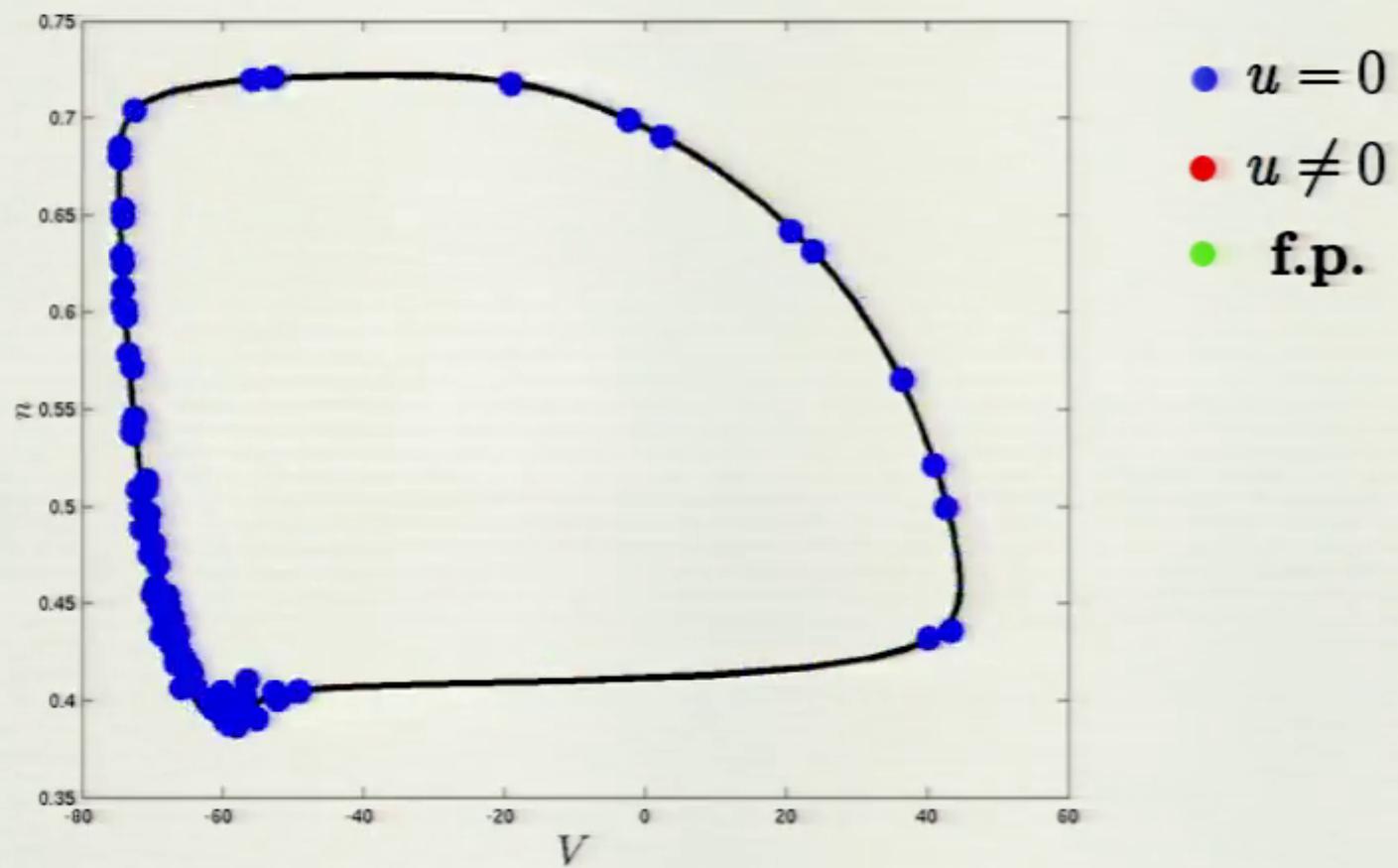


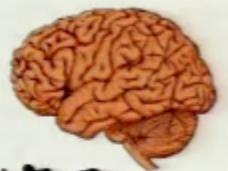
# Coupled, Noisy Neurons – No Control



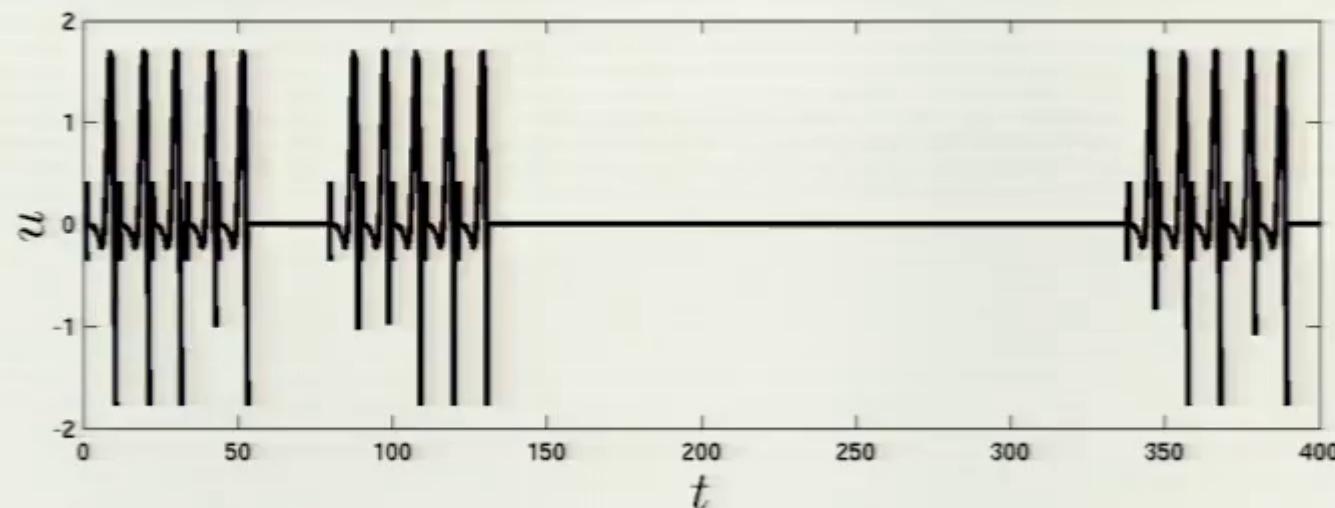
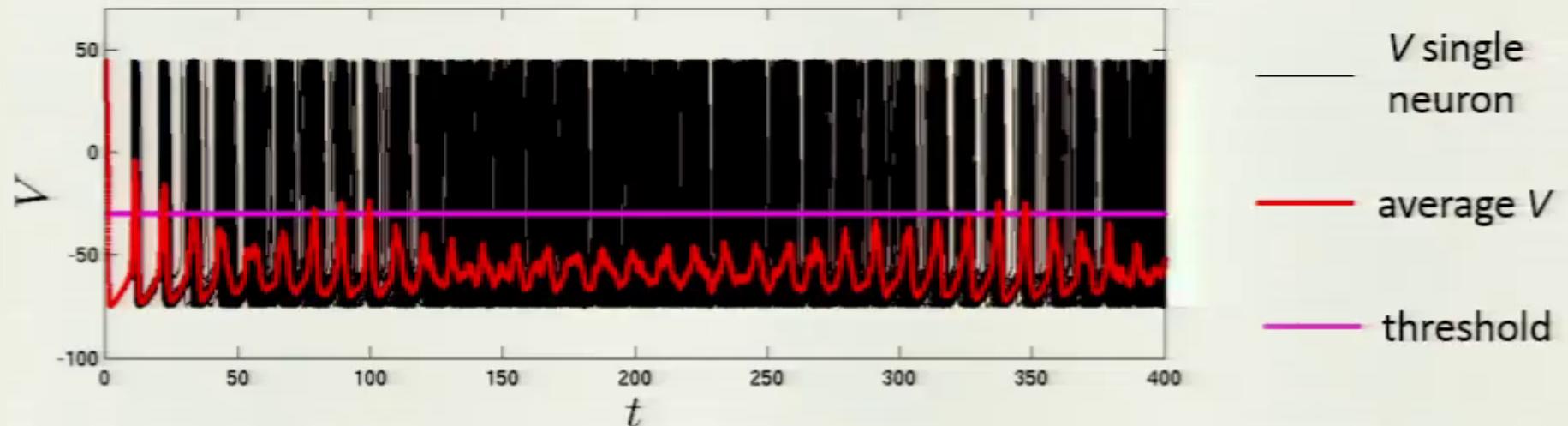


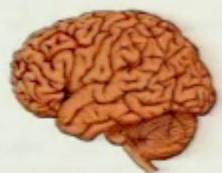
# Coupled, Noisy Neurons – Chaotic Desync



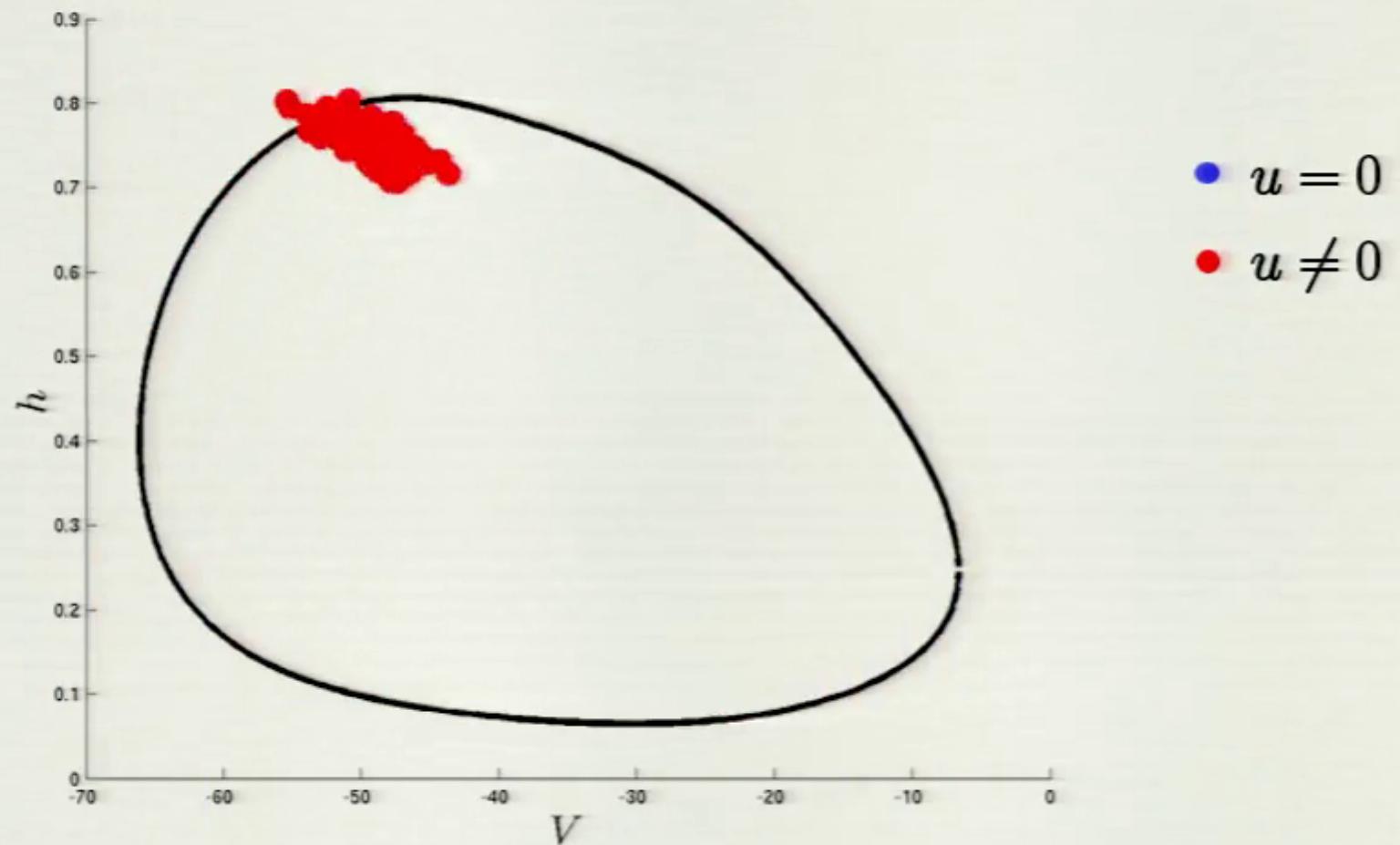


# Coupled, Noisy Neurons – Chaotic Desync



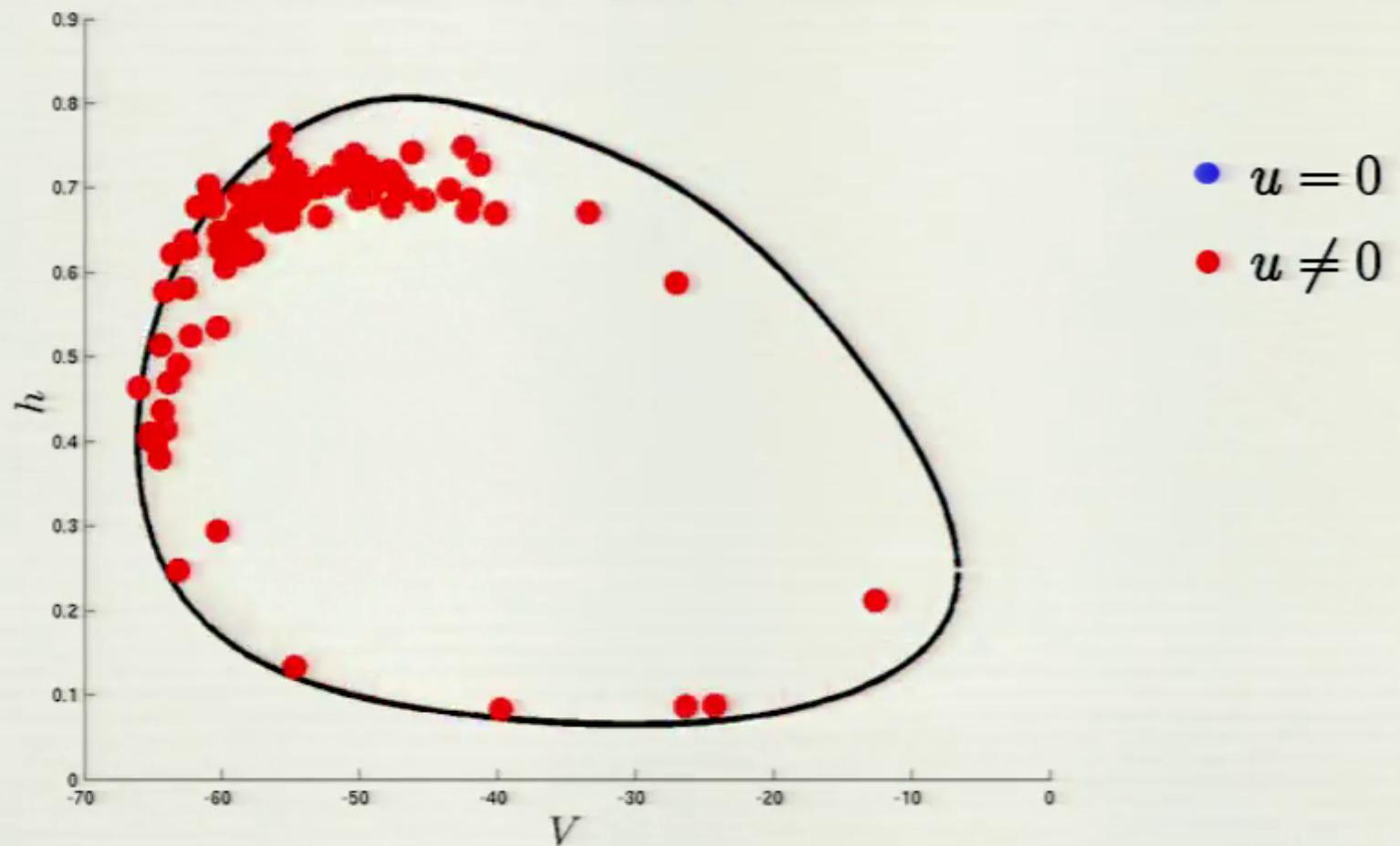


# Chaotic Desync of Thalamic Neurons



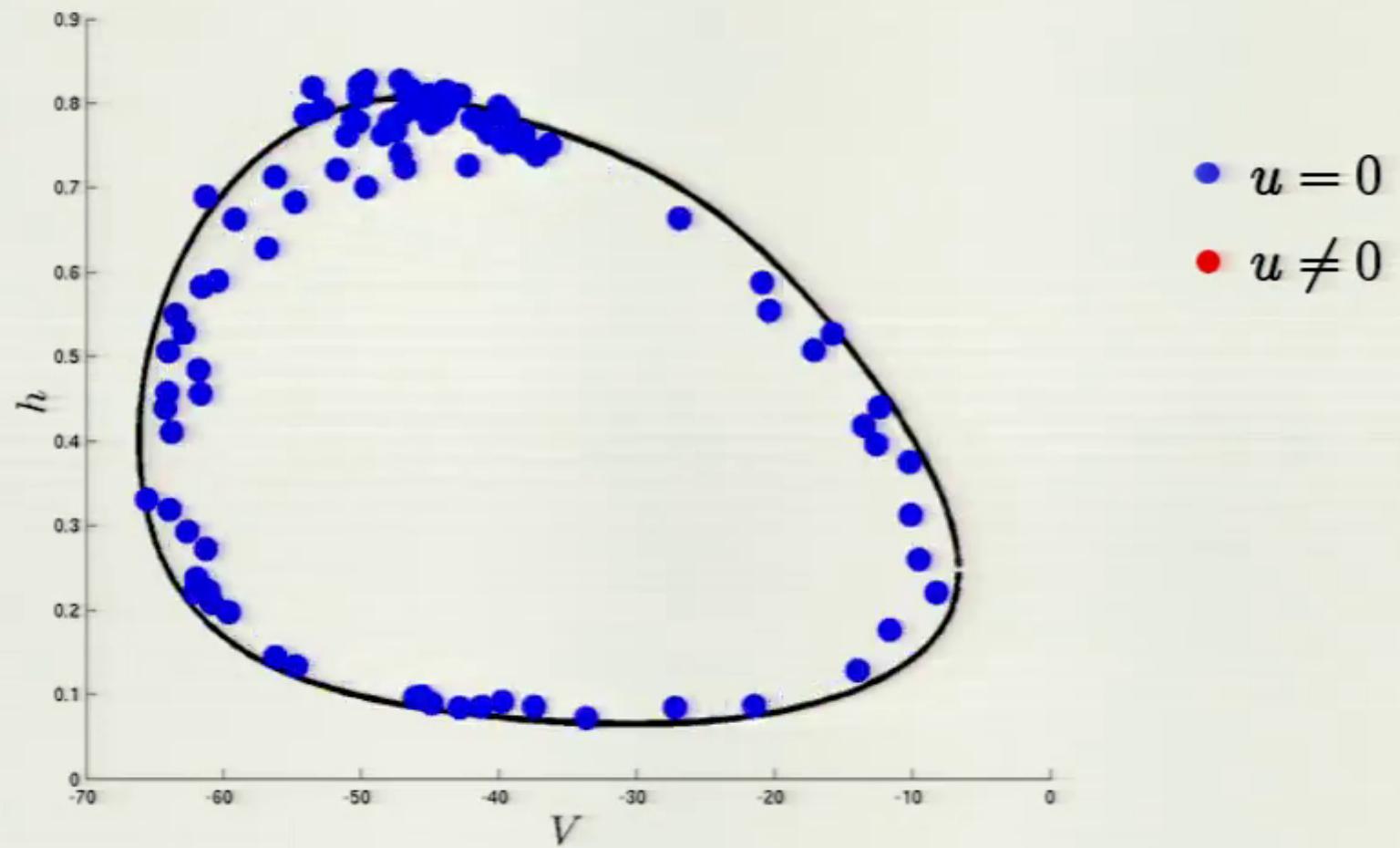


# Chaotic Desync of Thalamic Neurons



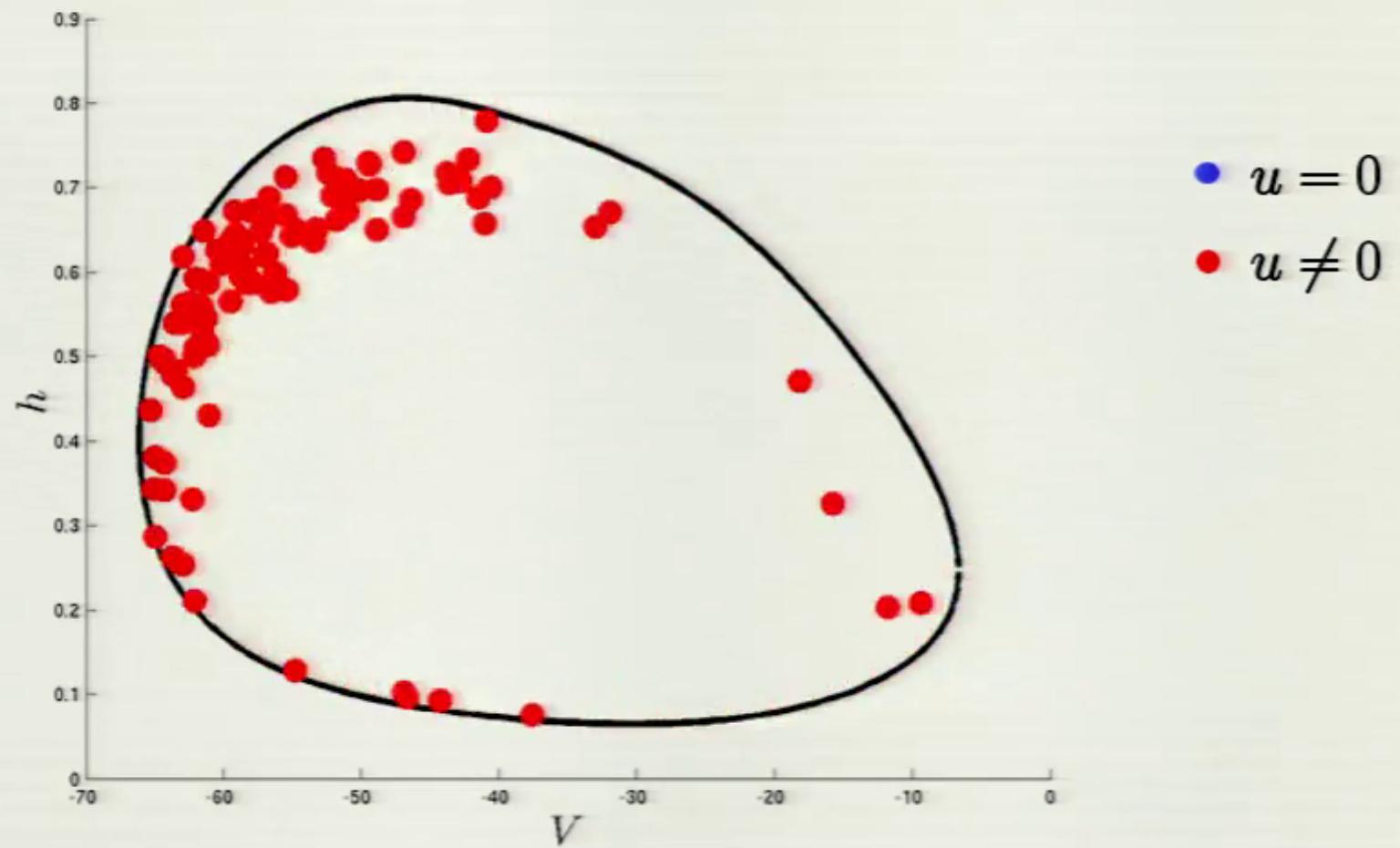


# Chaotic Desync of Thalamic Neurons



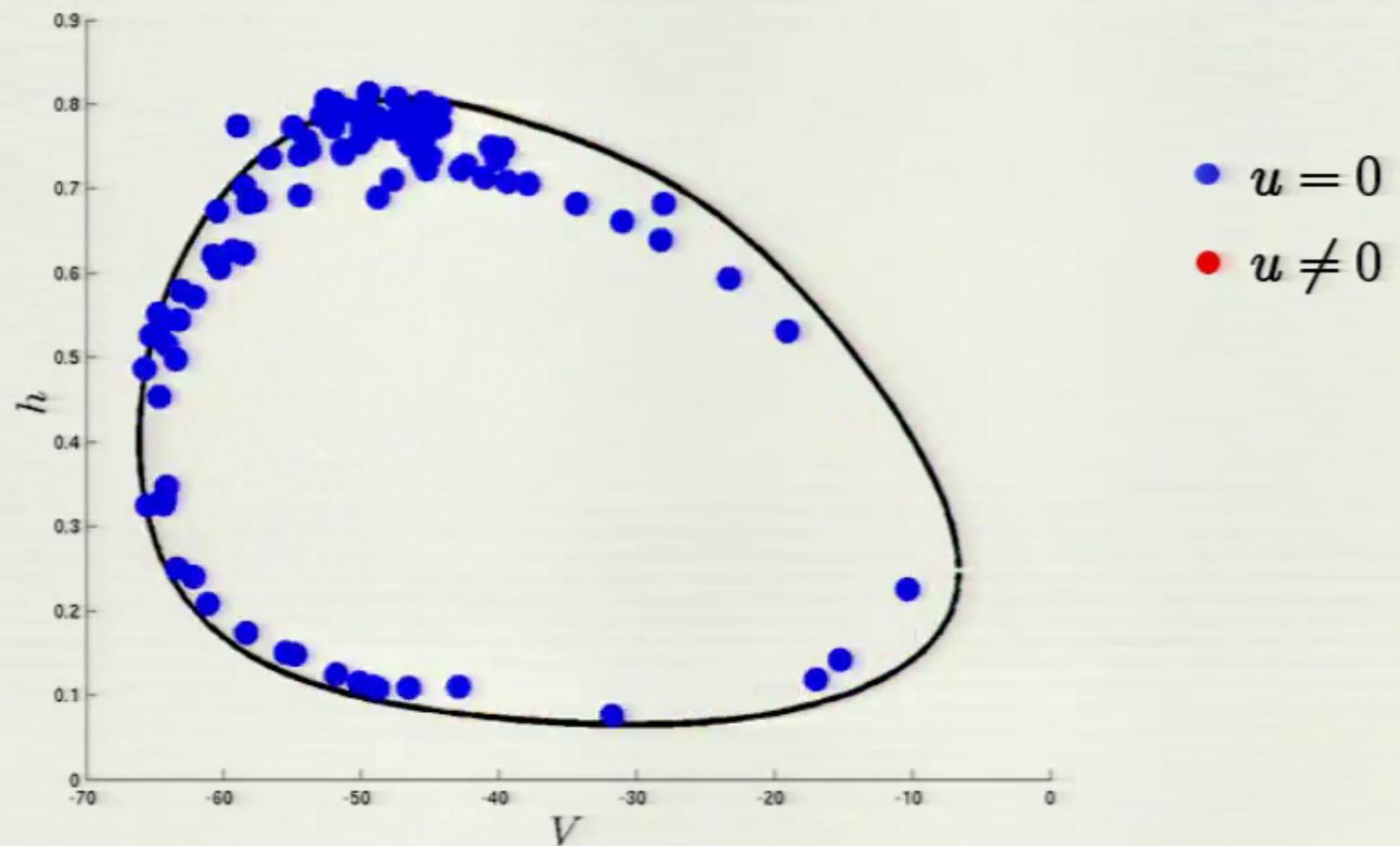


# Chaotic Desync of Thalamic Neurons



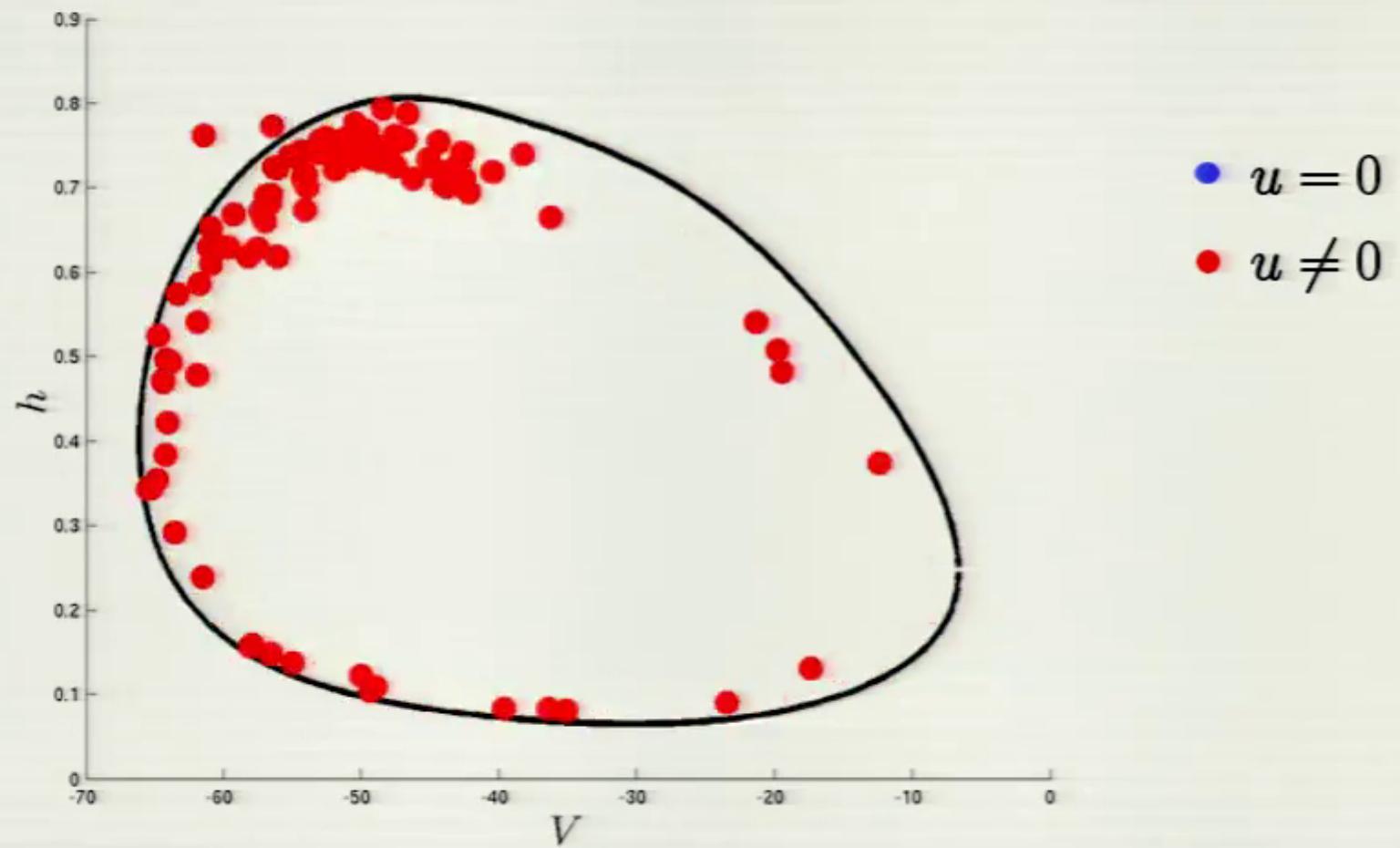


# Chaotic Desync of Thalamic Neurons



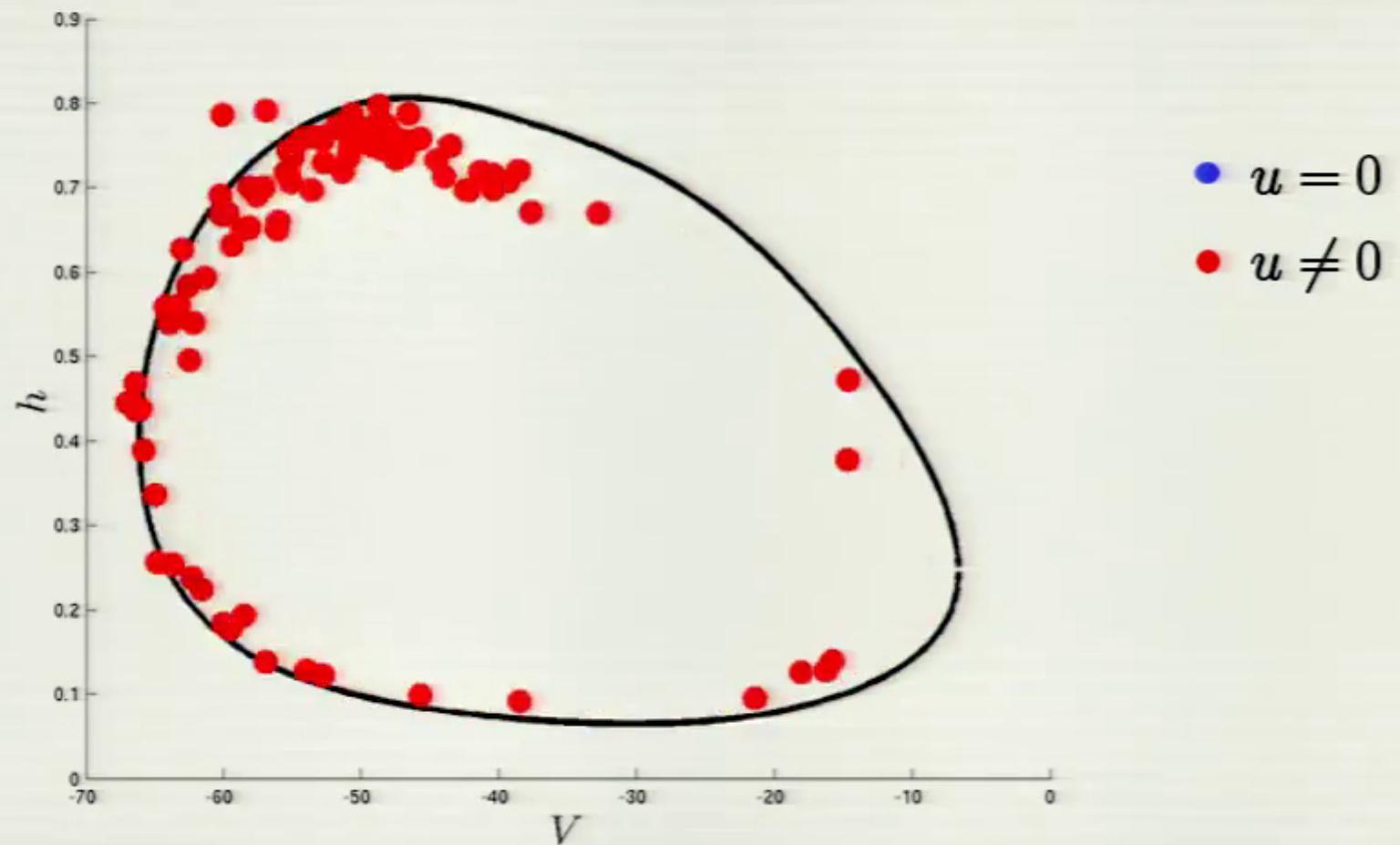


# Chaotic Desync of Thalamic Neurons



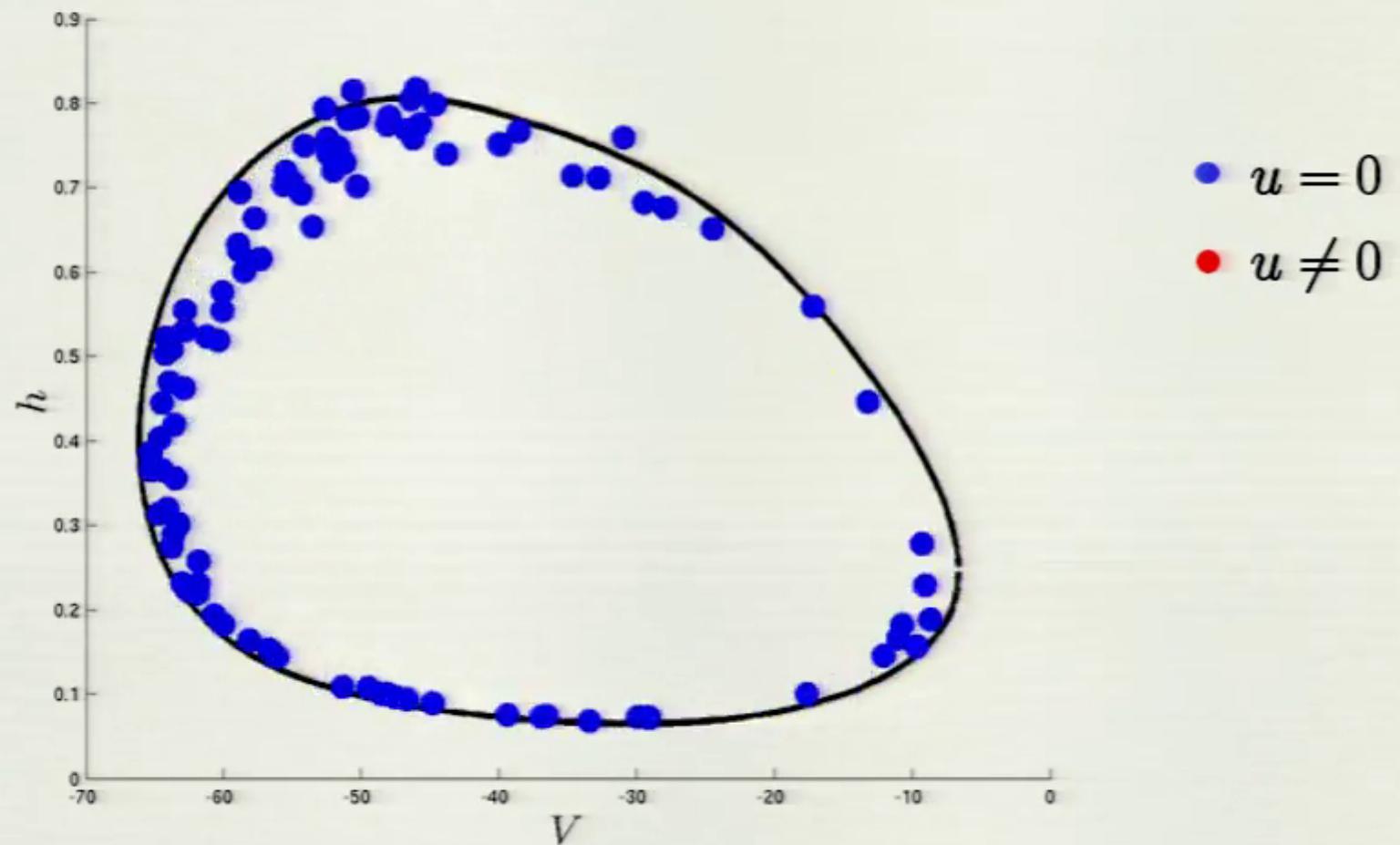


# Chaotic Desync of Thalamic Neurons



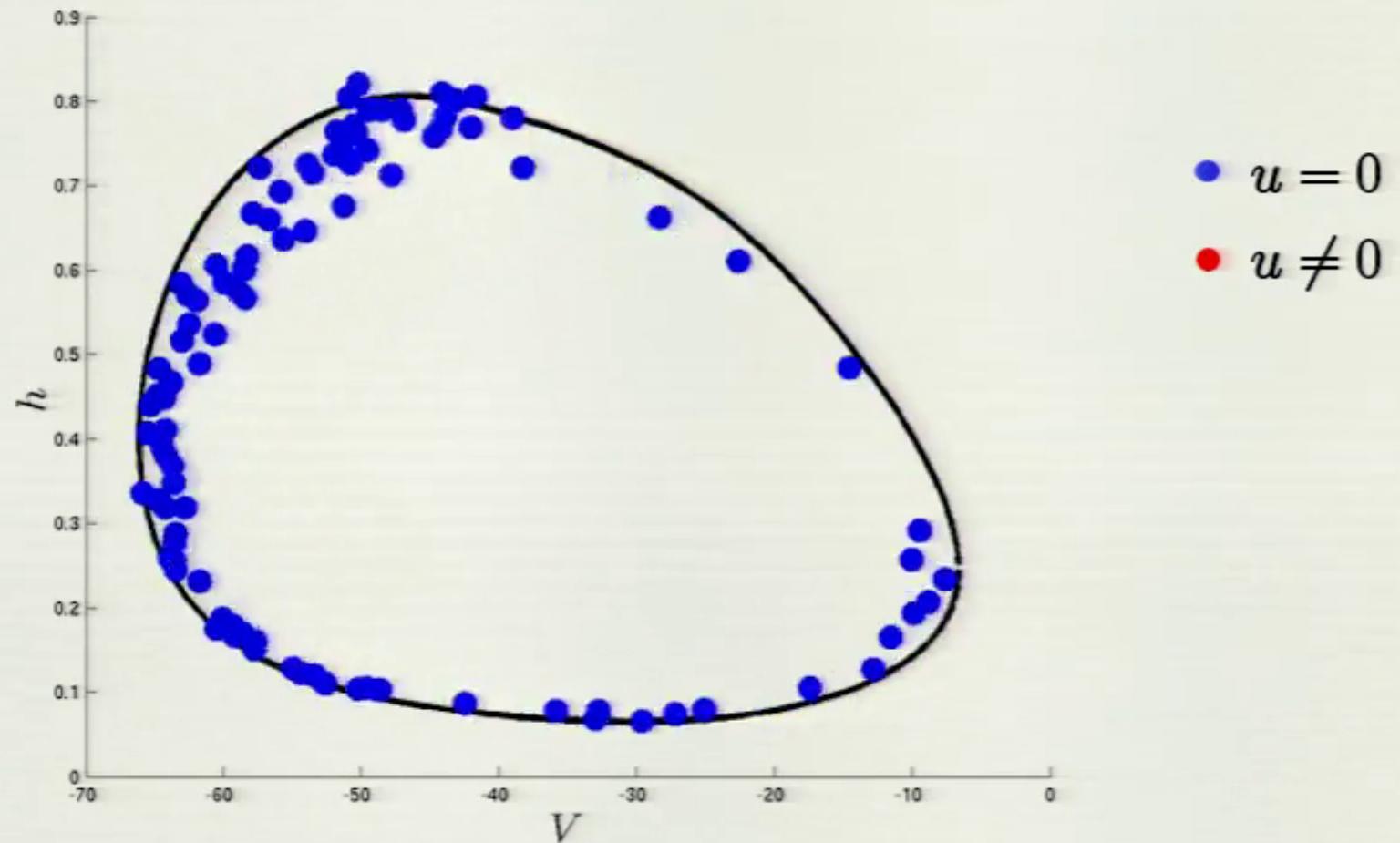


# Chaotic Desync of Thalamic Neurons



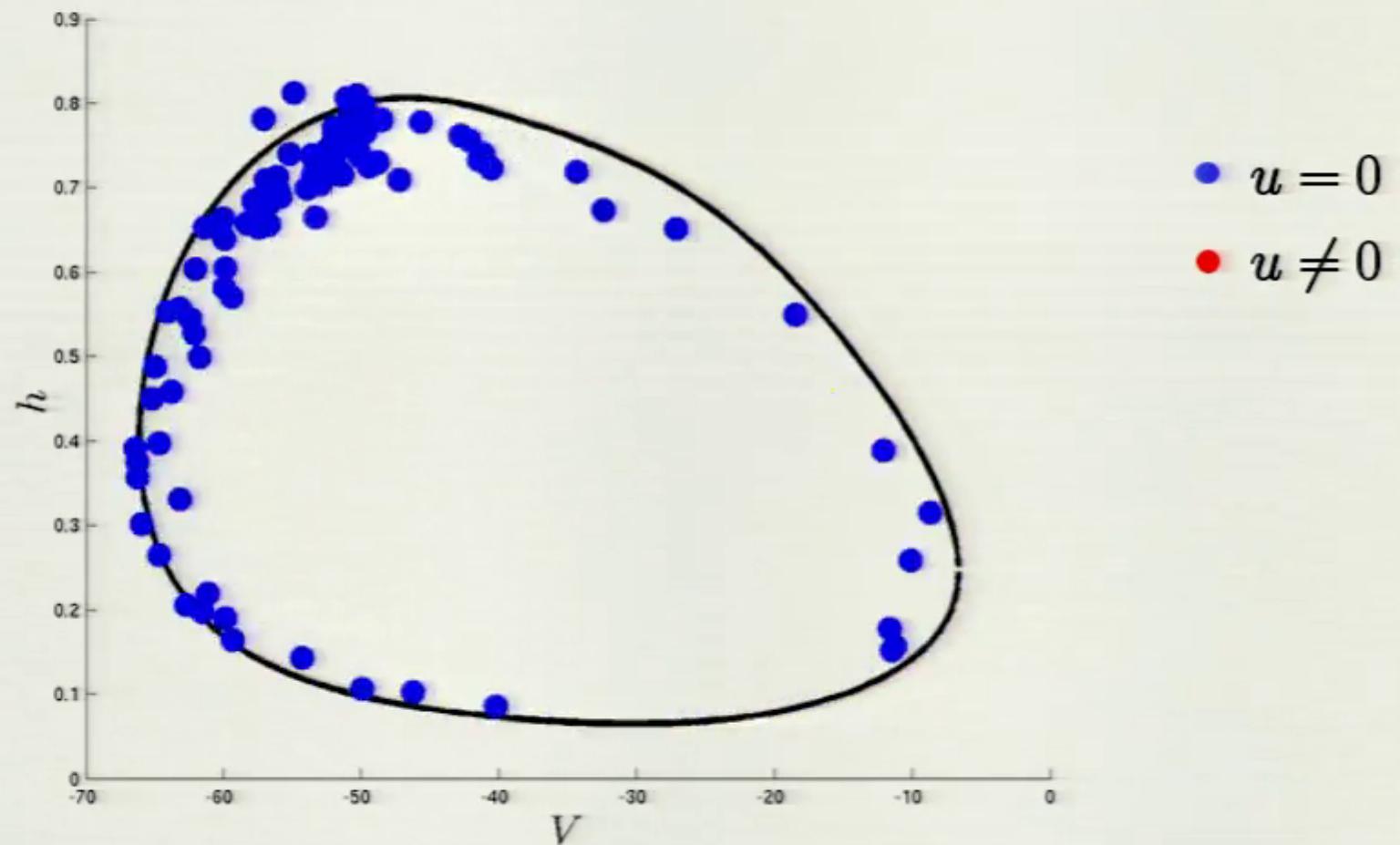


# Chaotic Desync of Thalamic Neurons



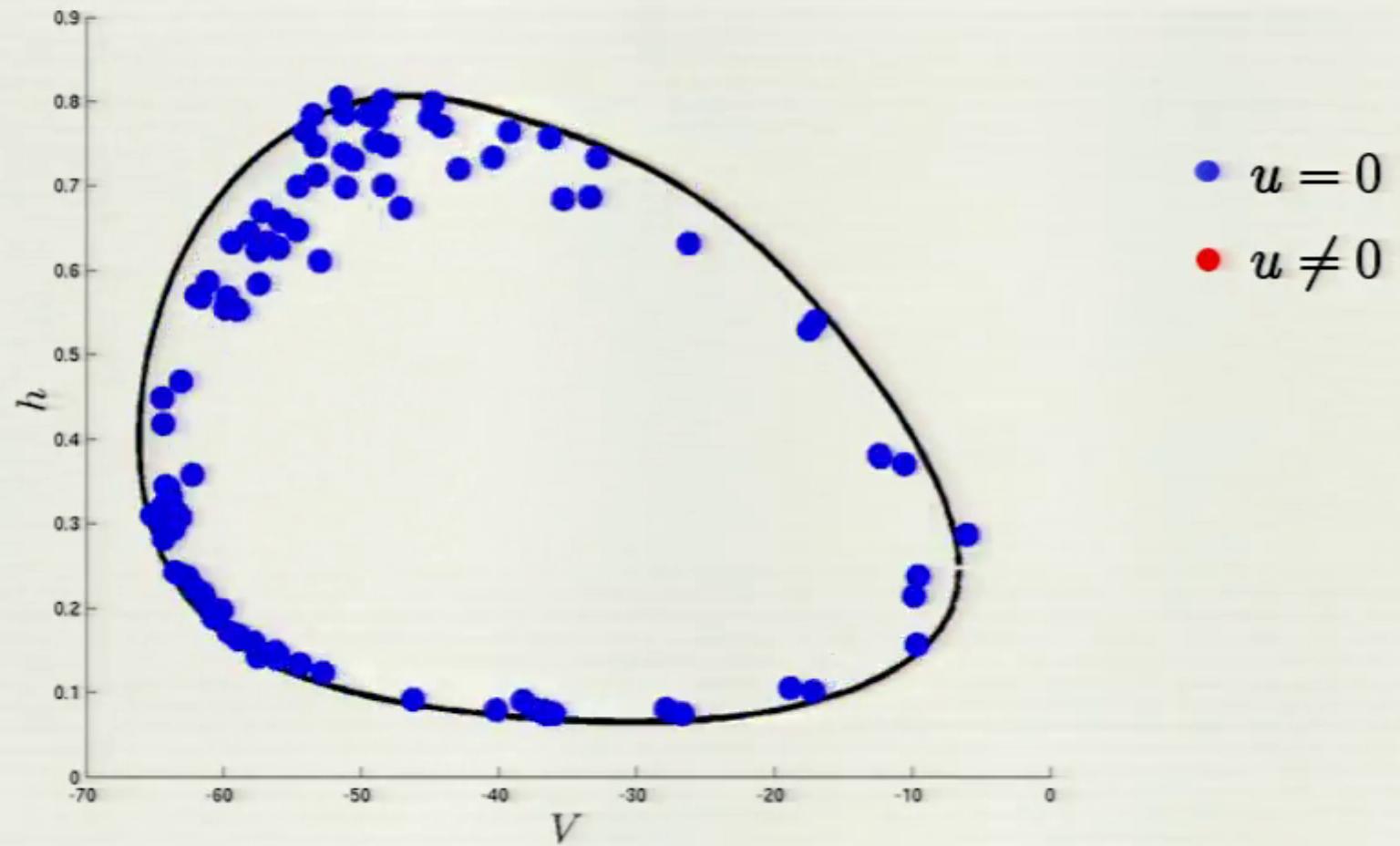


# Chaotic Desync of Thalamic Neurons



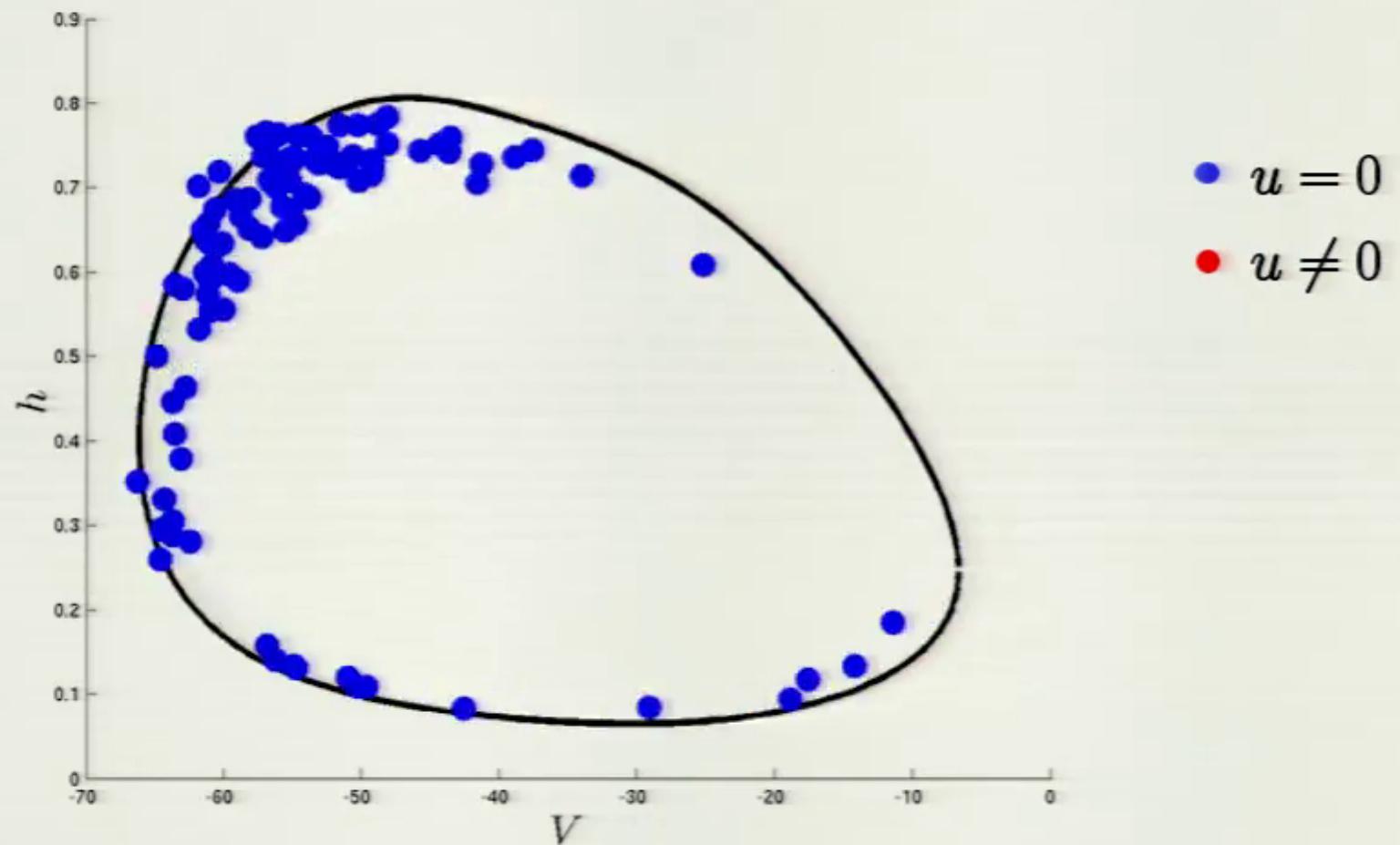


# Chaotic Desync of Thalamic Neurons



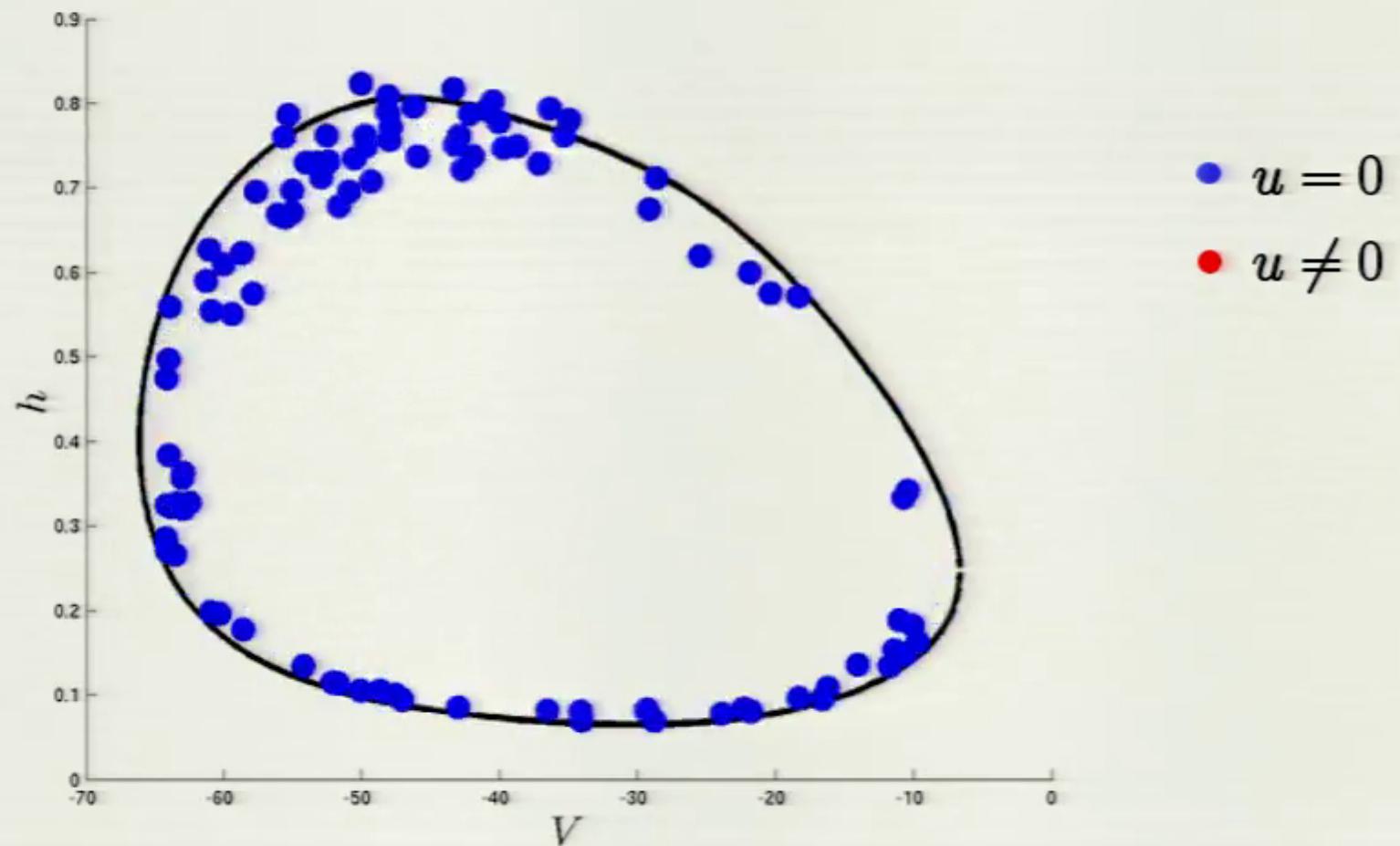


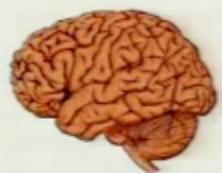
# Chaotic Desync of Thalamic Neurons



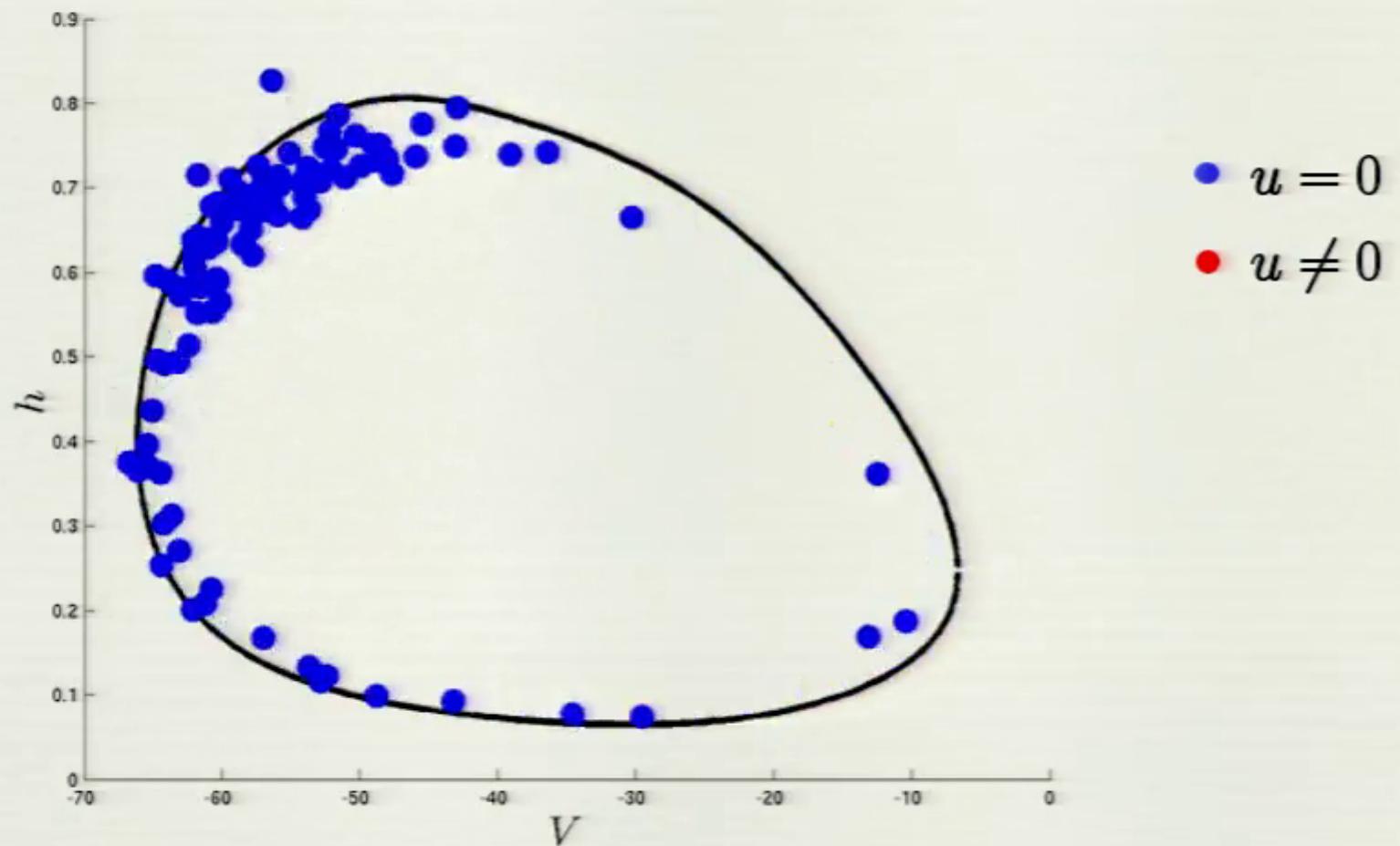


# Chaotic Desync of Thalamic Neurons



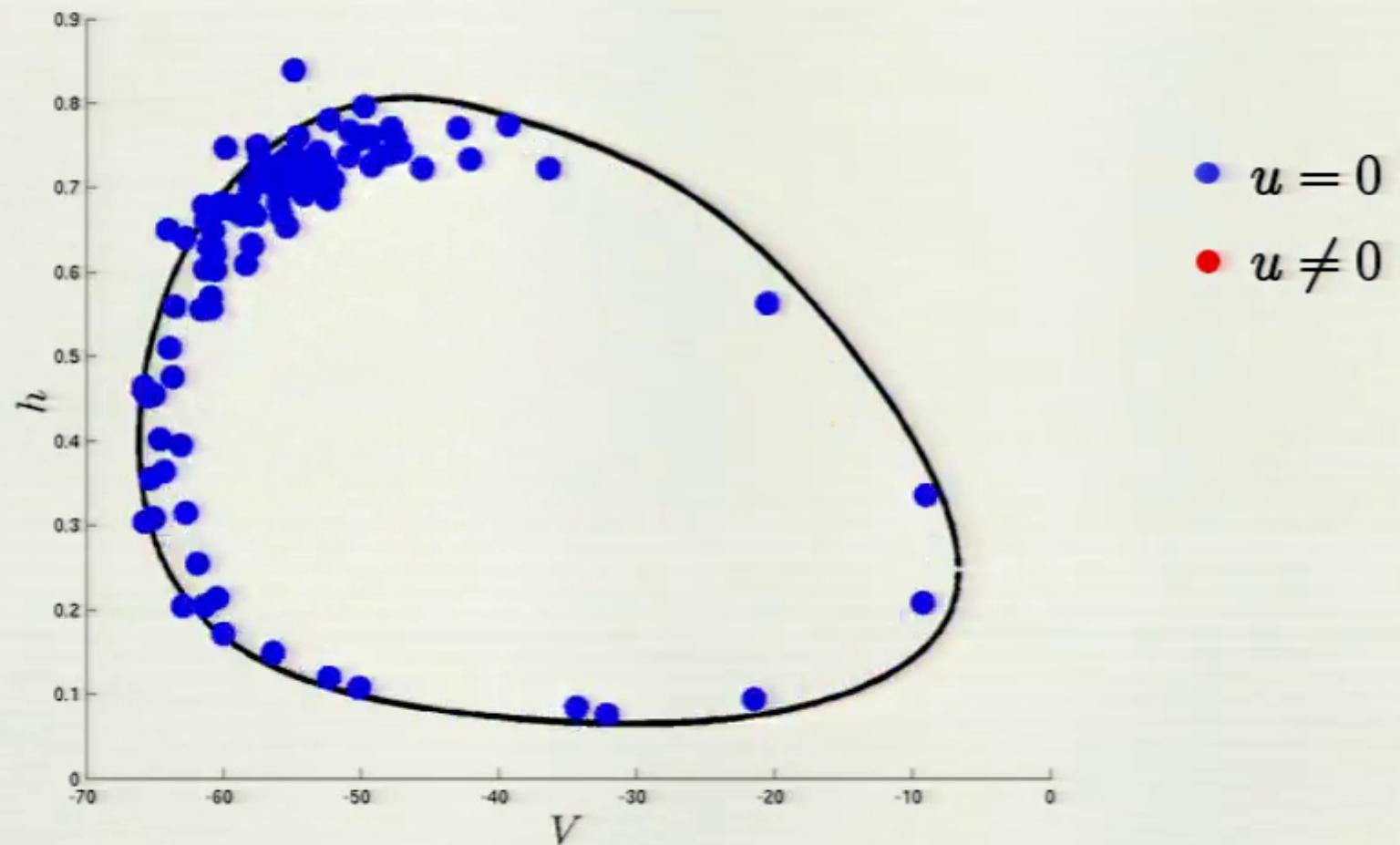


# Chaotic Desync of Thalamic Neurons



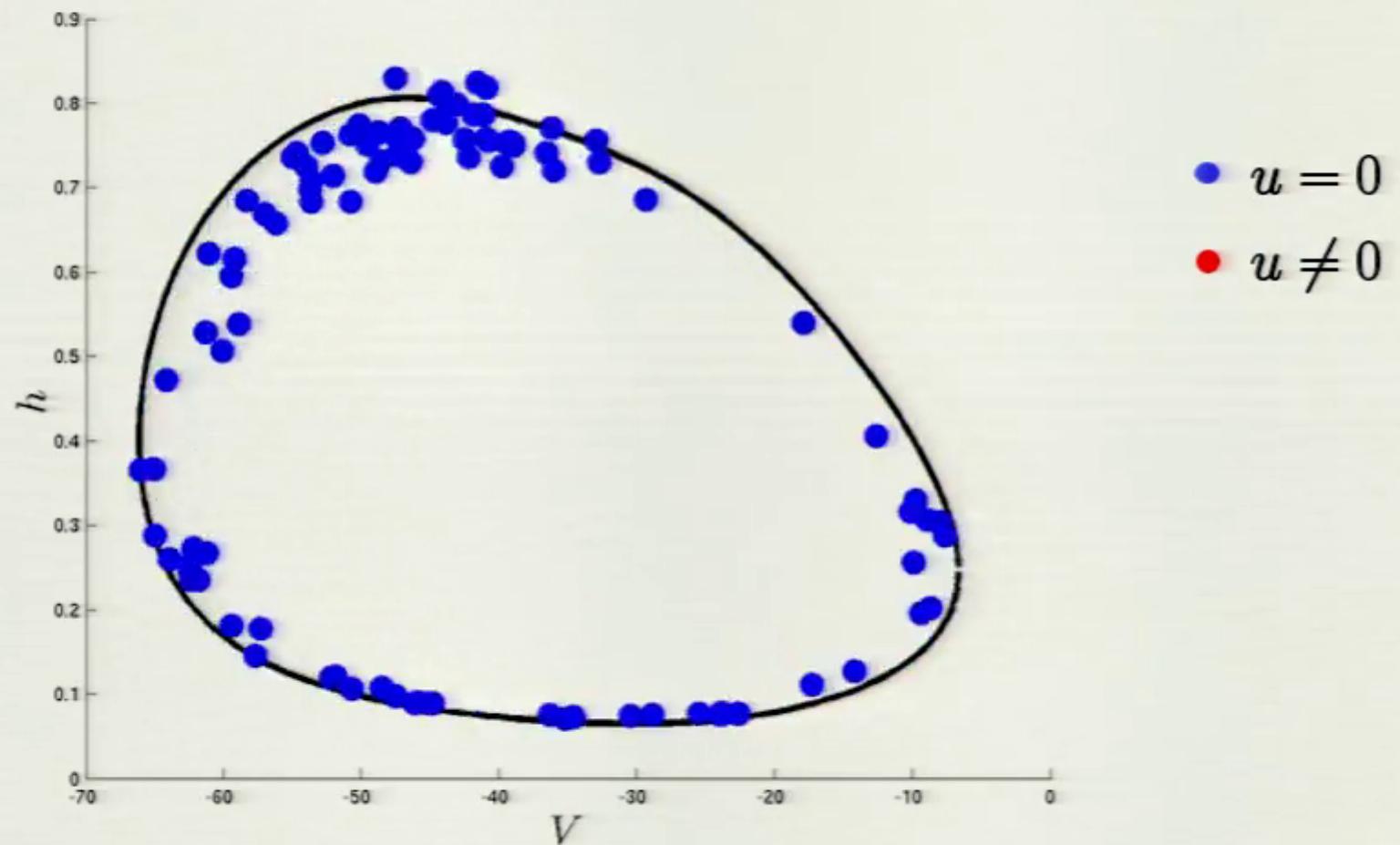


# Chaotic Desync of Thalamic Neurons



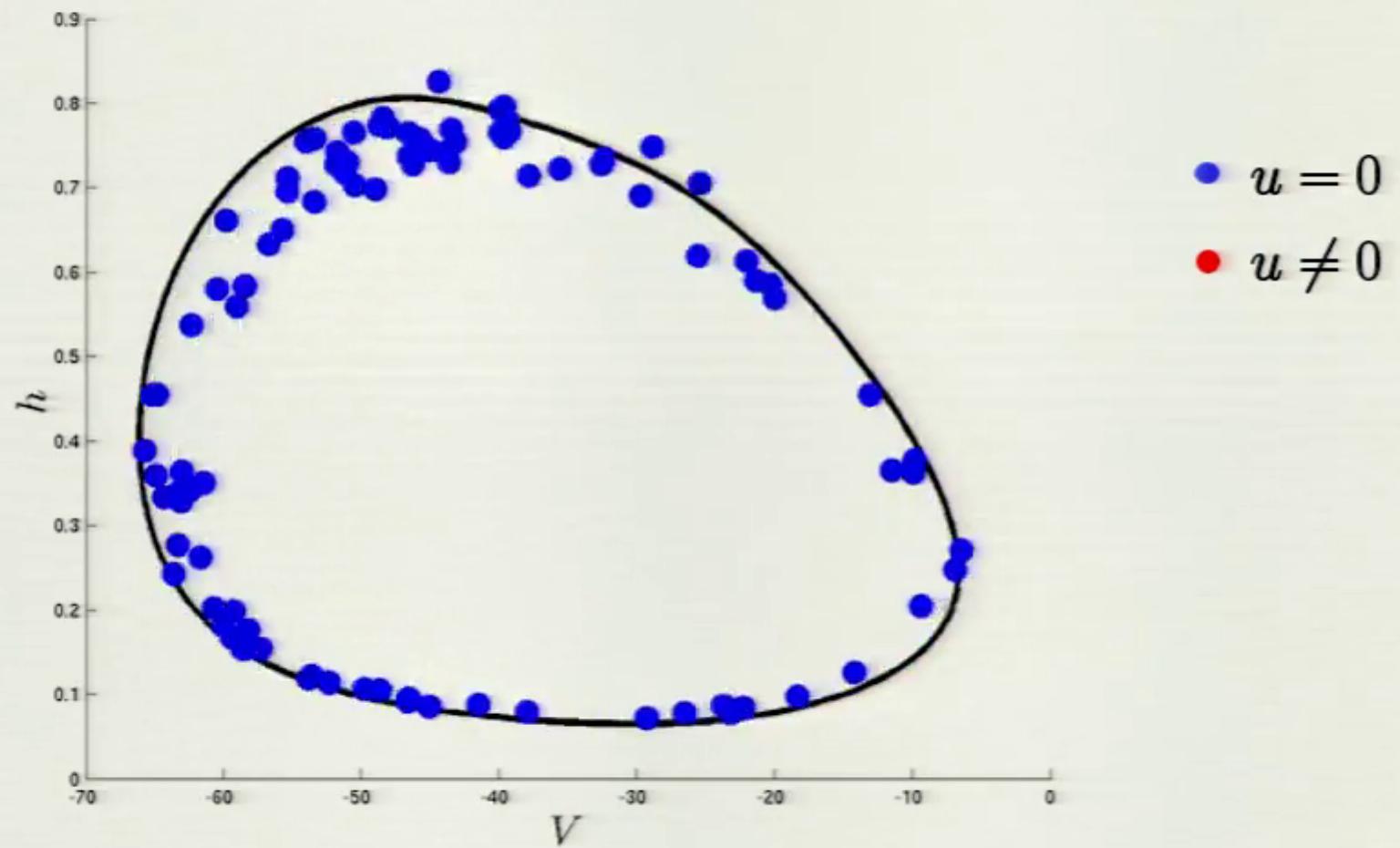


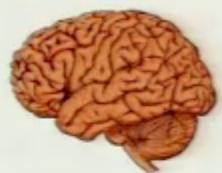
# Chaotic Desync of Thalamic Neurons



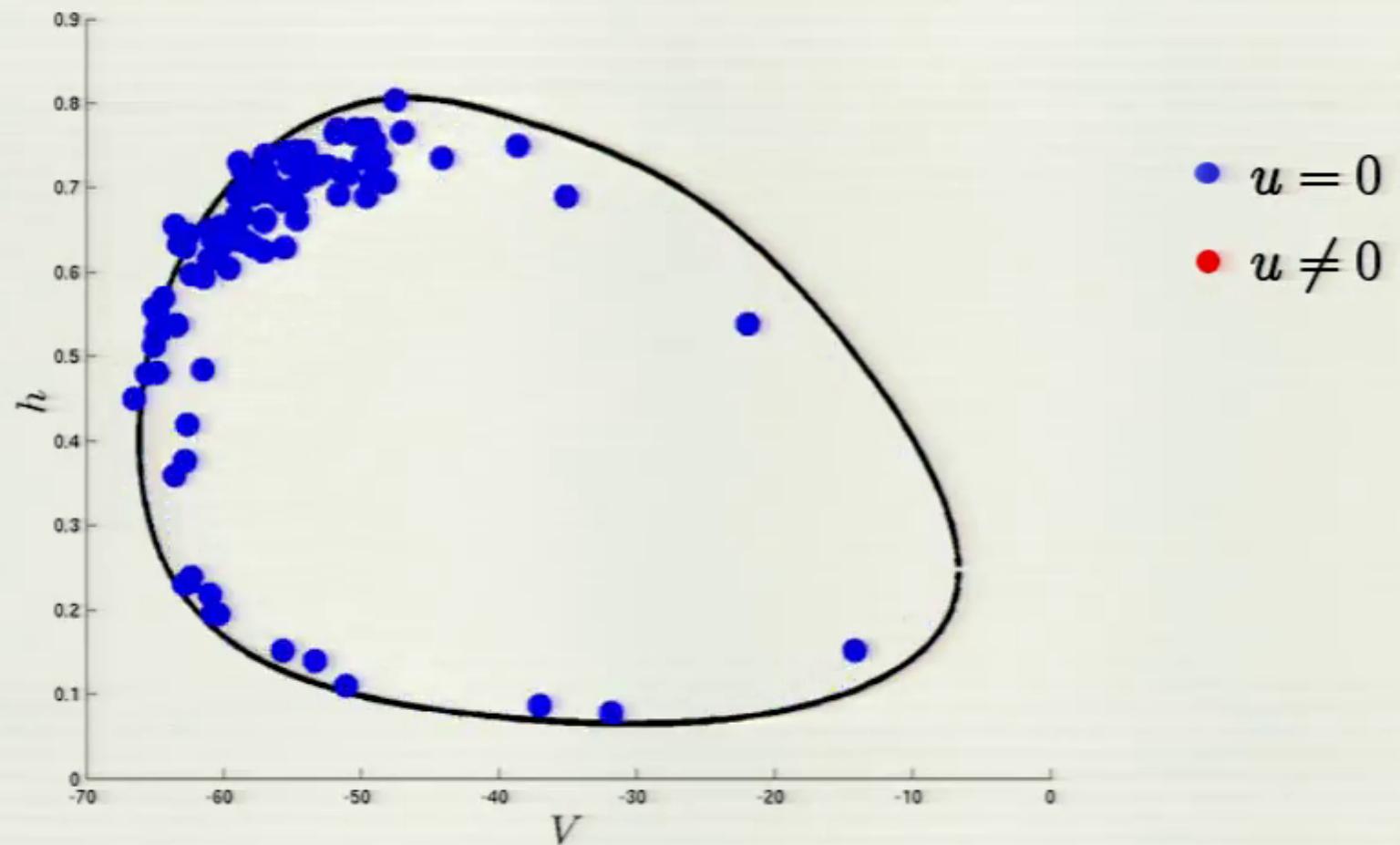


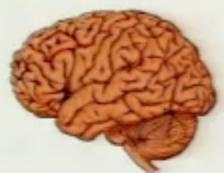
# Chaotic Desync of Thalamic Neurons



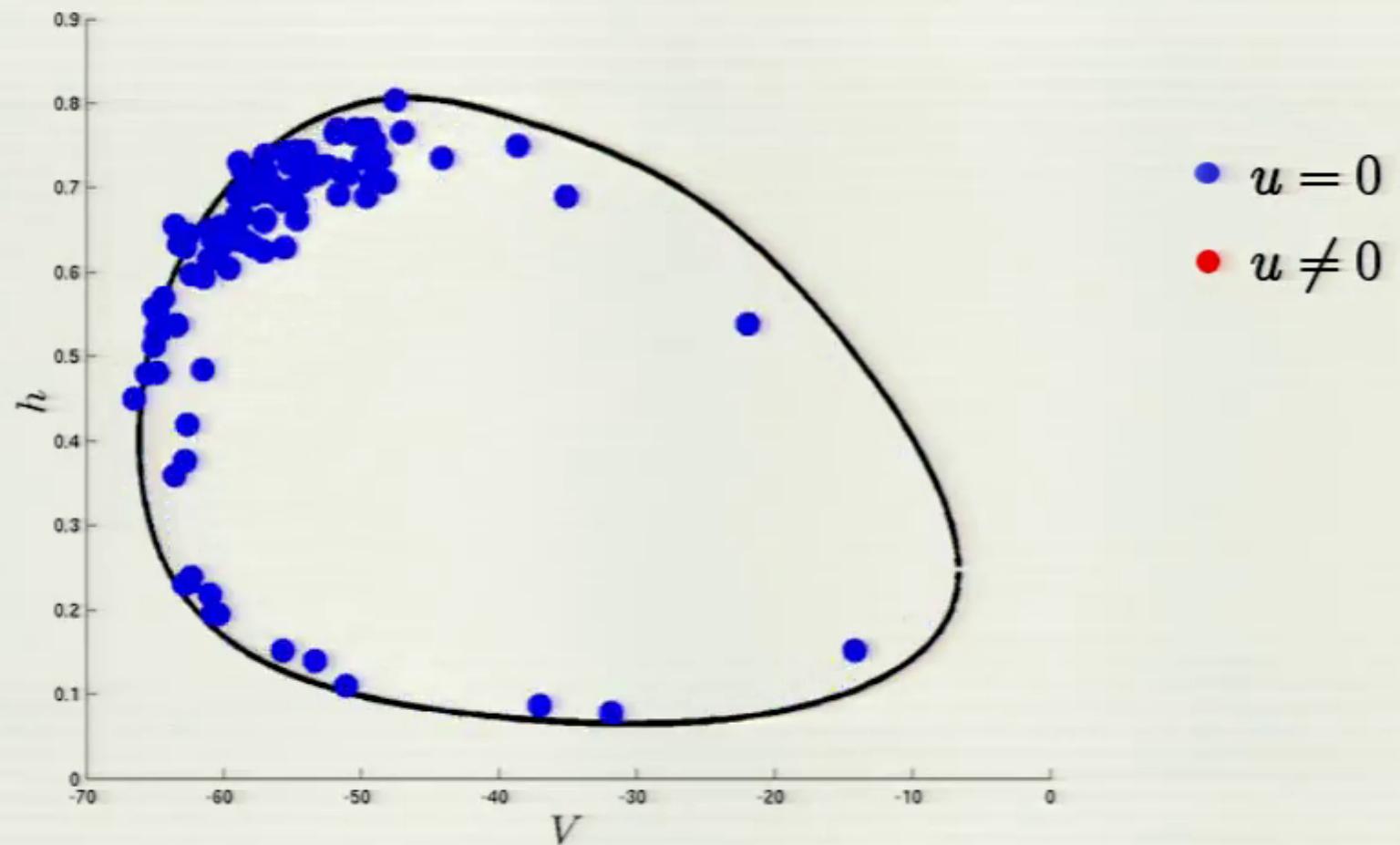


# Chaotic Desync of Thalamic Neurons



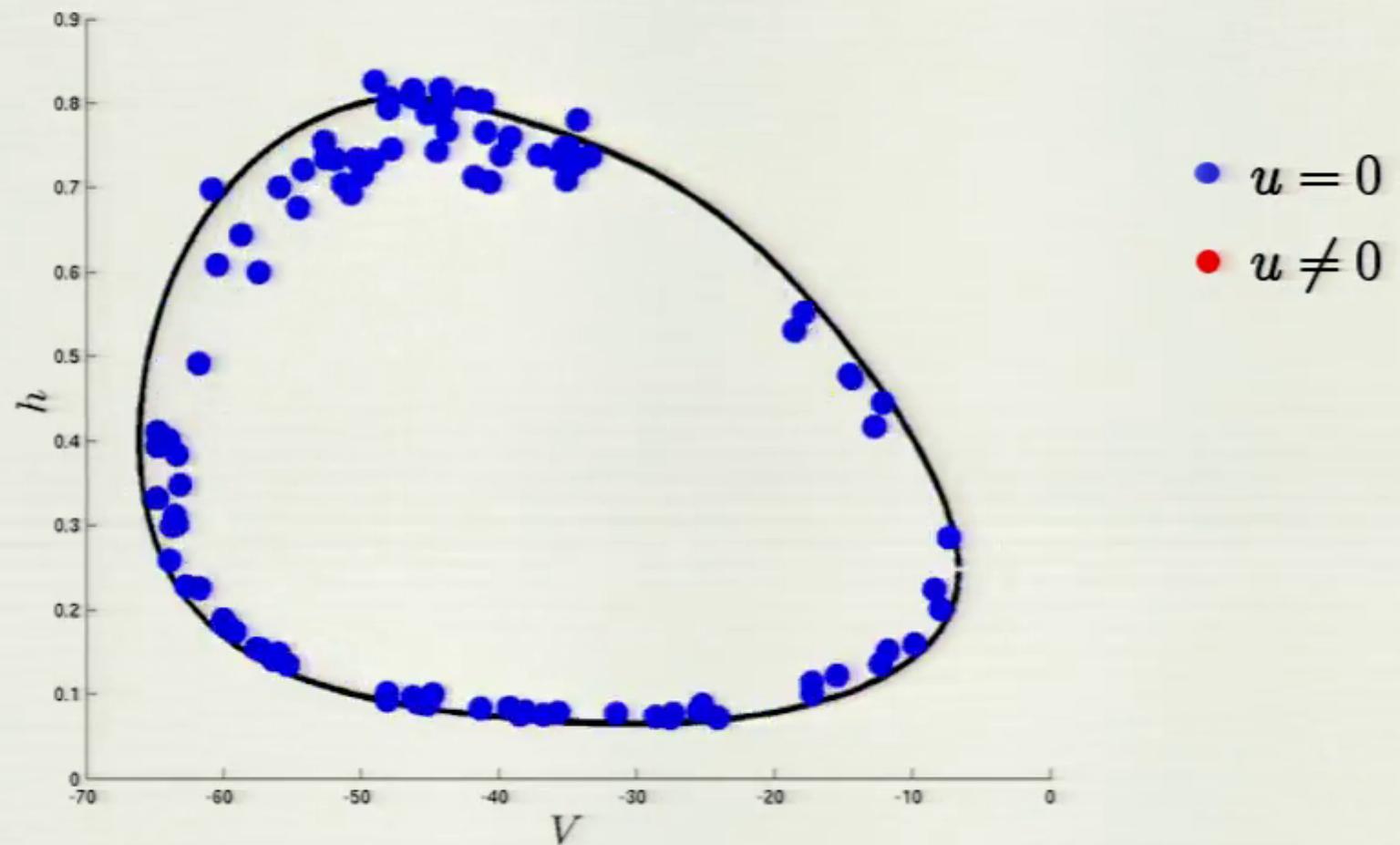


# Chaotic Desync of Thalamic Neurons



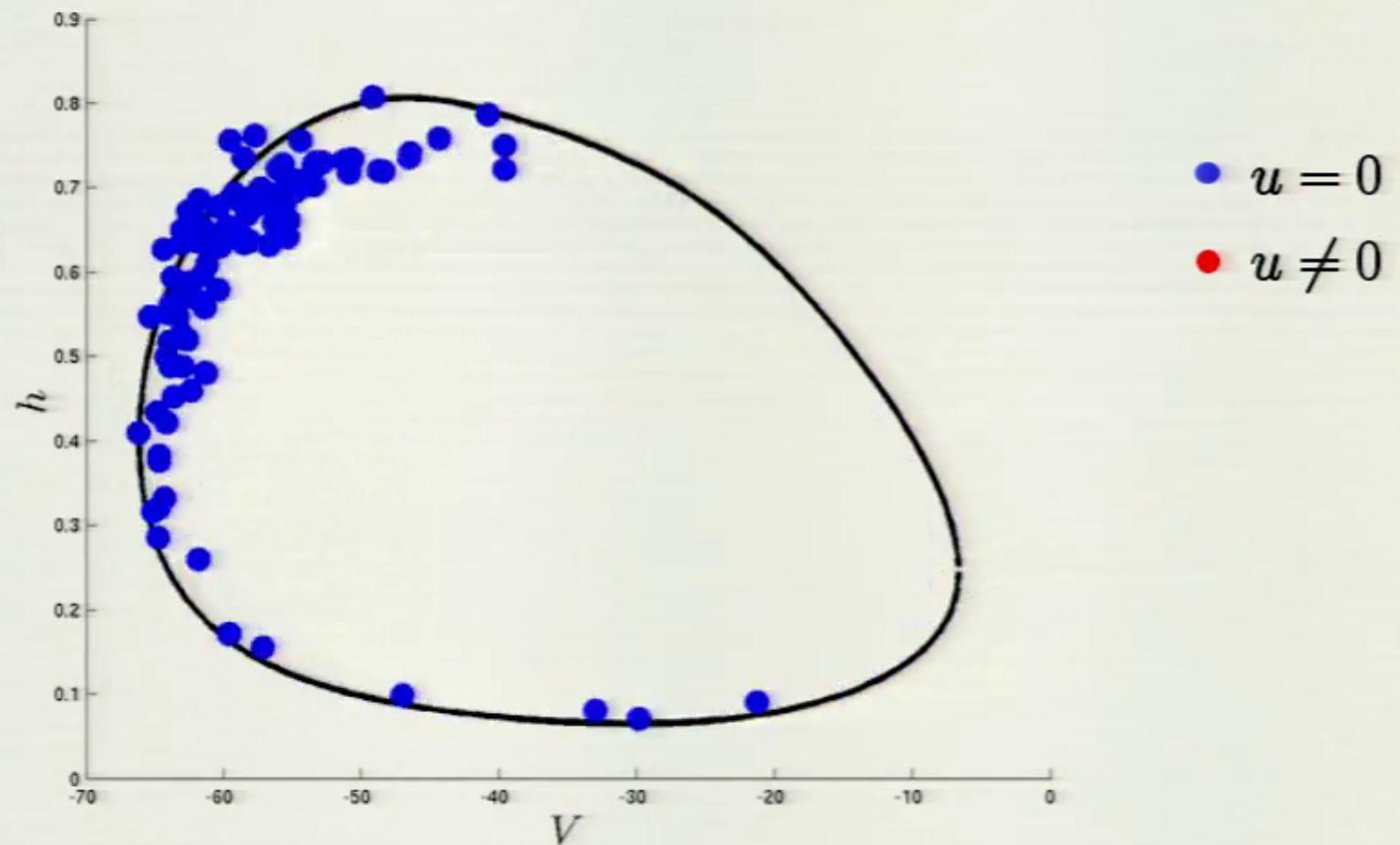


# Chaotic Desync of Thalamic Neurons



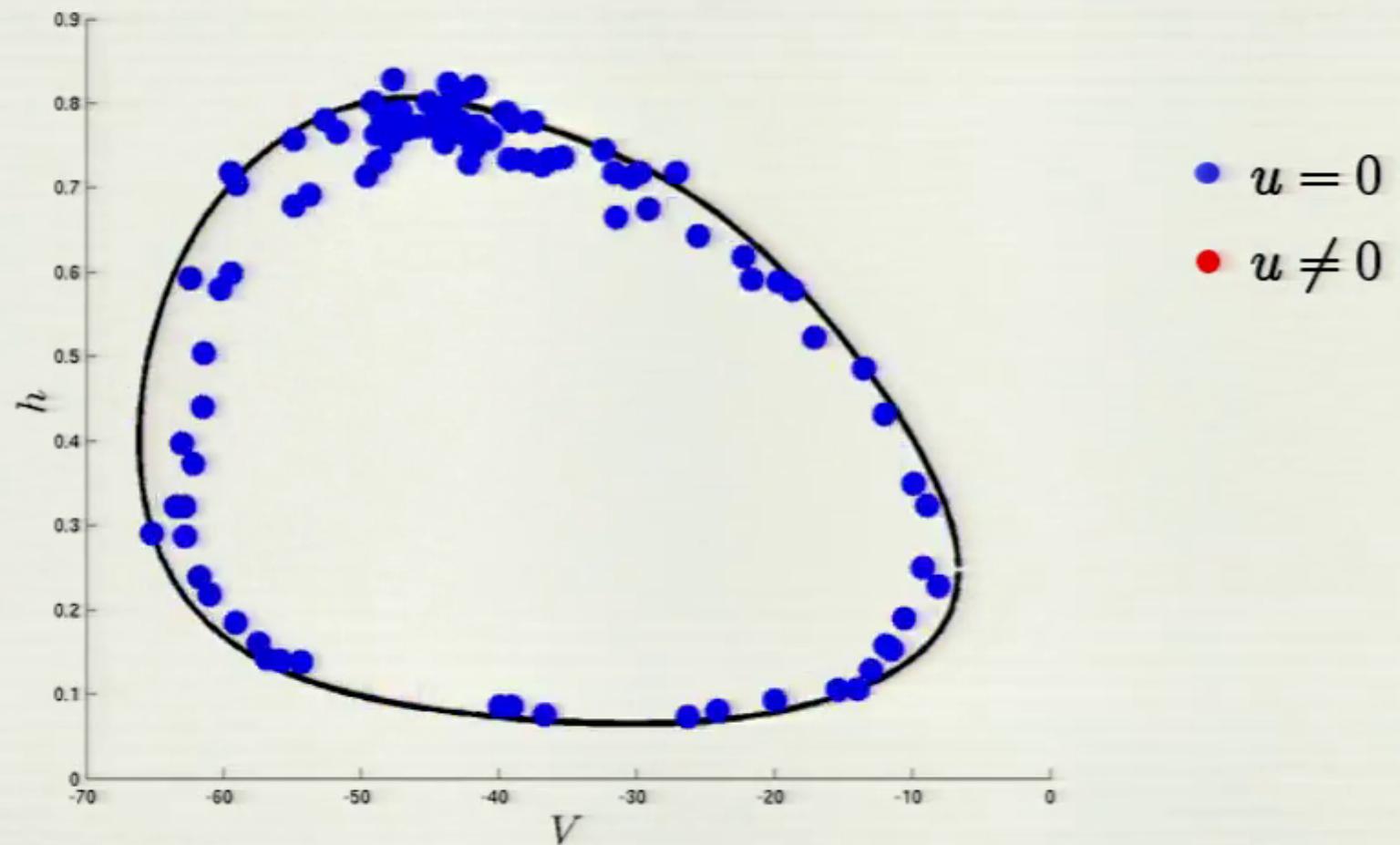


# Chaotic Desync of Thalamic Neurons



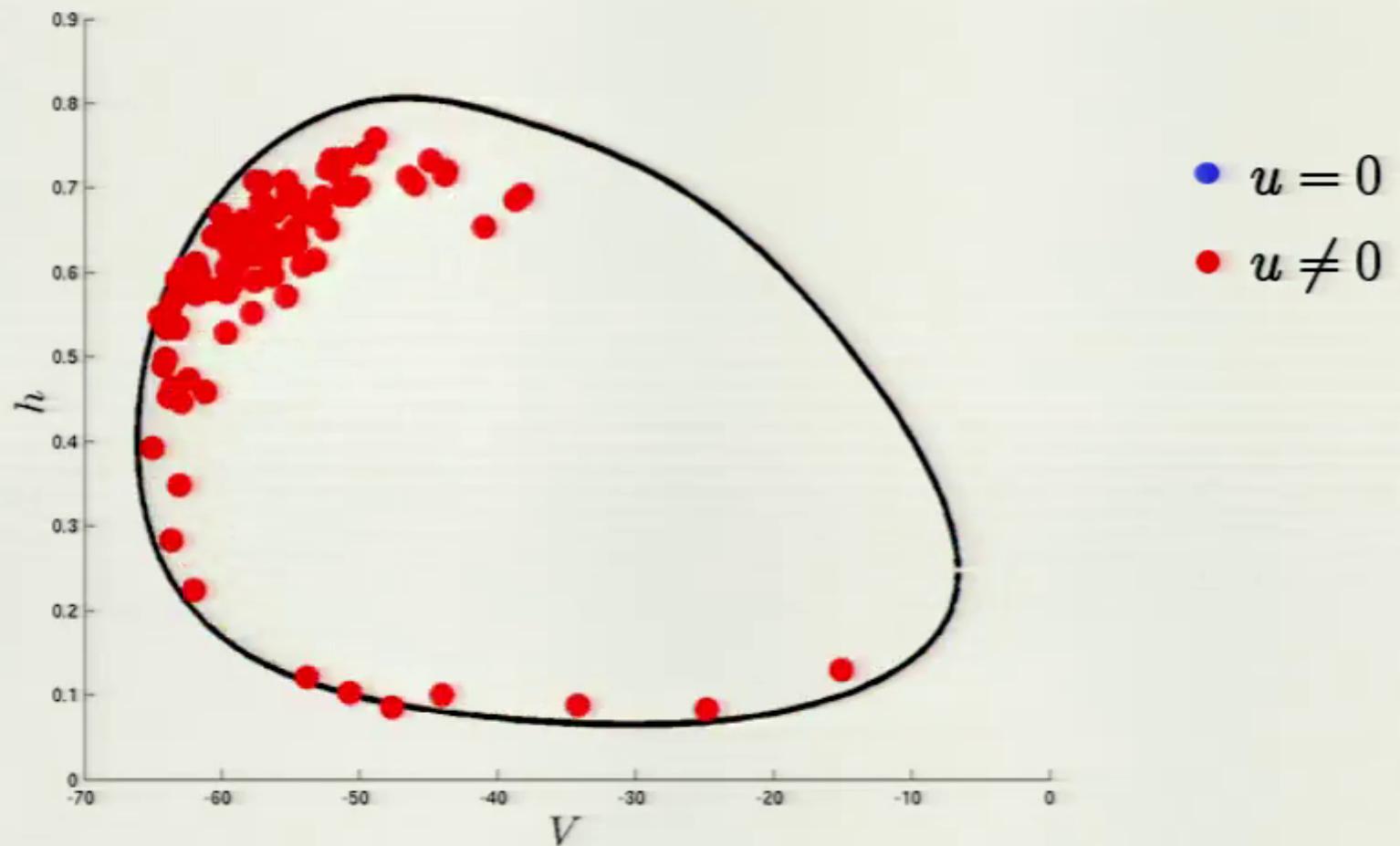


# Chaotic Desync of Thalamic Neurons



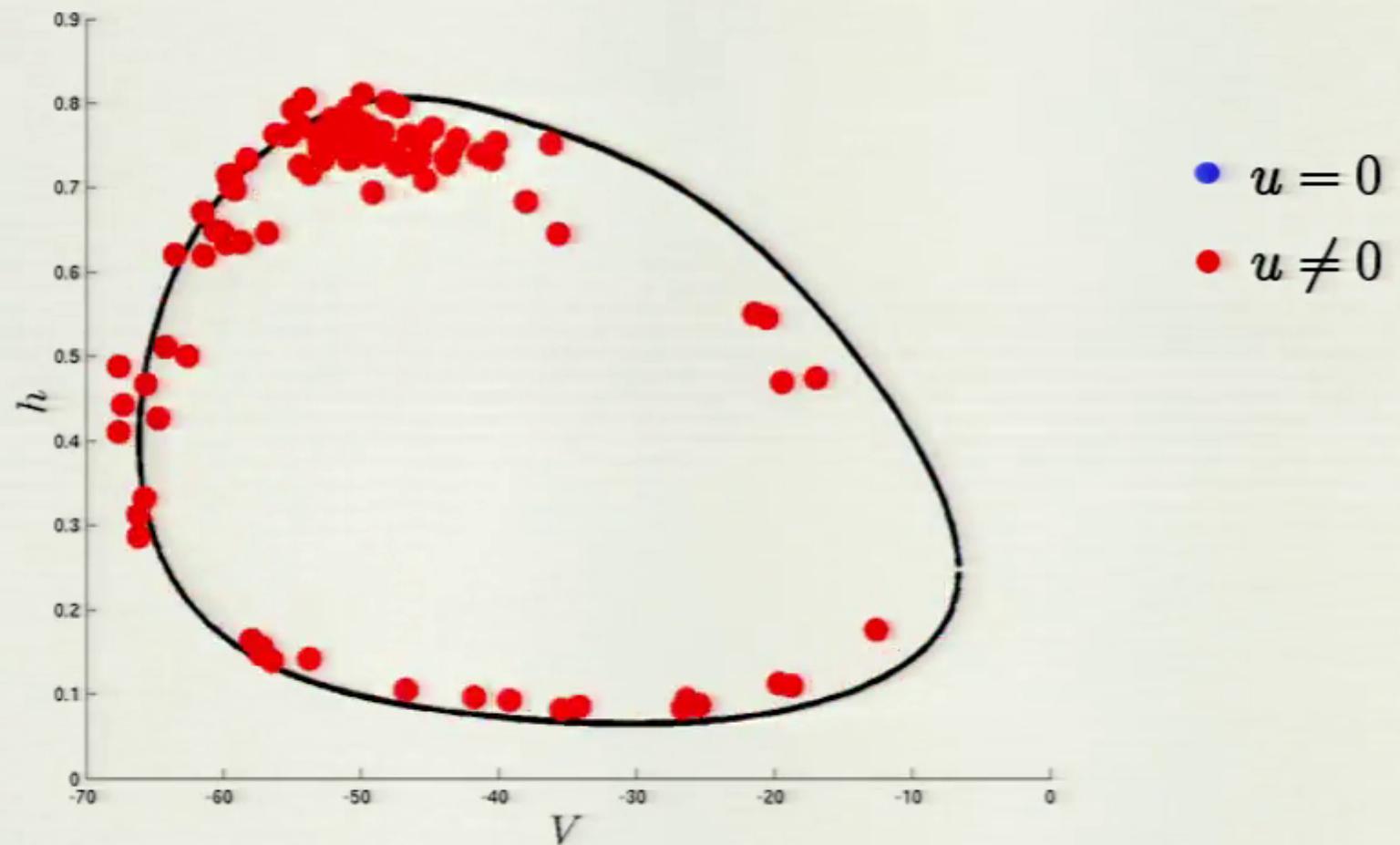


# Chaotic Desync of Thalamic Neurons



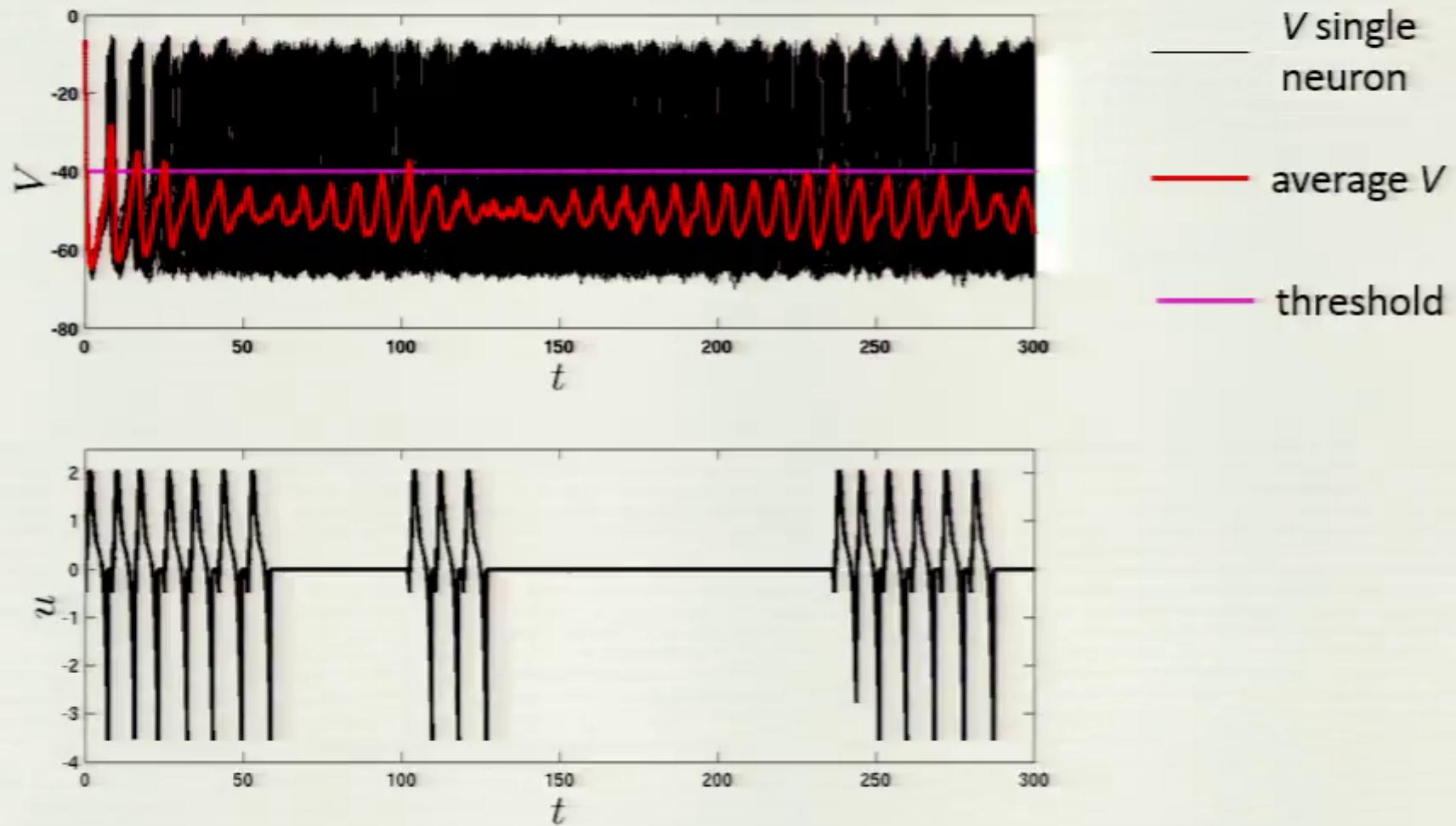


# Chaotic Desync of Thalamic Neurons

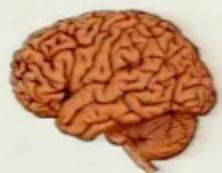




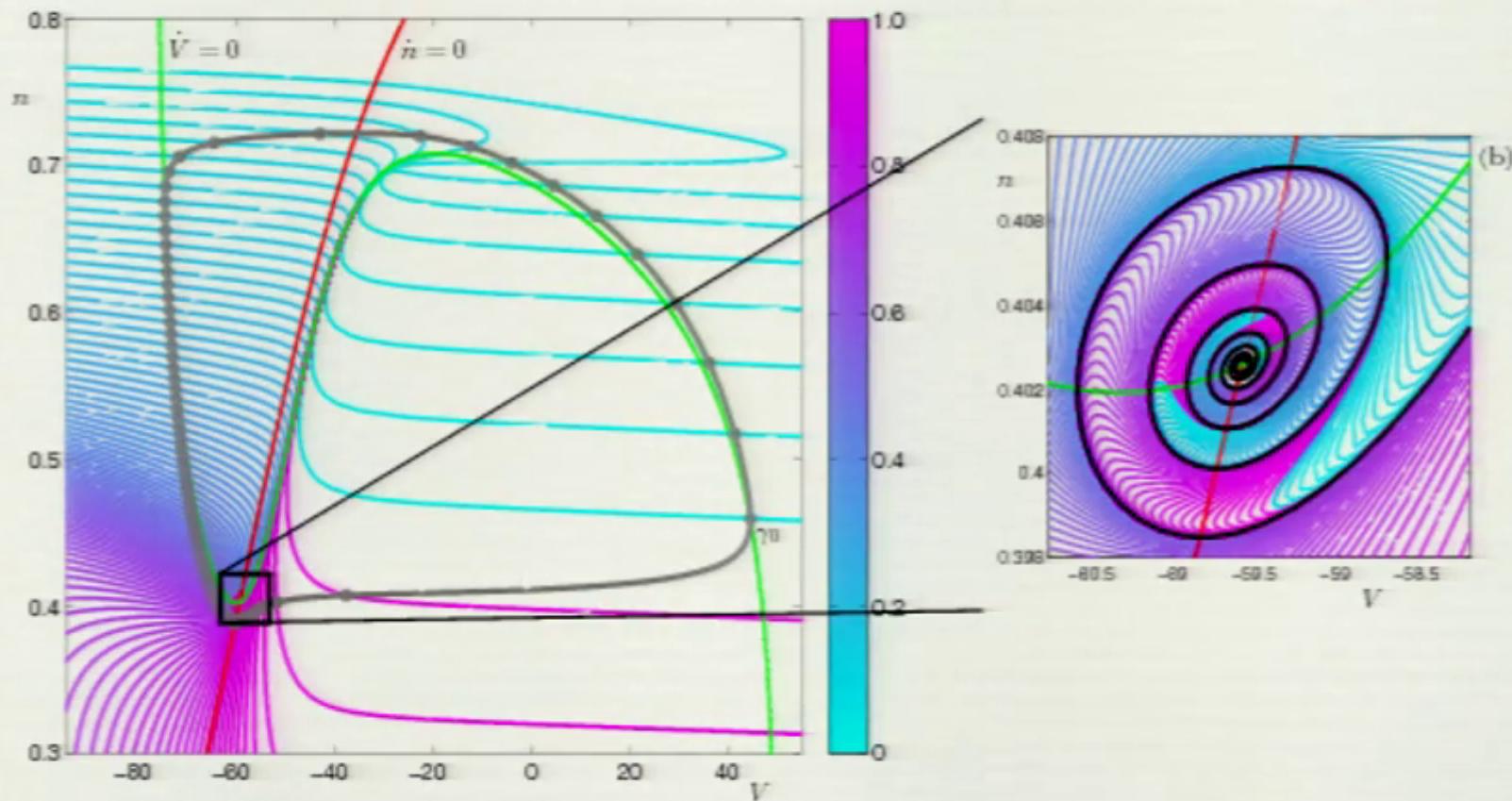
# Chaotic Desync of Thalamic Neurons



Wilson, M – SIADS 2014



# Isochrons Near the Phaseless Set



Osinga, M - SIADS 2010



# Optimal Phase Resetting

$$\frac{d\mathbf{x}}{dt} = \mathbf{F}(\mathbf{x}) + (u(t), 0, 0, \dots)^T, \quad |u(t)| \leq u_{max}$$

**cost function to be minimized:**

$$J(\mathbf{x}, u(t)) = \int_0^{T_{end}} u^2 dt + \gamma q(\mathbf{x}(T_{end}))$$

*q* is end-point cost

**Hamilton-Jacobi-Bellman equation:**

$$\frac{\partial V}{\partial t} + \min_{|u| \leq u_{max}} [u^2 + \nabla V(\mathbf{x}, t)(\mathbf{F}(\mathbf{x}) + (u(t), 0, 0, \dots)^T)] = 0$$

$$u^*(t) = \arg \min_{|u| \leq u_{max}} [u^2 + \nabla V(\mathbf{x}^*, t)(\mathbf{F}(\mathbf{x}^*) + (u(t), 0, 0, \dots)^T)]$$

where  $\mathbf{x}^*(t)$  is optimal trajectory



# Optimal Phase Resetting

$$\frac{d\mathbf{x}}{dt} = \mathbf{F}(\mathbf{x}) + (u(t), 0, 0, \dots)^T, \quad |u(t)| \leq u_{max}$$

**cost function to be minimized:**

$$J(\mathbf{x}, u(t)) = \int_0^{T_{end}} u^2 dt + \gamma q(\mathbf{x}(T_{end}))$$

*q* is end-point cost

**Hamilton-Jacobi-Bellman equation:**

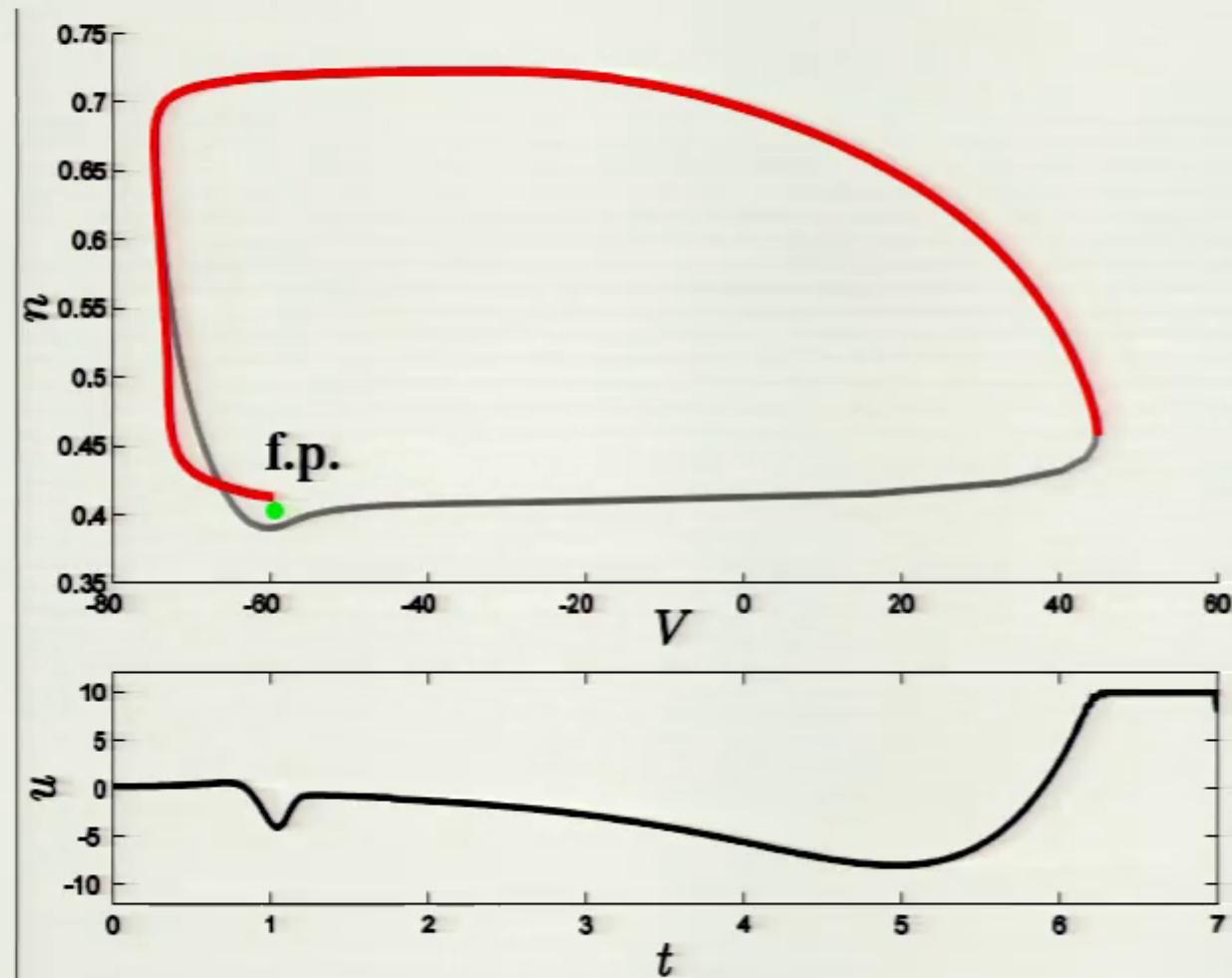
$$\frac{\partial V}{\partial t} + \min_{|u| \leq u_{max}} [u^2 + \nabla V(\mathbf{x}, t)(\mathbf{F}(\mathbf{x}) + (u(t), 0, 0, \dots)^T)] = 0$$

$$u^*(t) = \arg \min_{|u| \leq u_{max}} [u^2 + \nabla V(\mathbf{x}^*, t)(\mathbf{F}(\mathbf{x}^*) + (u(t), 0, 0, \dots)^T)]$$

where  $\mathbf{x}^*(t)$  is optimal trajectory

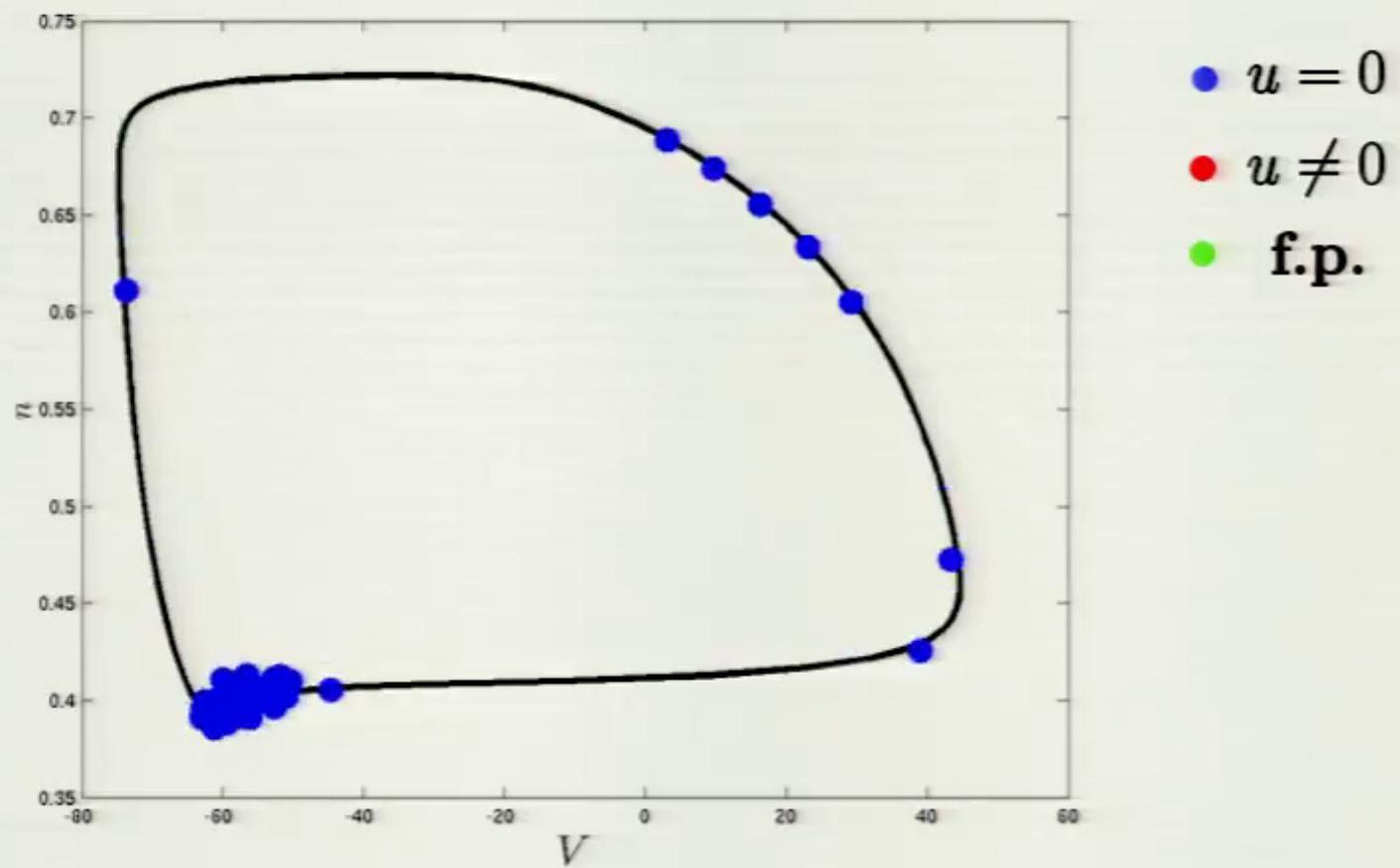


# Optimal Phase Resetting



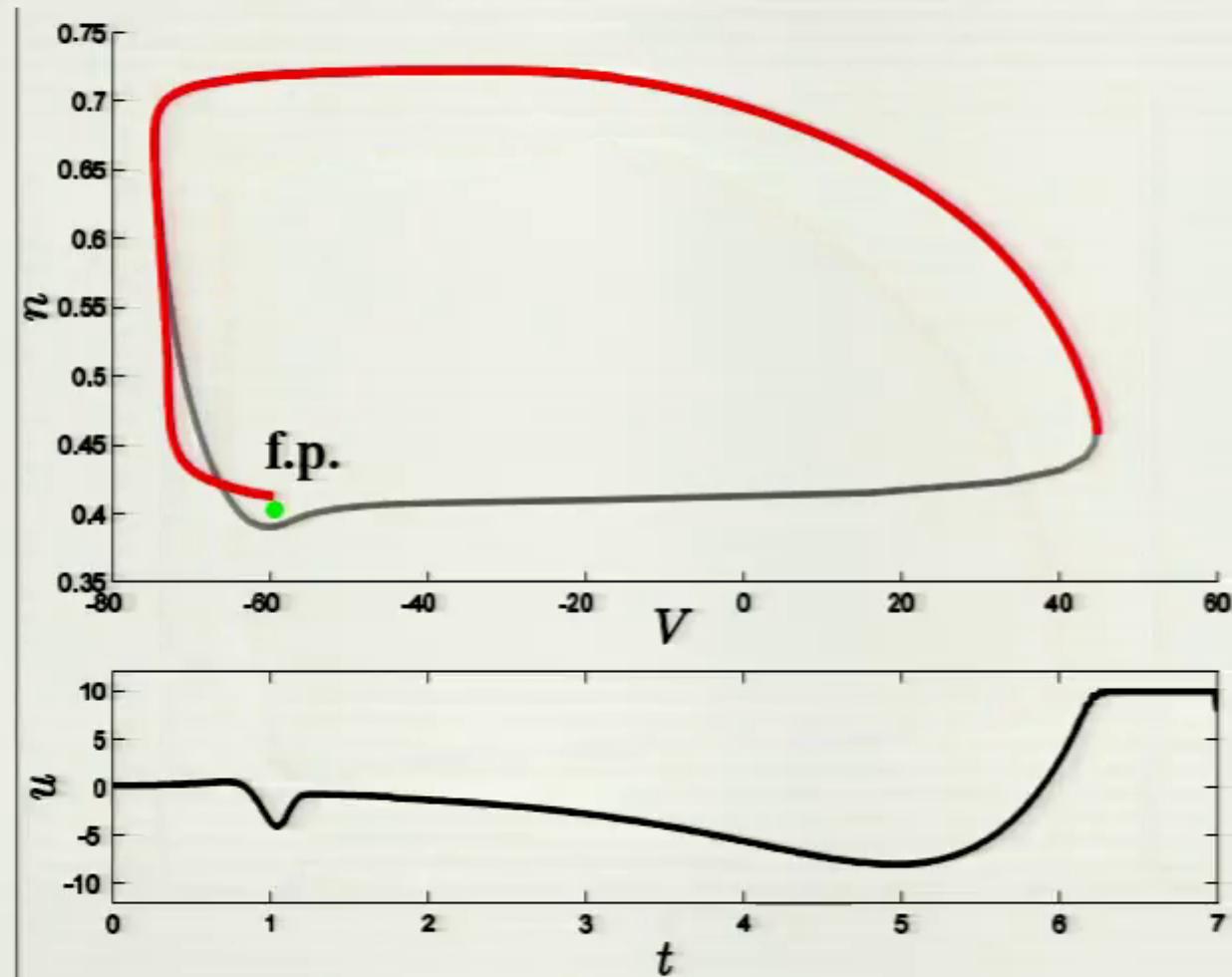


# Coupled, Noisy Neurons – Phase Resetting



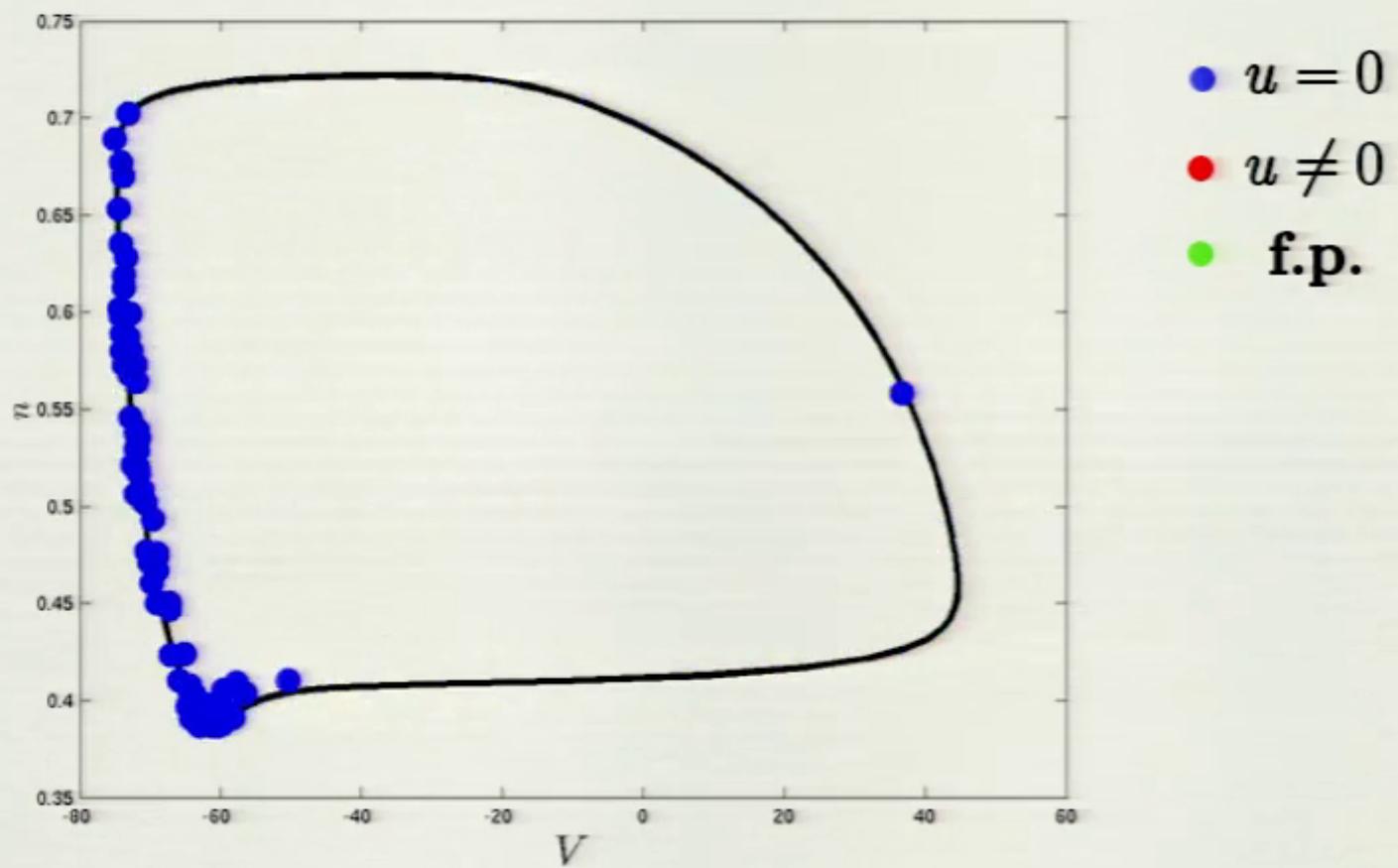


# Optimal Phase Resetting



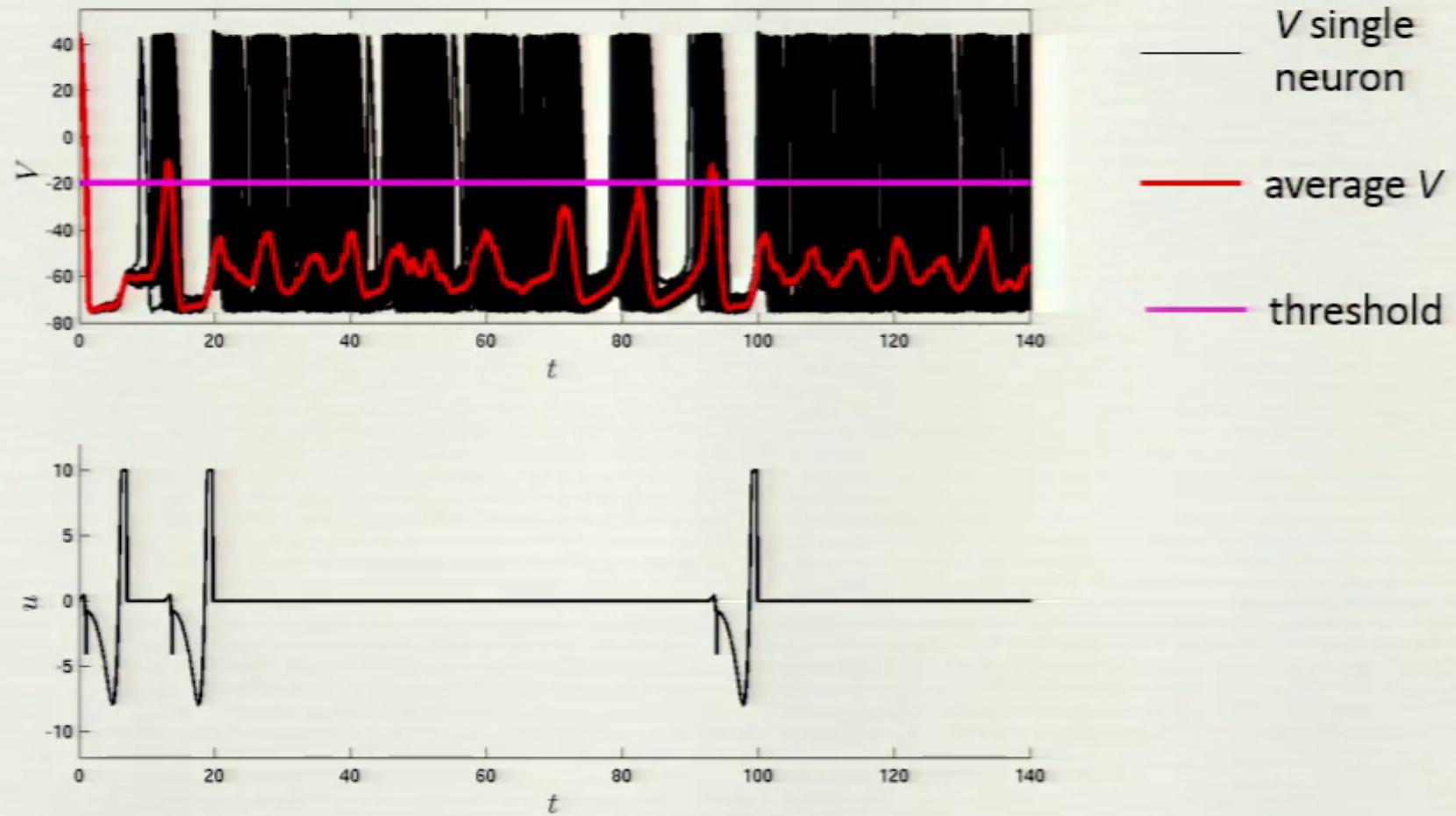


# Coupled, Noisy Neurons – Phase Resetting



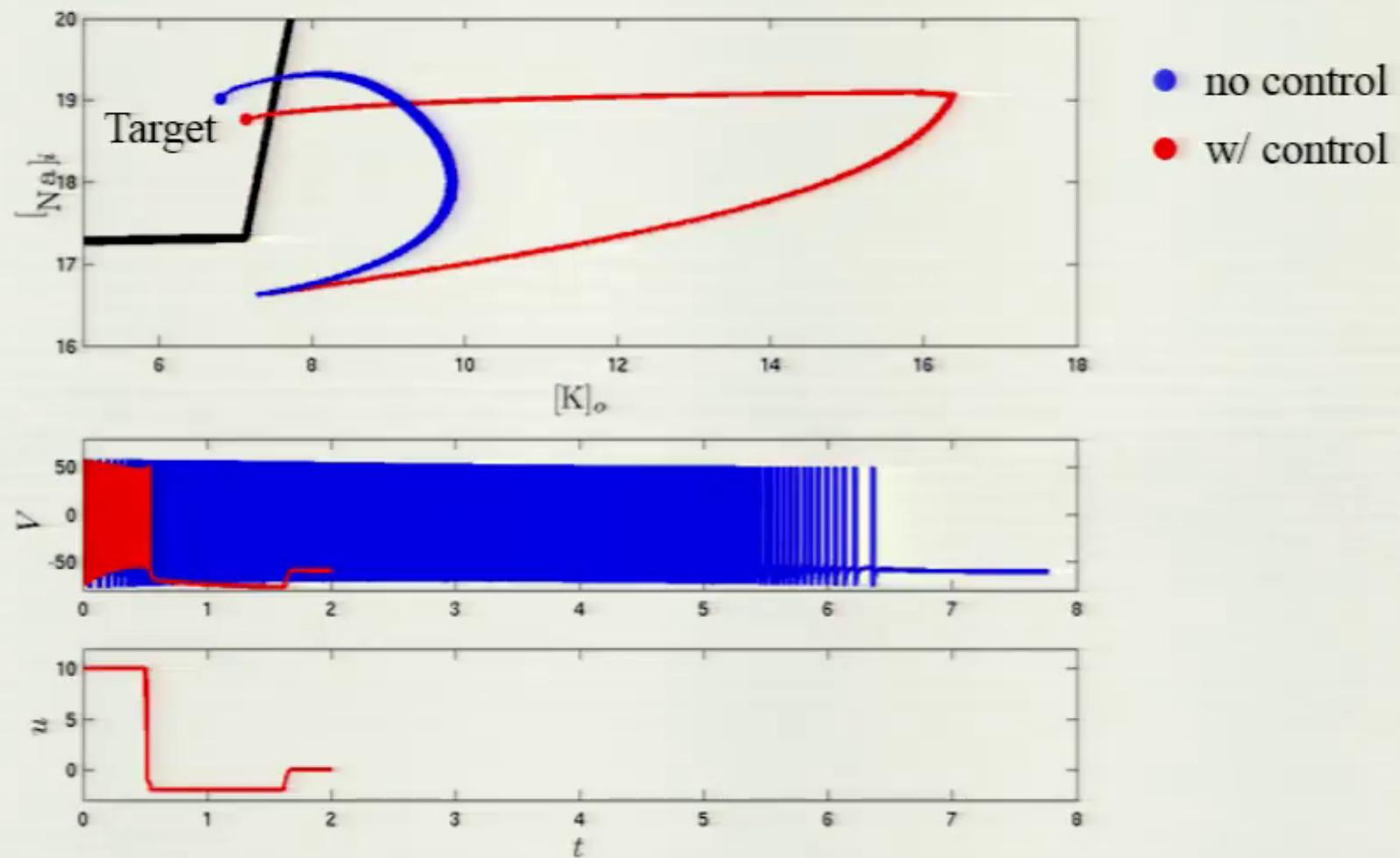


# Coupled, Noisy Neurons – Phase Resetting



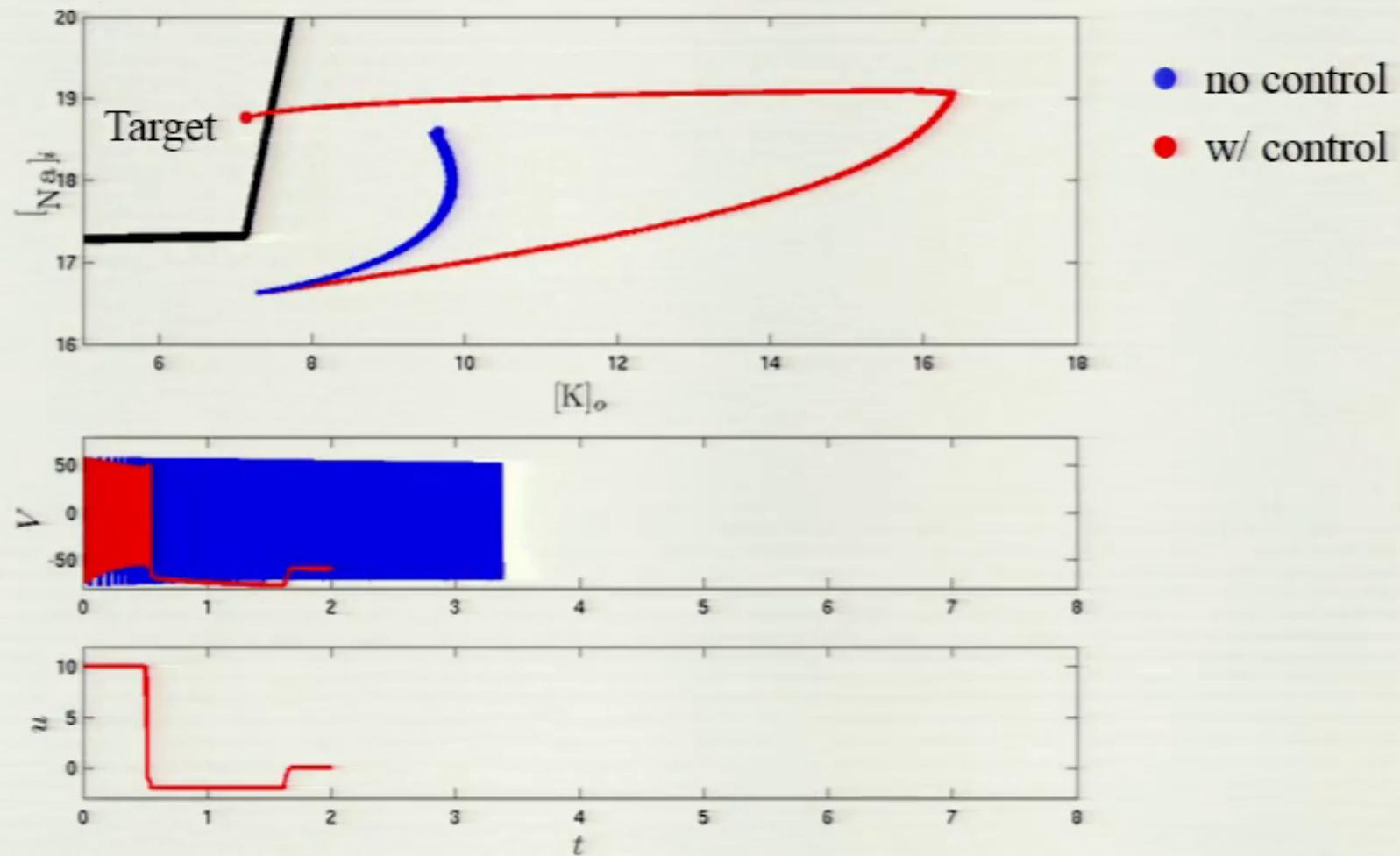


# Control of Seizure-like Bursting





# Control of Seizure-like Bursting



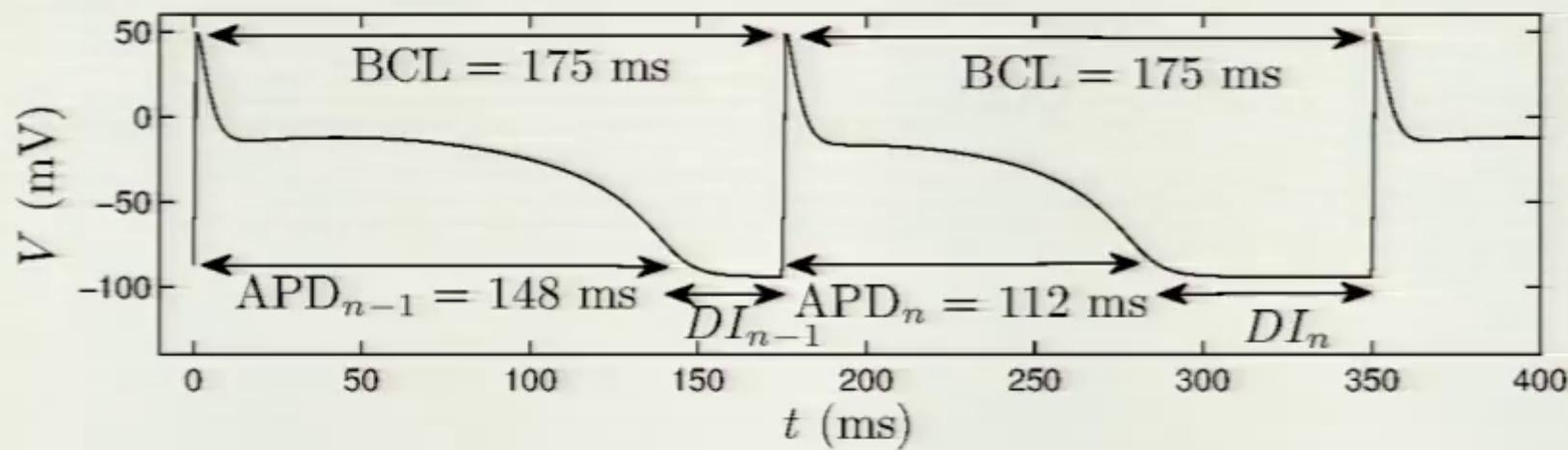


# Cardiac Dynamics

- excitable cells, not oscillators
  - driven by sinoatrial node, which acts as a pacemaker
- cardiac arrhythmias – irregular heartbeat
  - **alternans**: beat-to-beat alternation of cardiac dynamics
  - **fibrillation**: rapid, irregular contraction of heart muscle fibers
    - typically associated with spiral waves



# Alternans



BCL = Basic Cycle Length

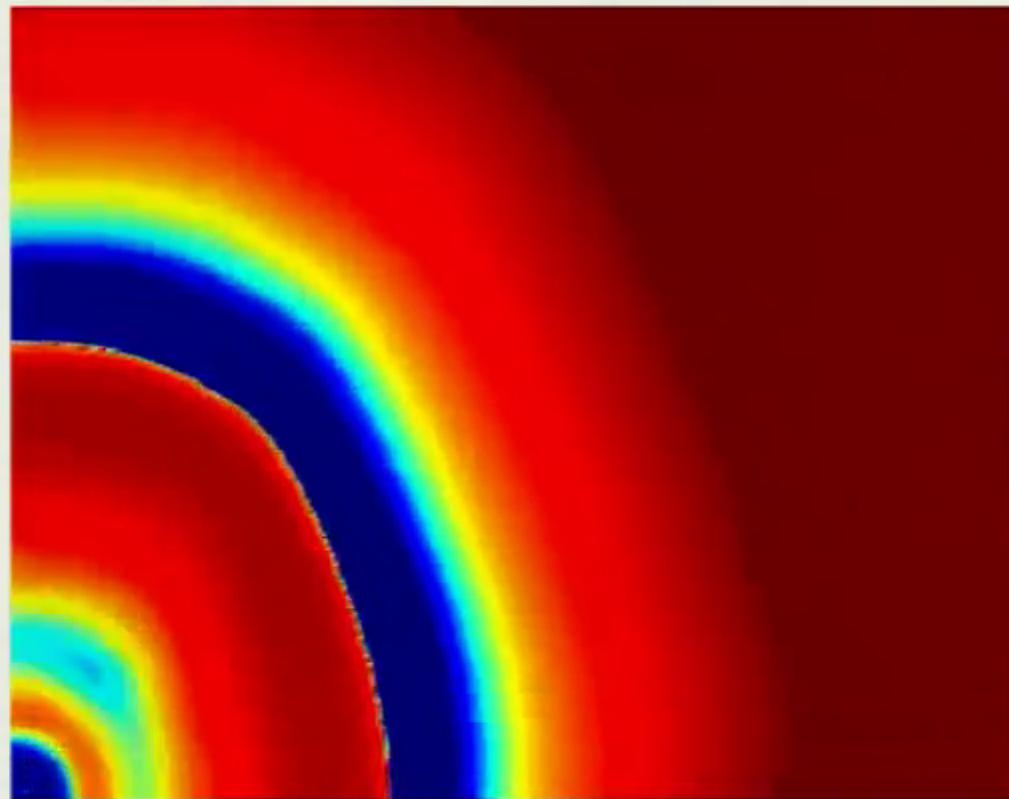
APD = Action Potential Duration

DI = Diastolic Interval



# Alternans: Possible Precursor to fibrillation

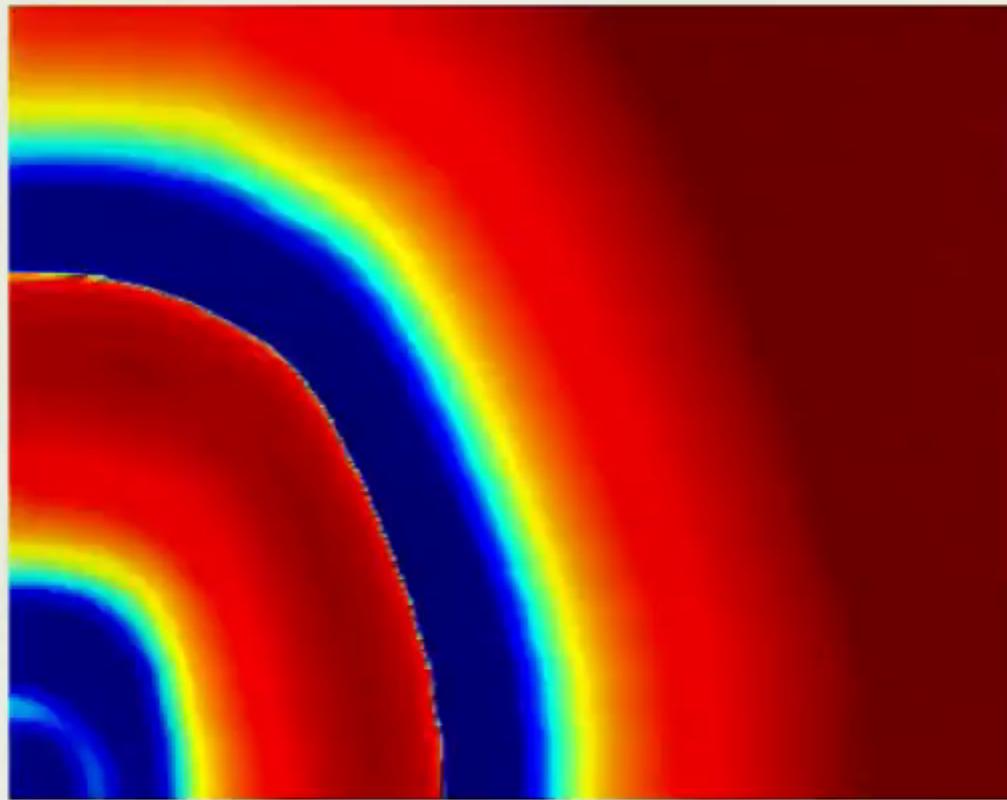
$t = 474$





# Alternans: Possible Precursor to fibrillation

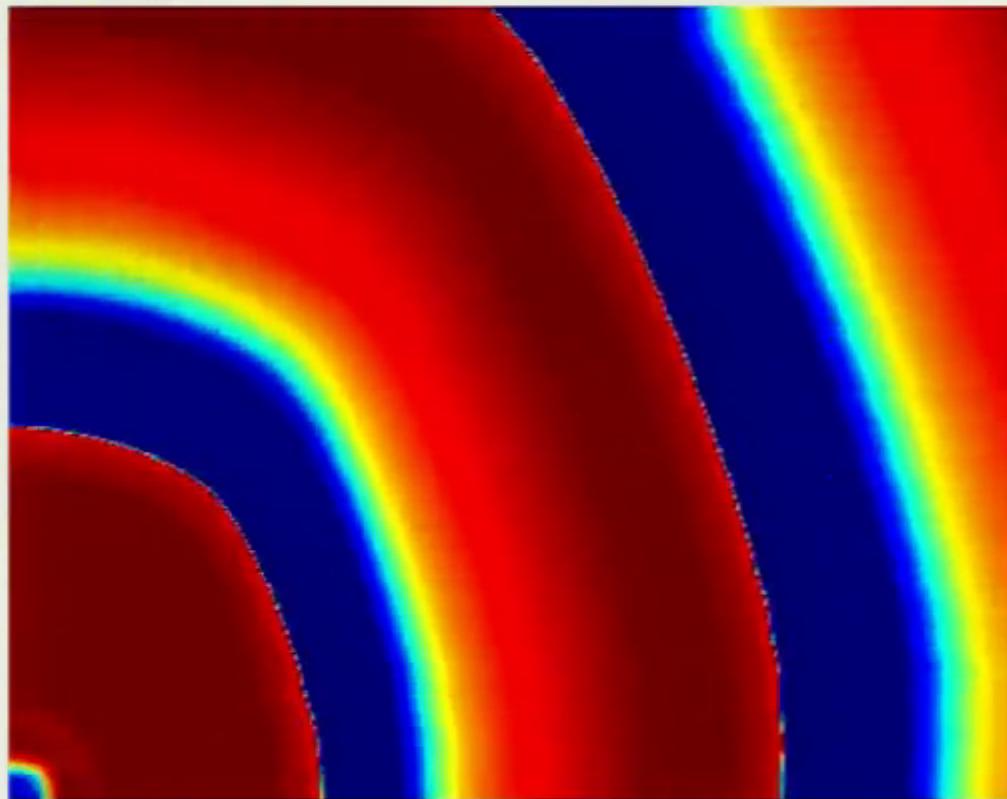
$t = 502$





# Alternans: Possible Precursor to fibrillation

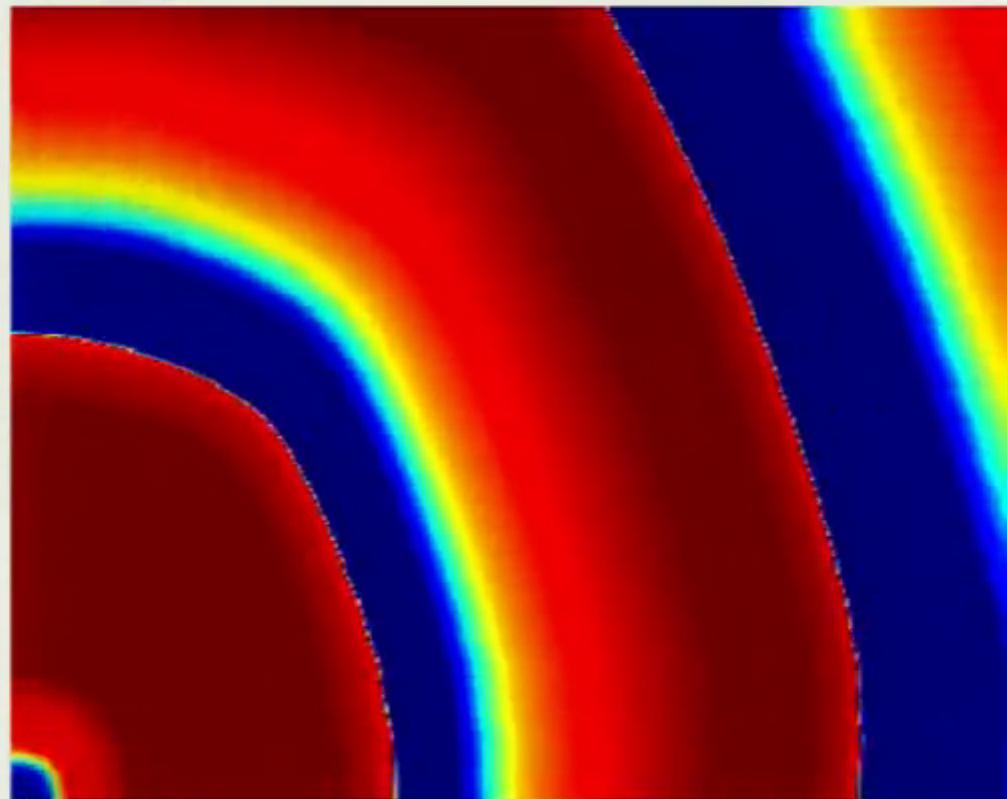
$t = 654$





# Alternans: Possible Precursor to fibrillation

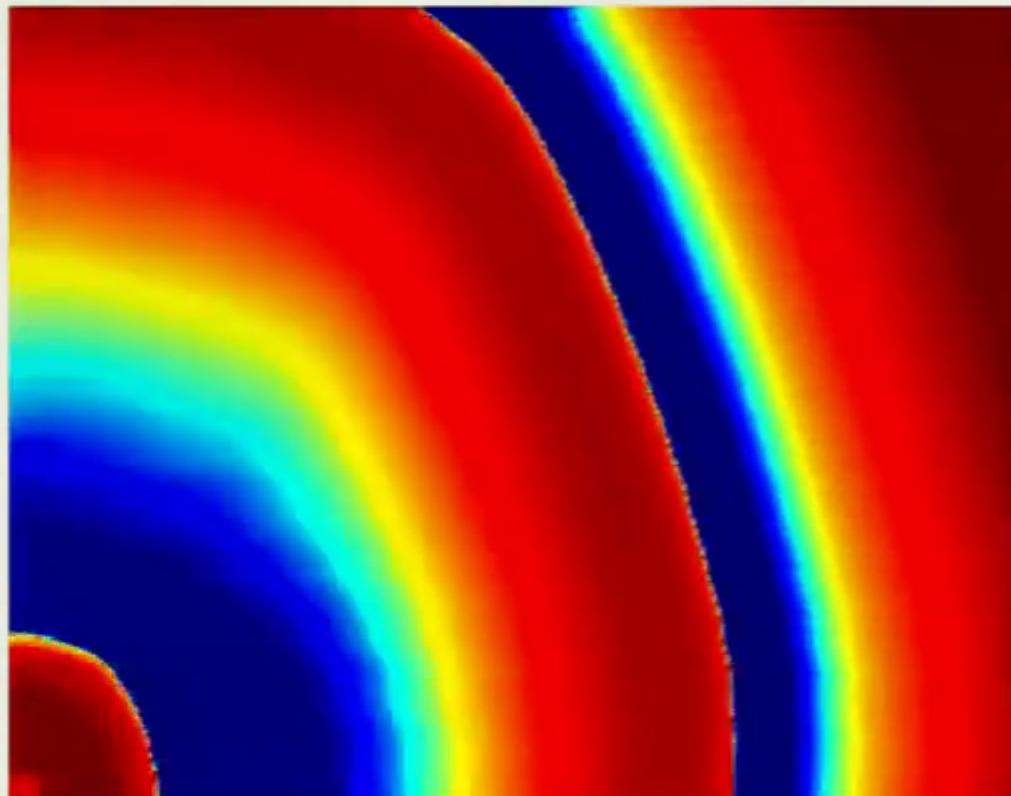
$t = 686$





# Alternans: Possible Precursor to fibrillation

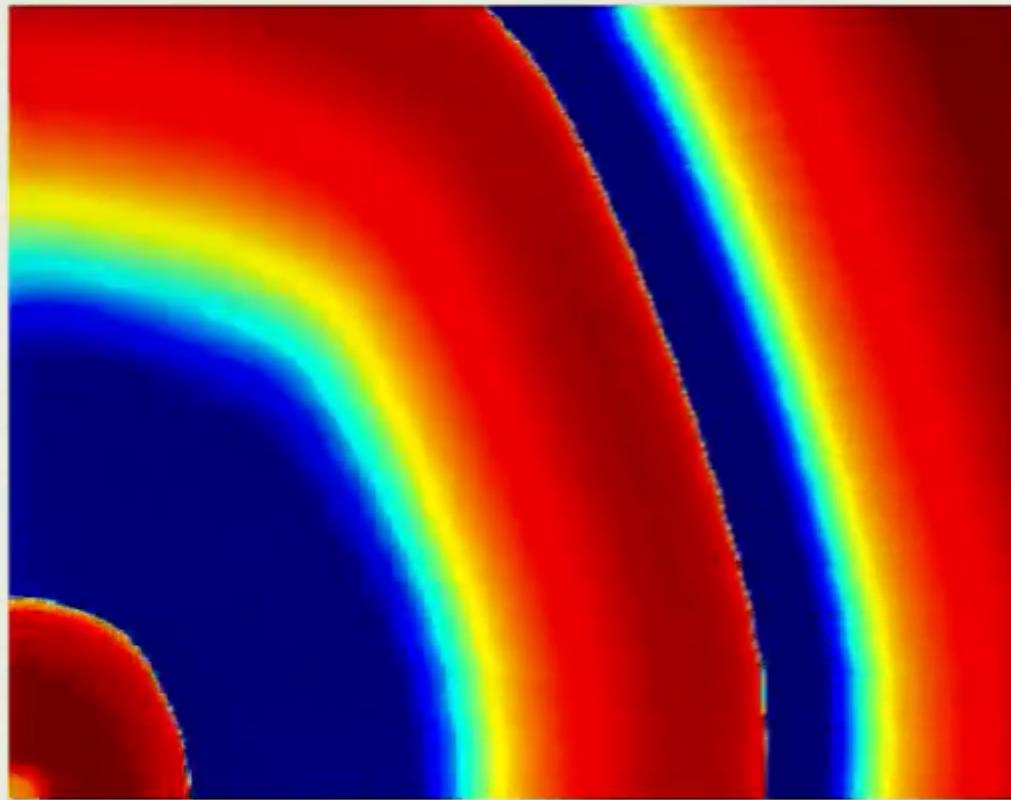
$t = 862$





# Alternans: Possible Precursor to fibrillation

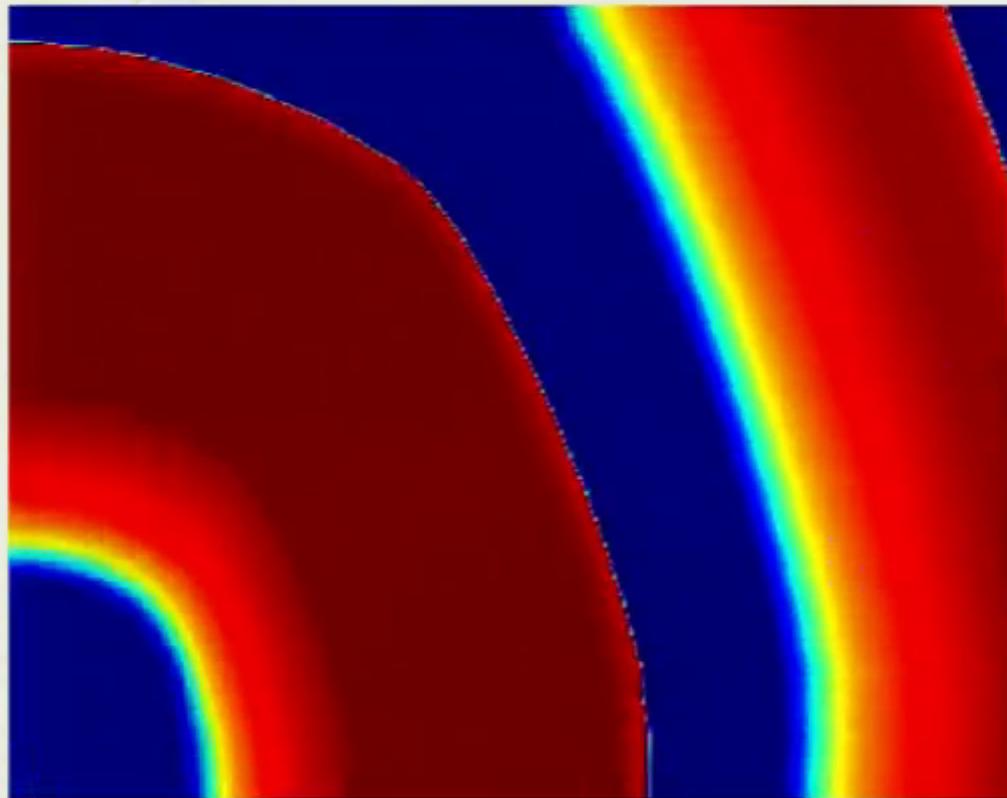
$t = 878$





# Alternans: Possible Precursor to fibrillation

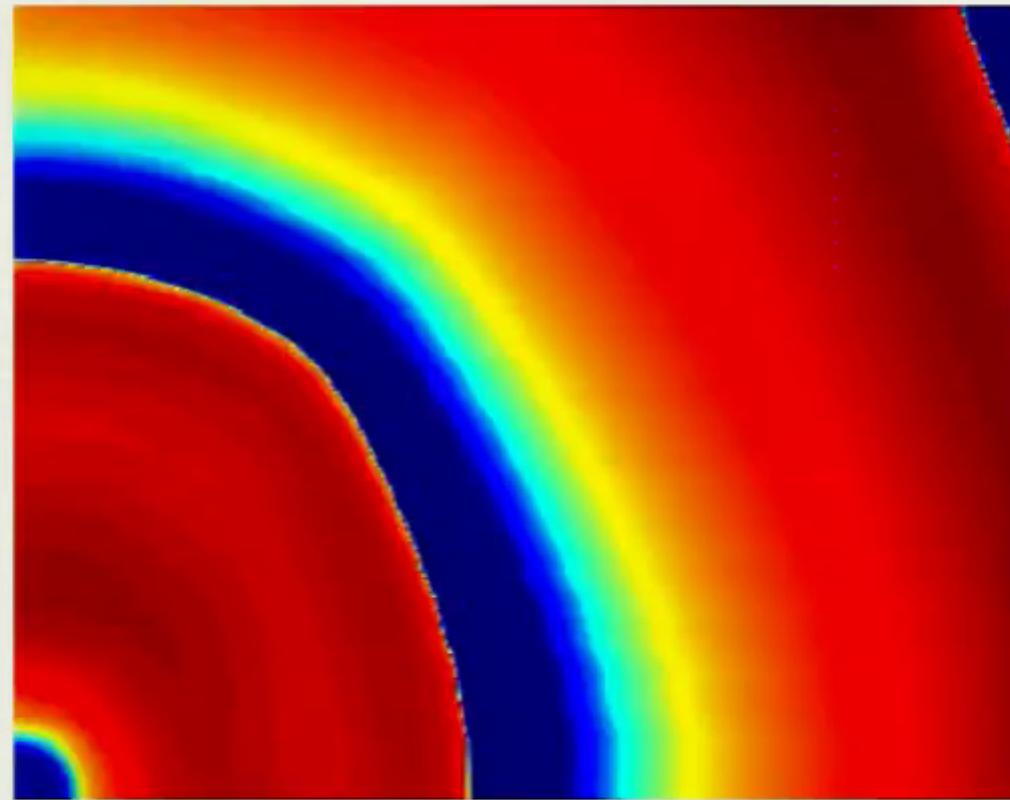
$t = 1058$





# Alternans: Possible Precursor to fibrillation

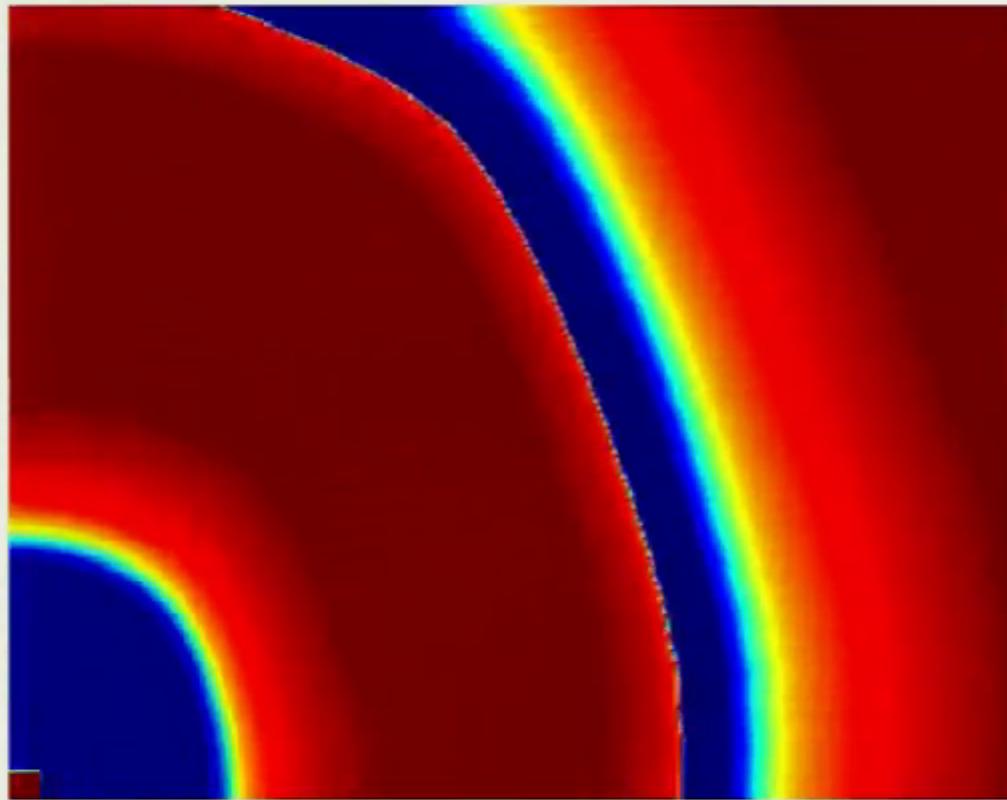
$t = 1274$





# Alternans: Possible Precursor to fibrillation

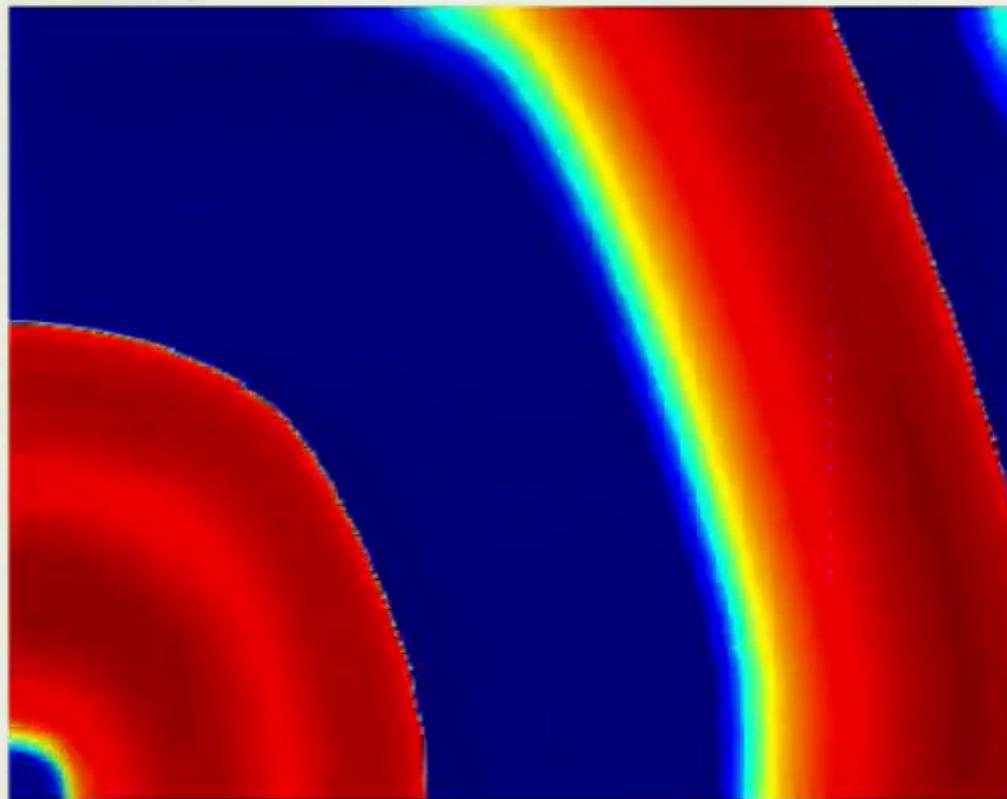
$t = 1622$





# Alternans: Possible Precursor to fibrillation

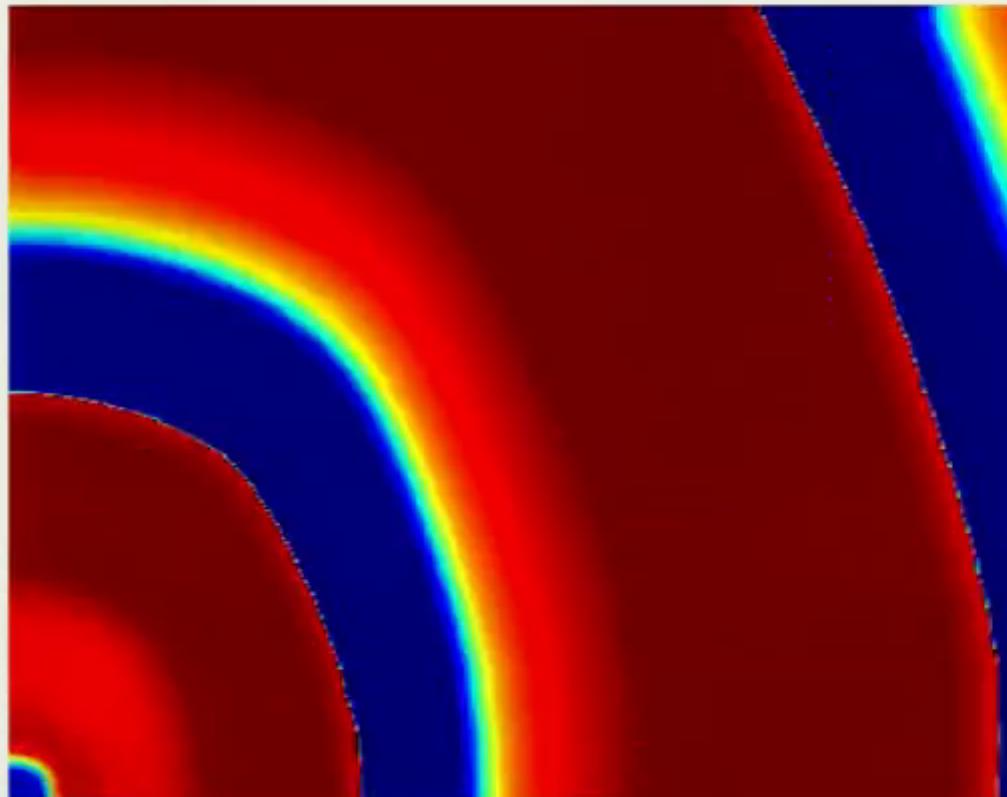
$t = 1806$





# Alternans: Possible Precursor to fibrillation

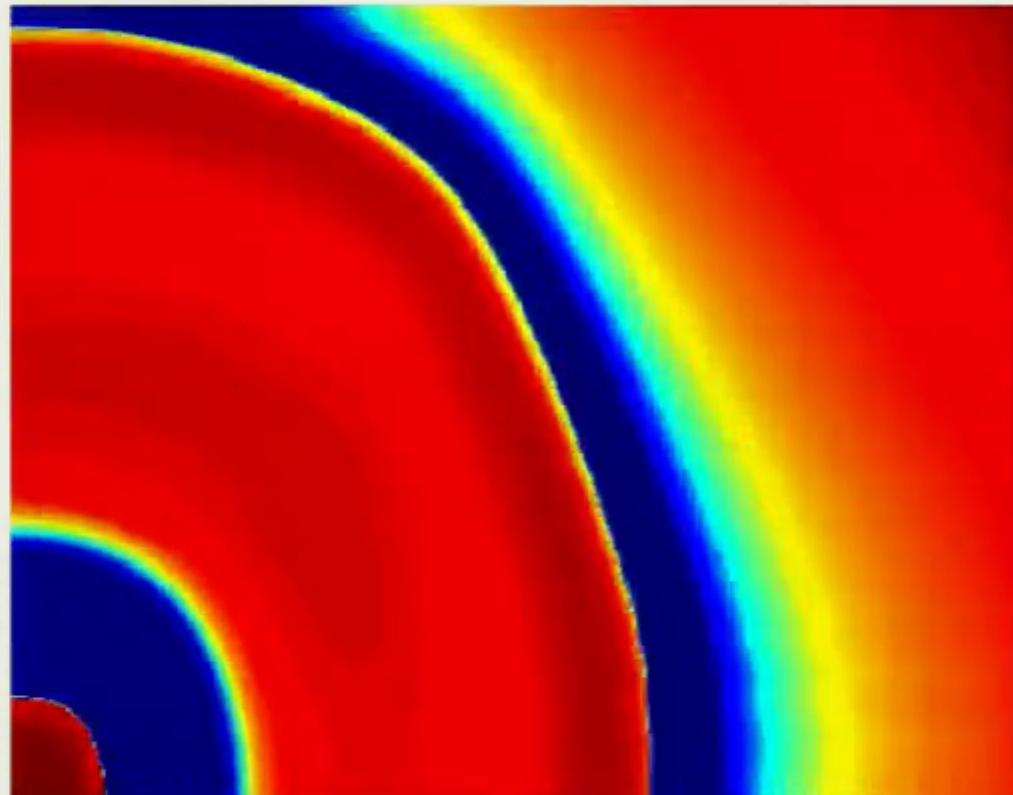
$t = 2026$





# Alternans: Possible Precursor to fibrillation

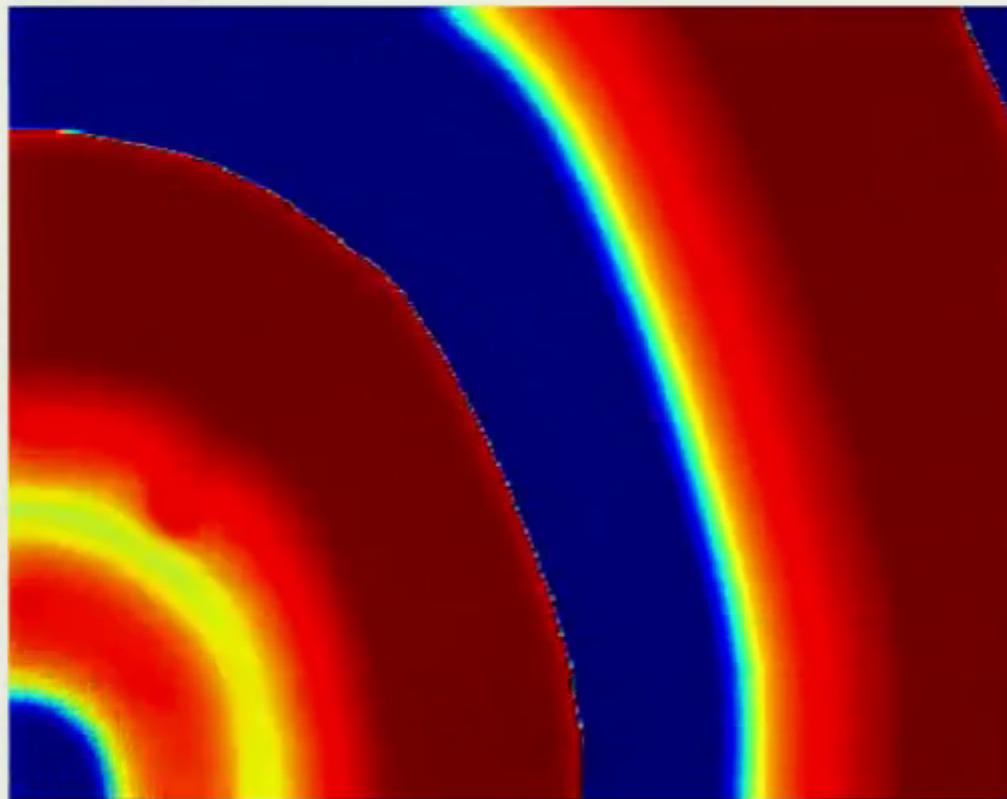
$t = 2186$





# Alternans: Possible Precursor to fibrillation

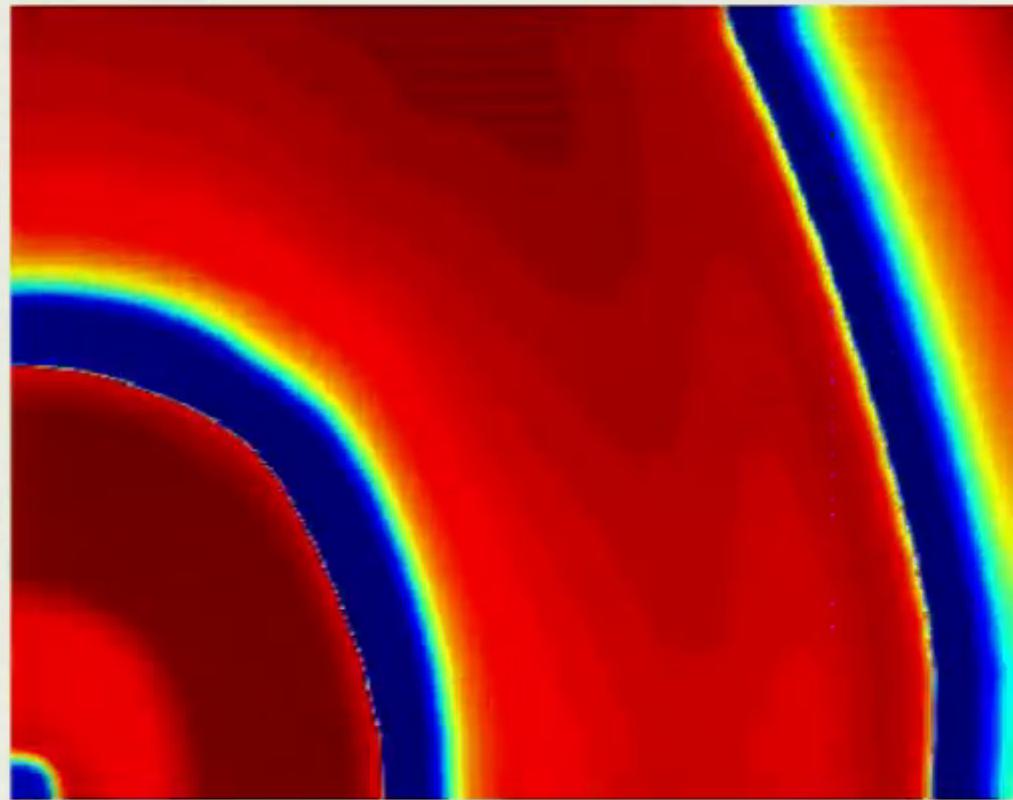
$t = 2402$





# Alternans: Possible Precursor to fibrillation

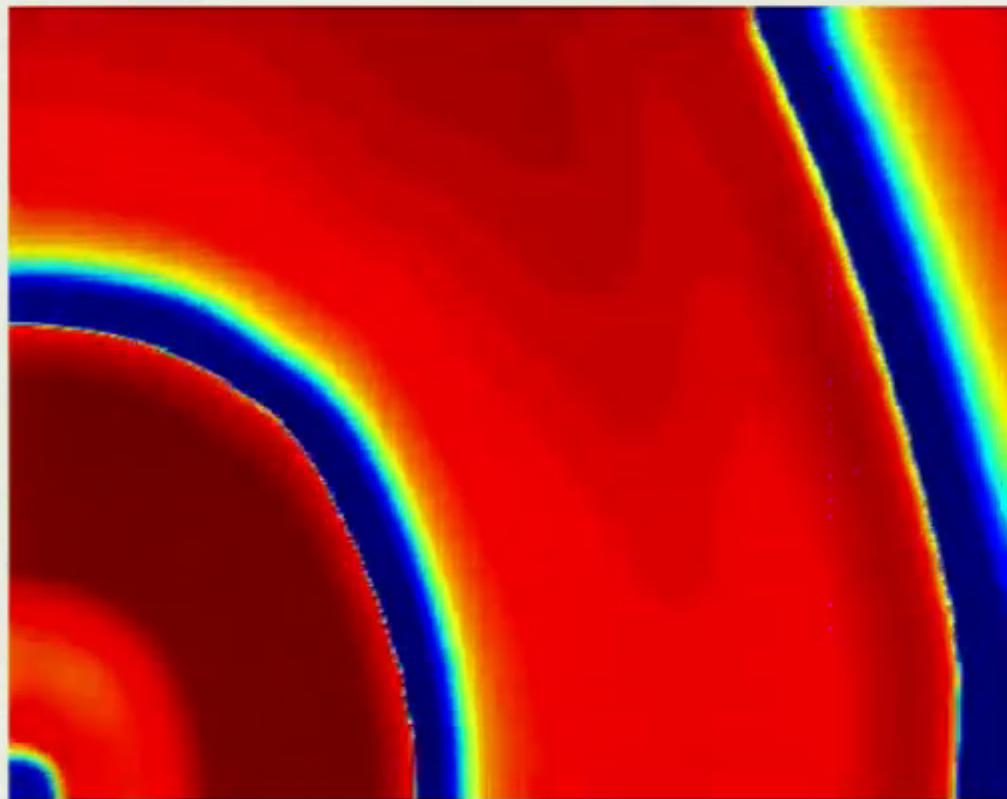
$t = 2574$





# Alternans: Possible Precursor to fibrillation

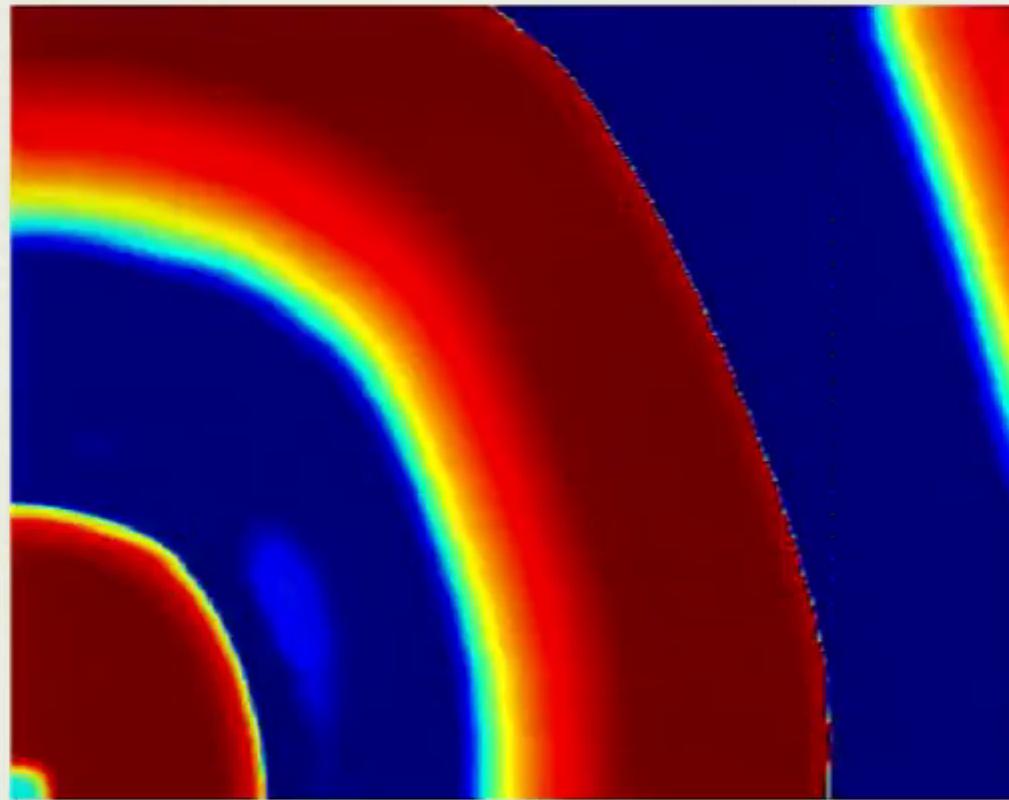
$t = 2590$





# Alternans: Possible Precursor to fibrillation

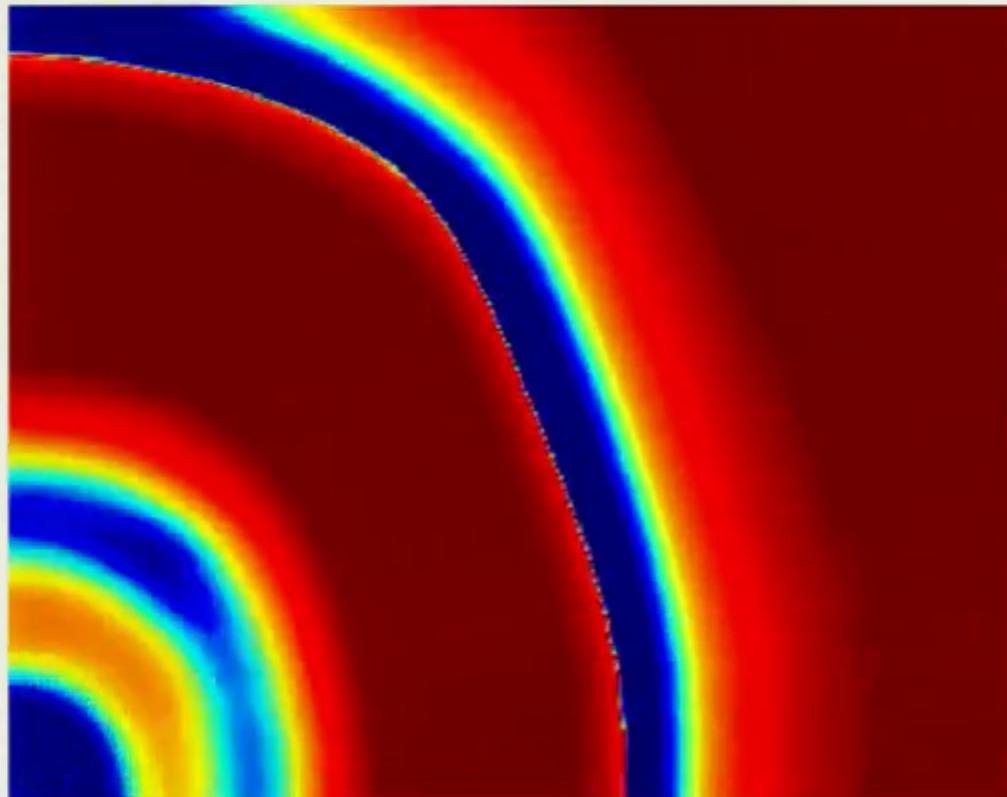
$t = 2798$





# Alternans: Possible Precursor to fibrillation

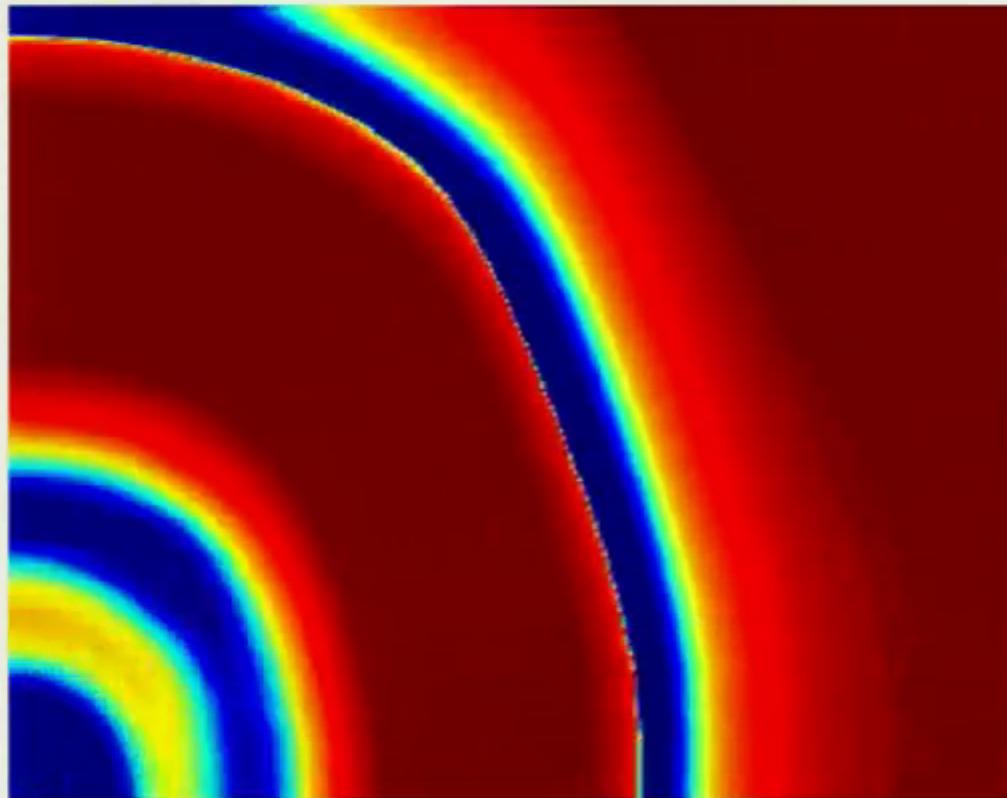
$t = 2958$





# Alternans: Possible Precursor to fibrillation

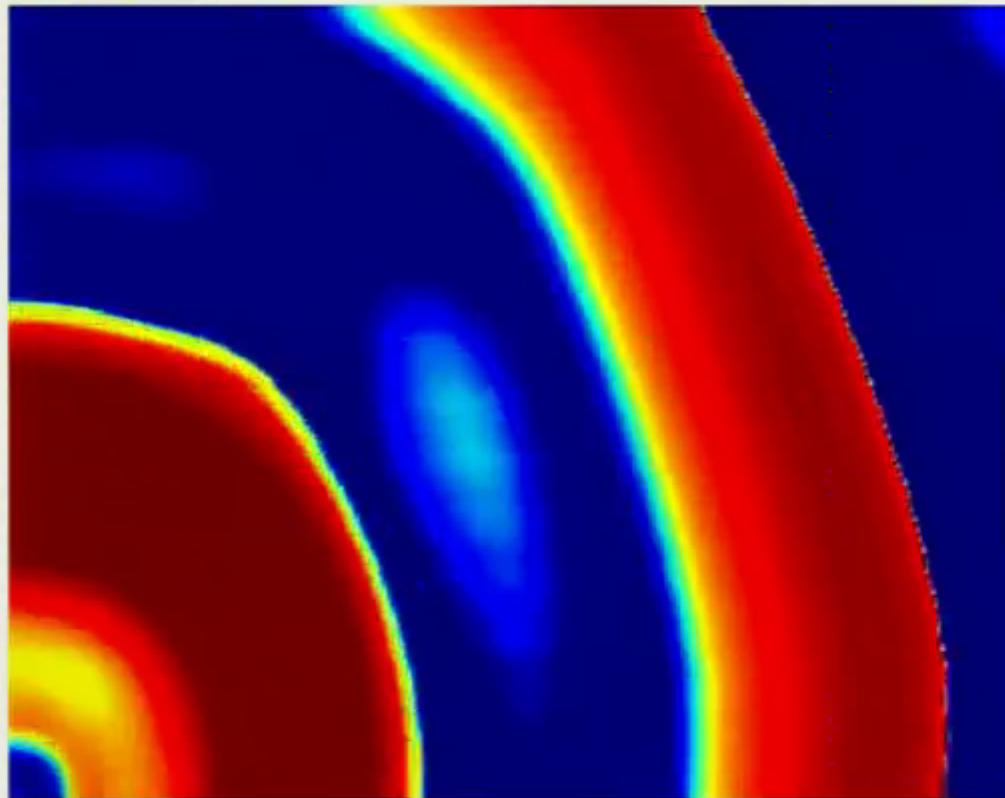
$t = 2966$





# Alternans: Possible Precursor to fibrillation

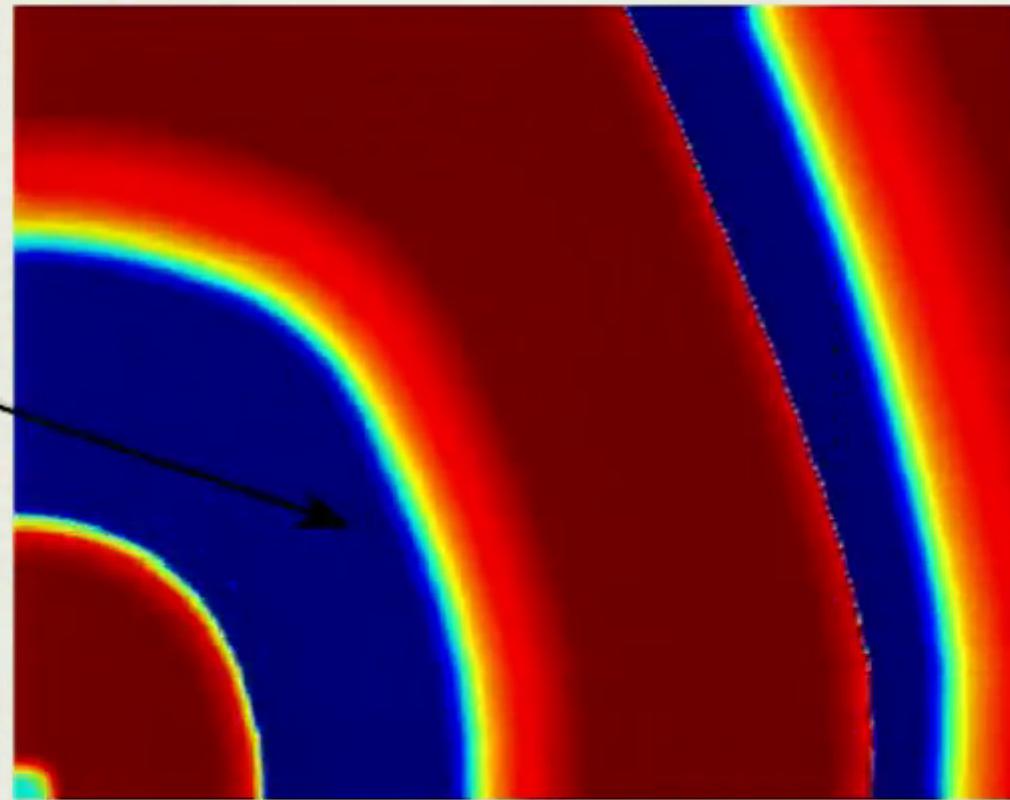
$t = 3154$





# Alternans: Possible Precursor to fibrillation

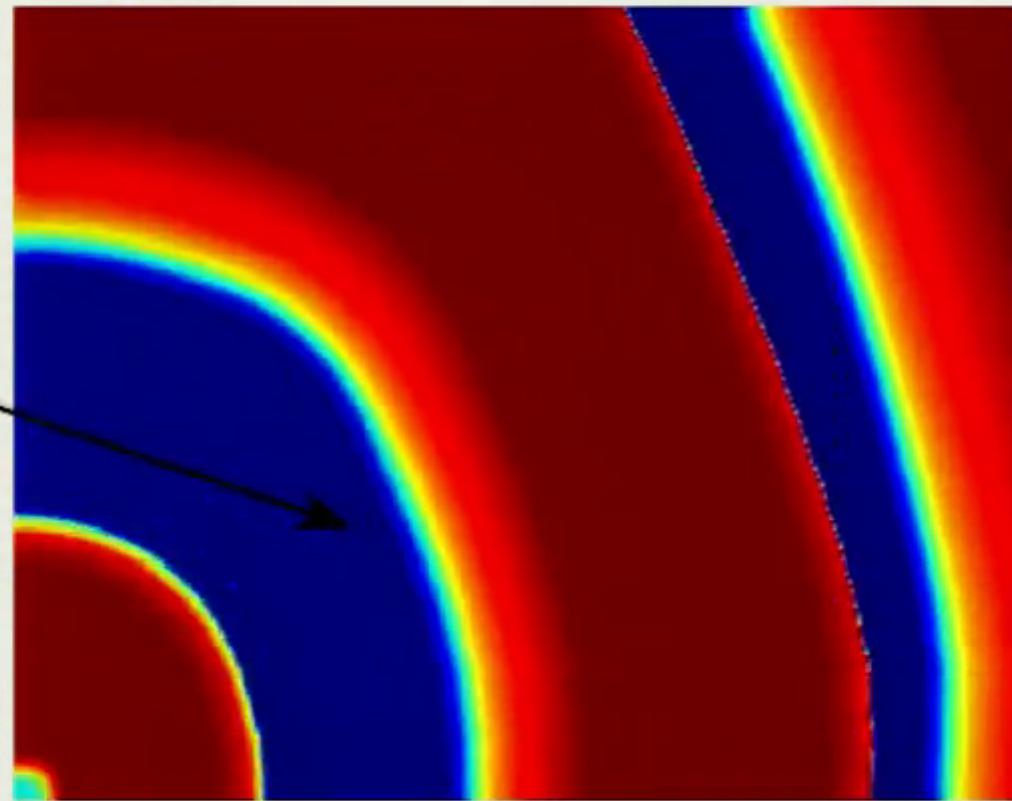
$t = 3338$





# Alternans: Possible Precursor to fibrillation

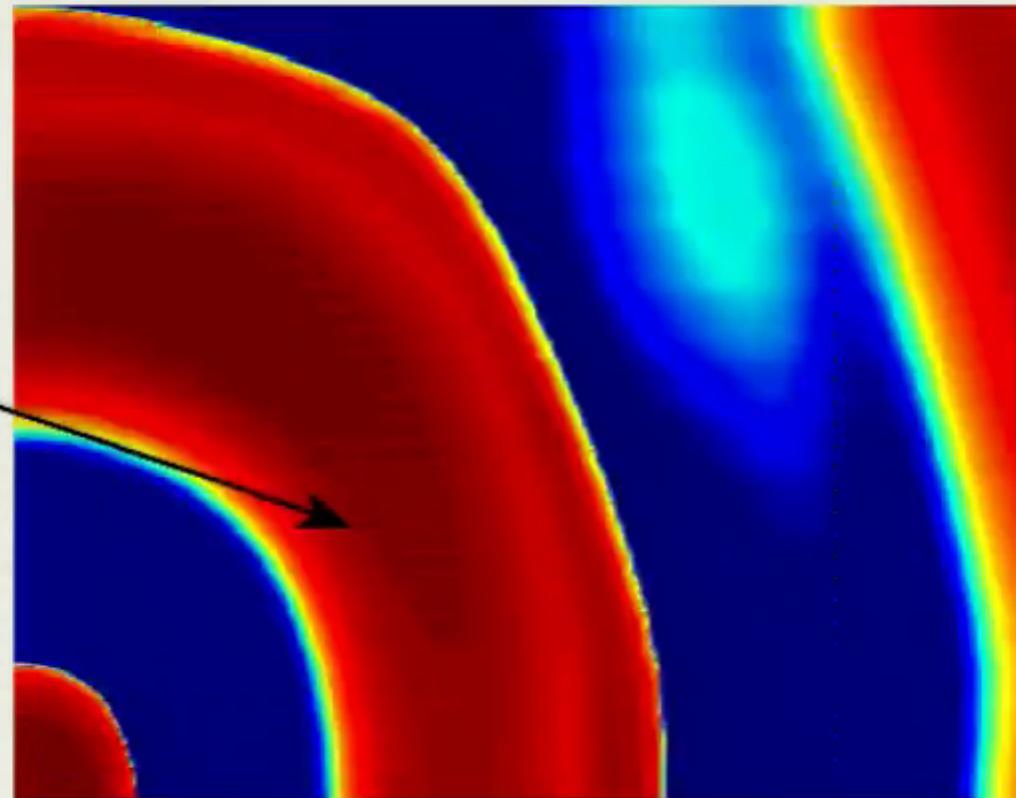
$t = 3338$





# Alternans: Possible Precursor to fibrillation

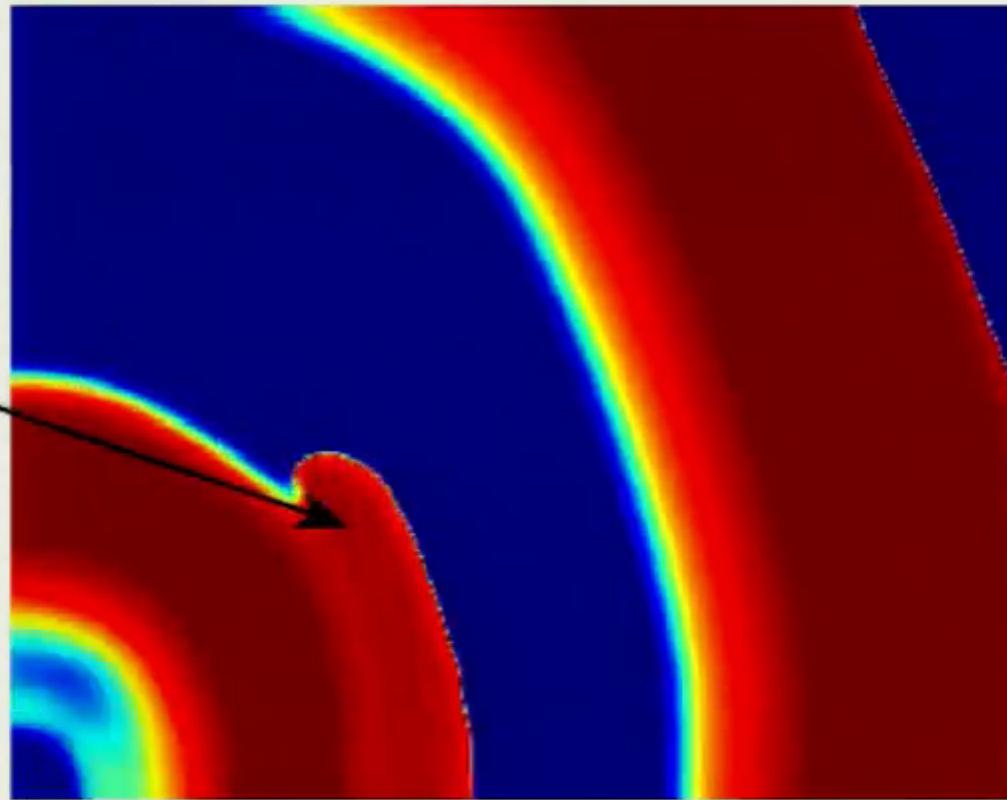
$t = 3550$





# Alternans: Possible Precursor to fibrillation

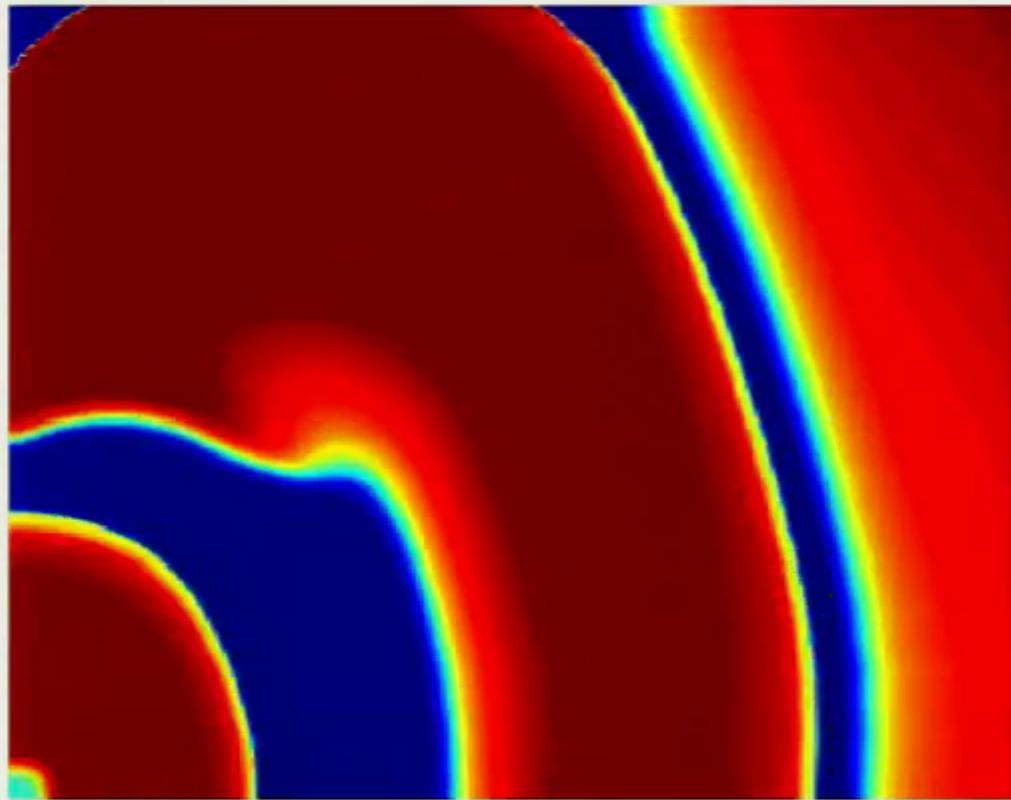
$t = 3718$





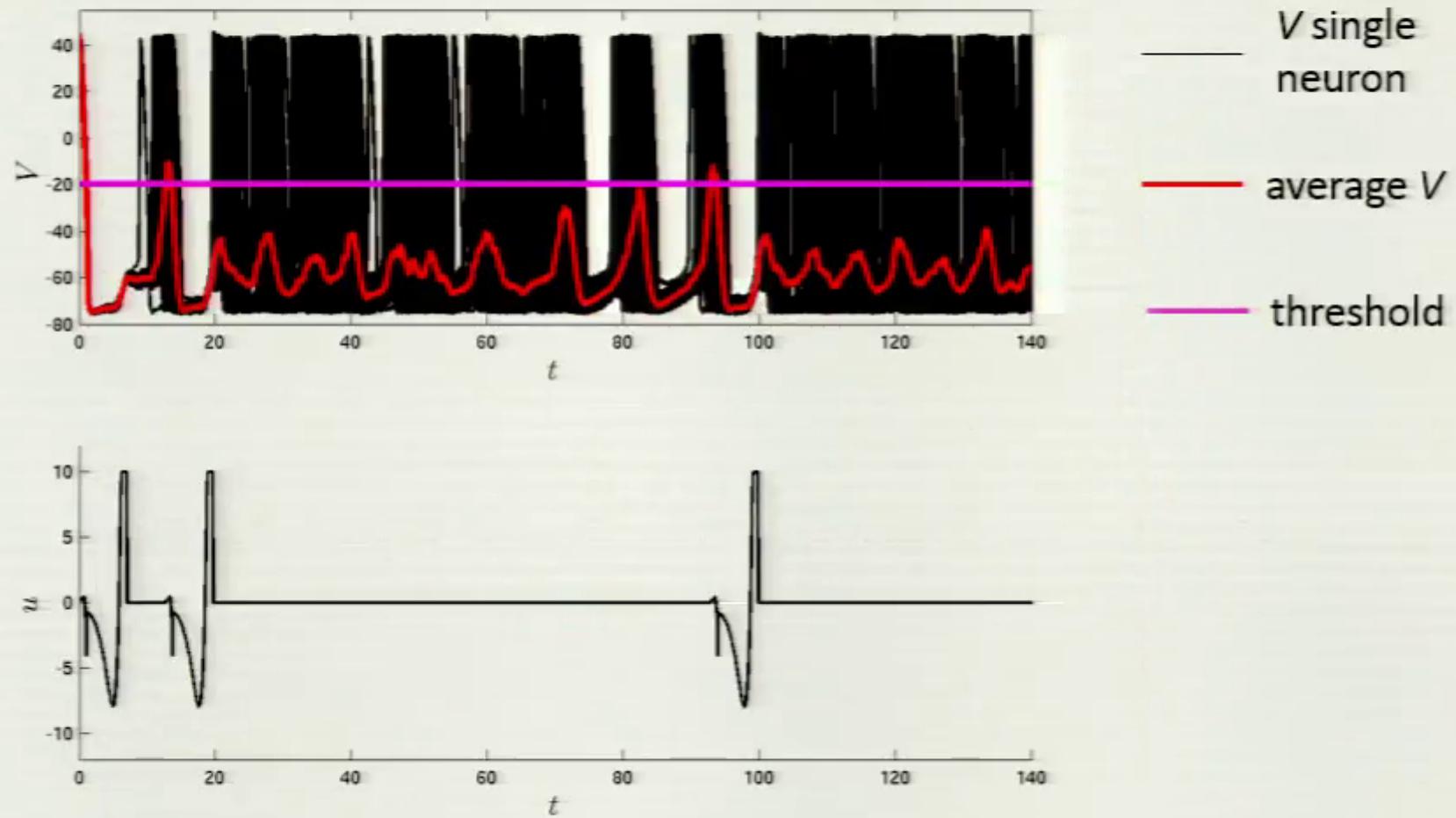
# Alternans: Possible Precursor to fibrillation

$t = 3878$





# Coupled, Noisy Neurons – Phase Resetting



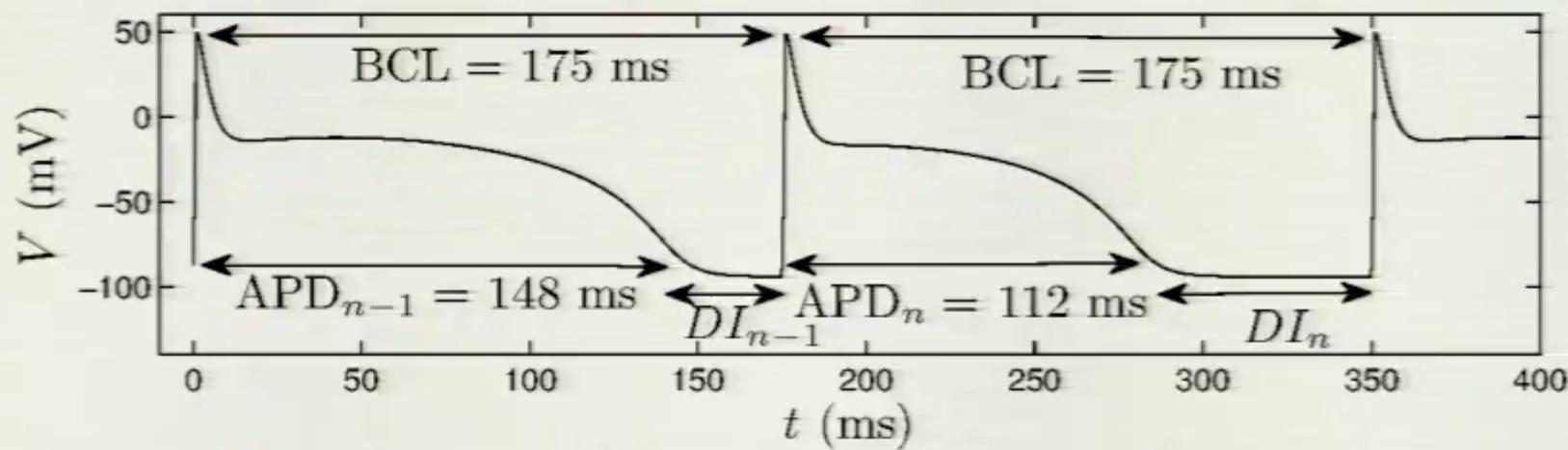


# Cardiac Dynamics

- excitable cells, not oscillators
  - driven by sinoatrial node, which acts as a pacemaker
- cardiac arrhythmias – irregular heartbeat
  - **alternans**: beat-to-beat alternation of cardiac dynamics
  - **fibrillation**: rapid, irregular contraction of heart muscle fibers
    - typically associated with spiral waves



# Alternans



BCL = Basic Cycle Length

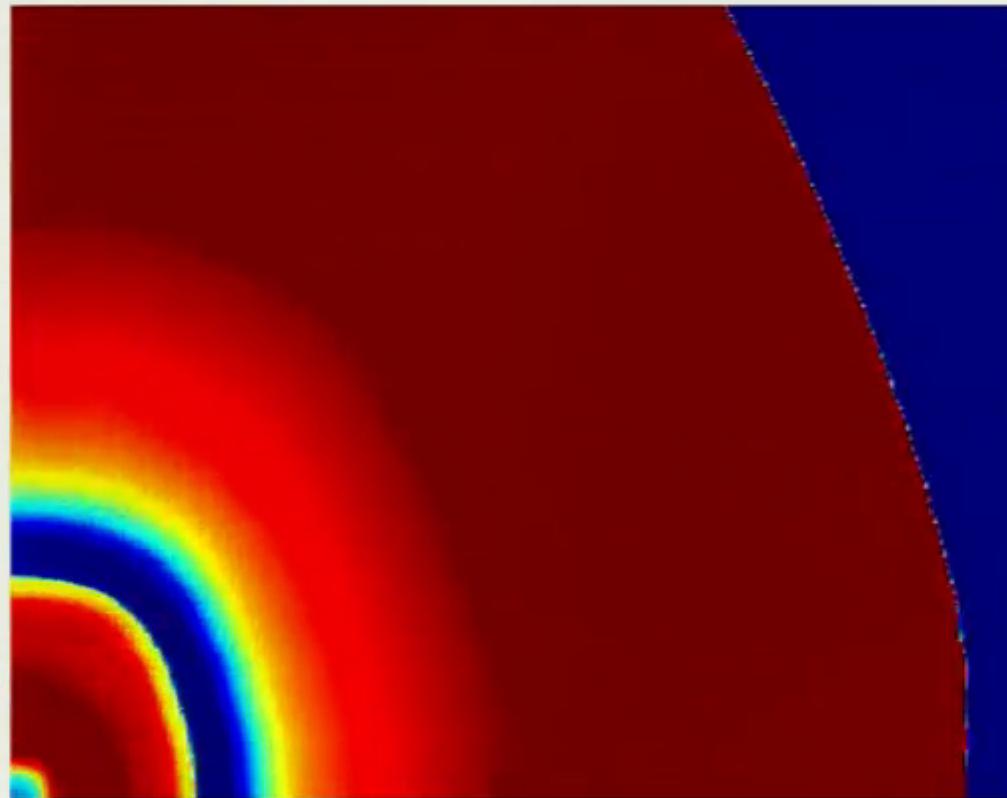
APD = Action Potential Duration

DI = Diastolic Interval



# Alternans: Possible Precursor to fibrillation

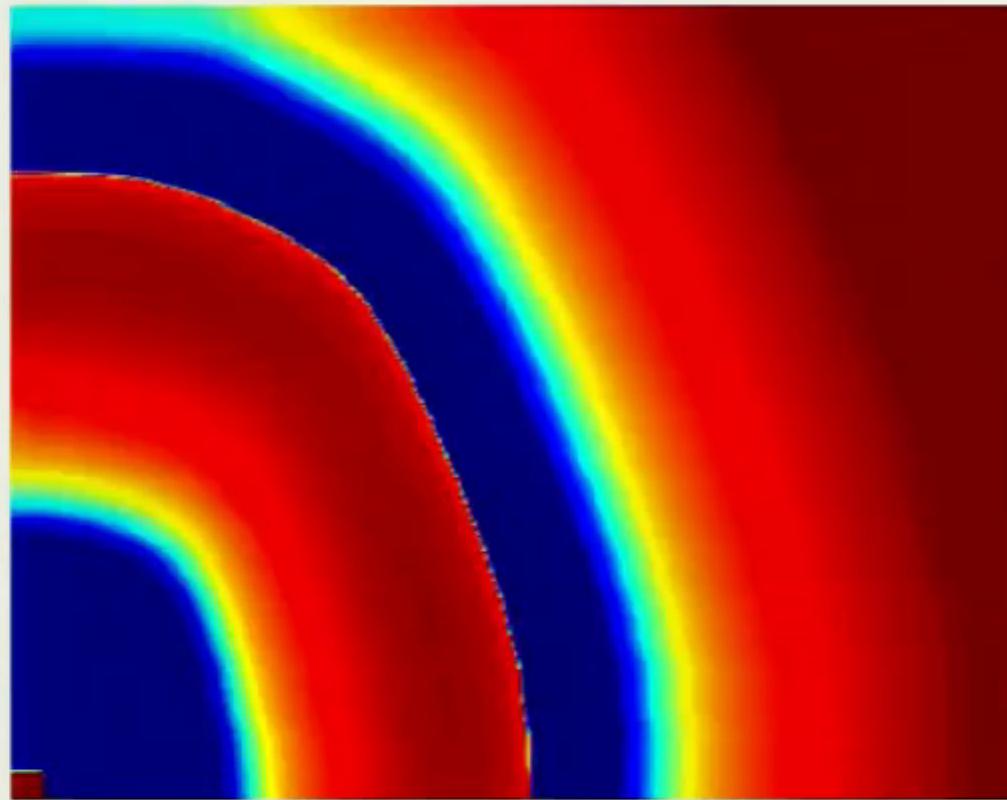
$t = 362$





# Alternans: Possible Precursor to fibrillation

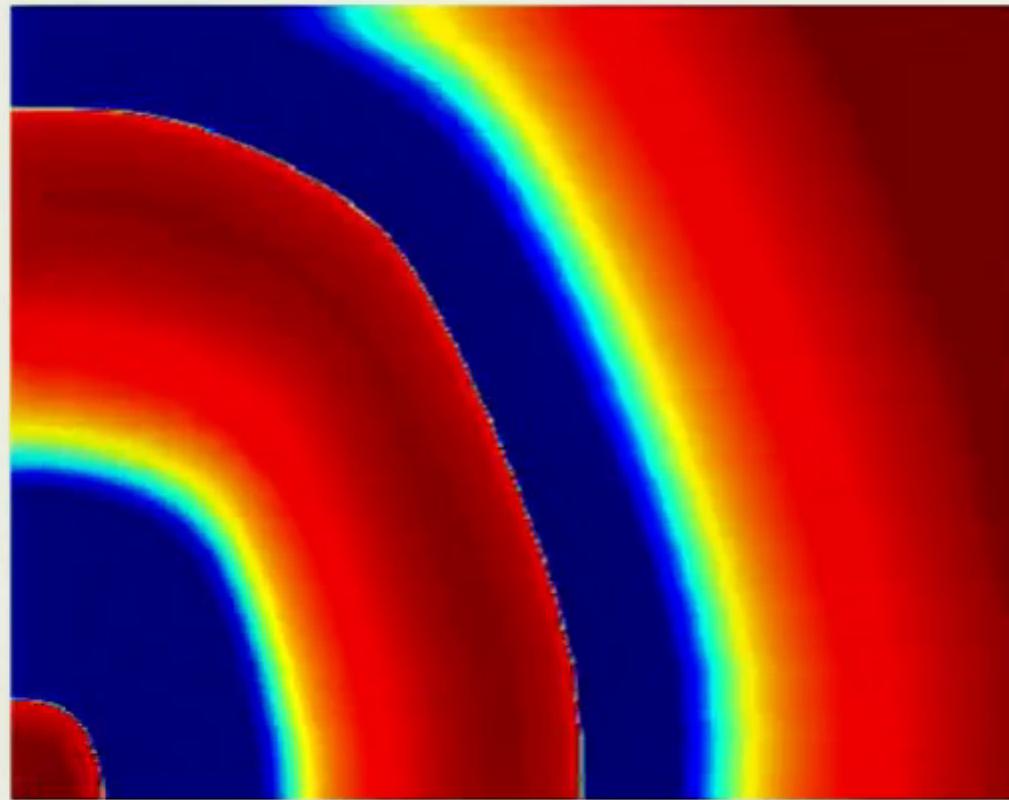
$t = 542$





# Alternans: Possible Precursor to fibrillation

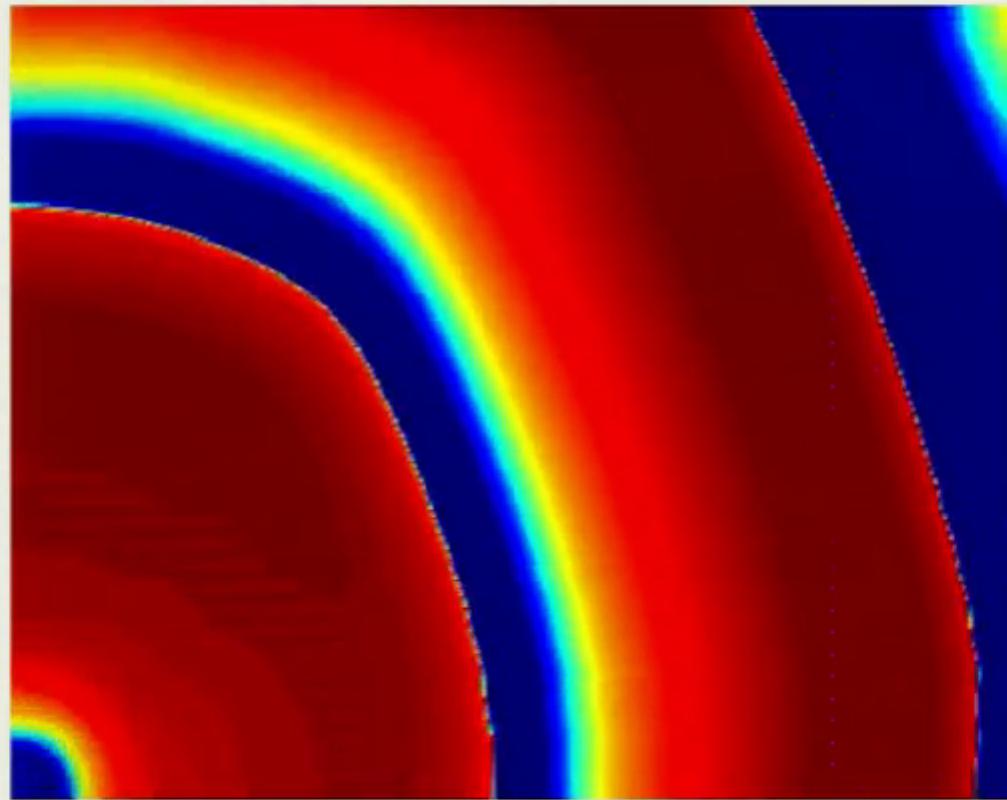
$t = 566$





# Alternans: Possible Precursor to fibrillation

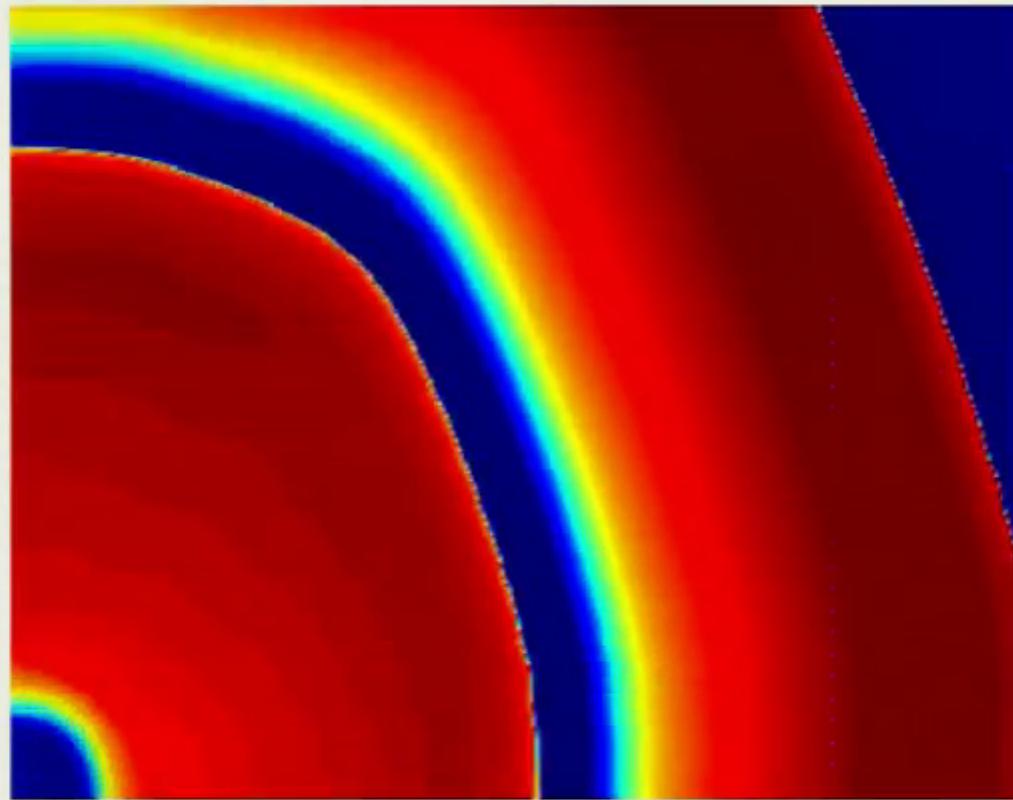
$t = 734$





# Alternans: Possible Precursor to fibrillation

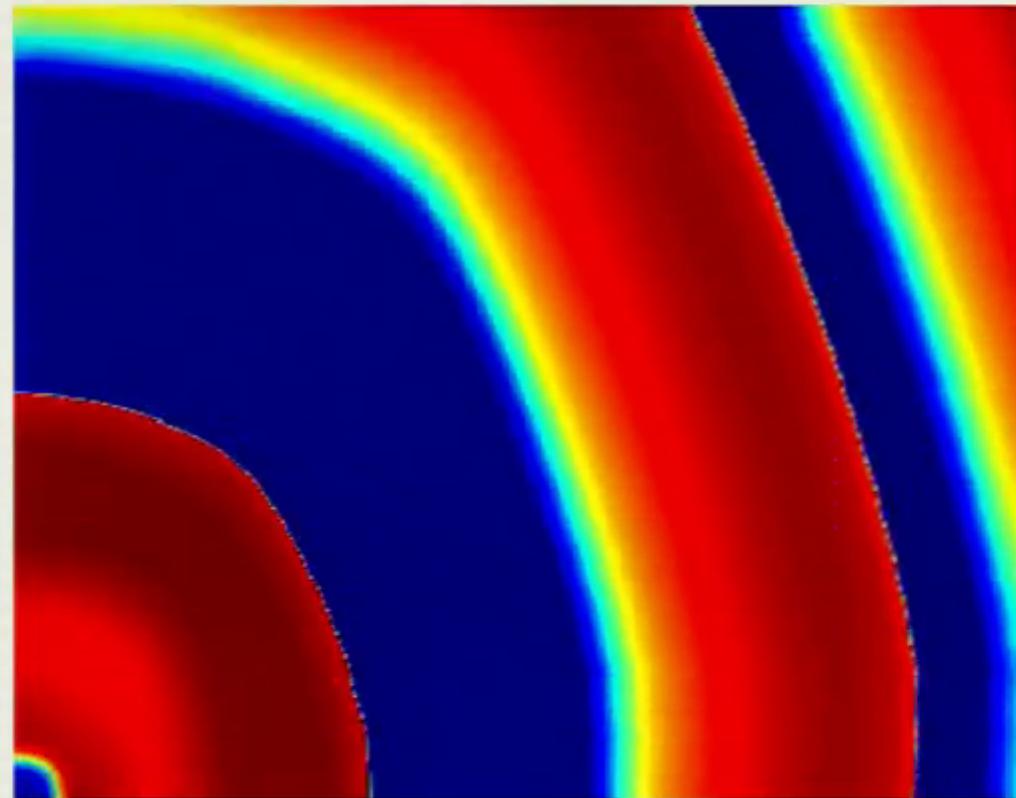
$t = 758$





# Alternans: Possible Precursor to fibrillation

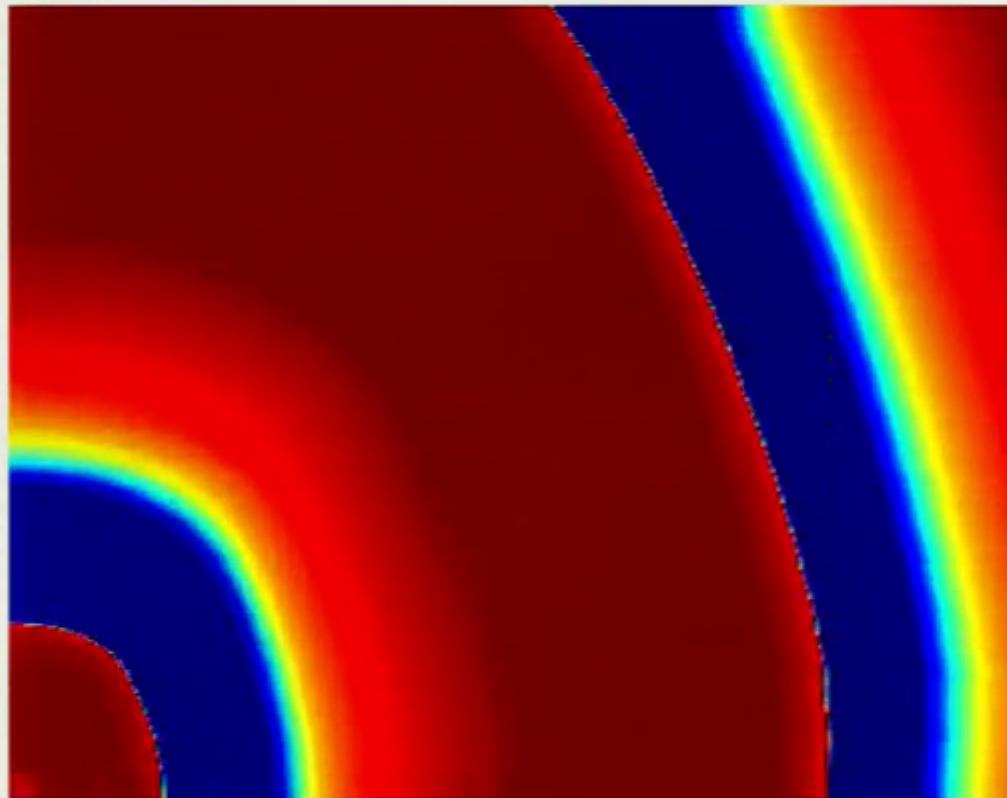
$t = 950$





# Alternans: Possible Precursor to fibrillation

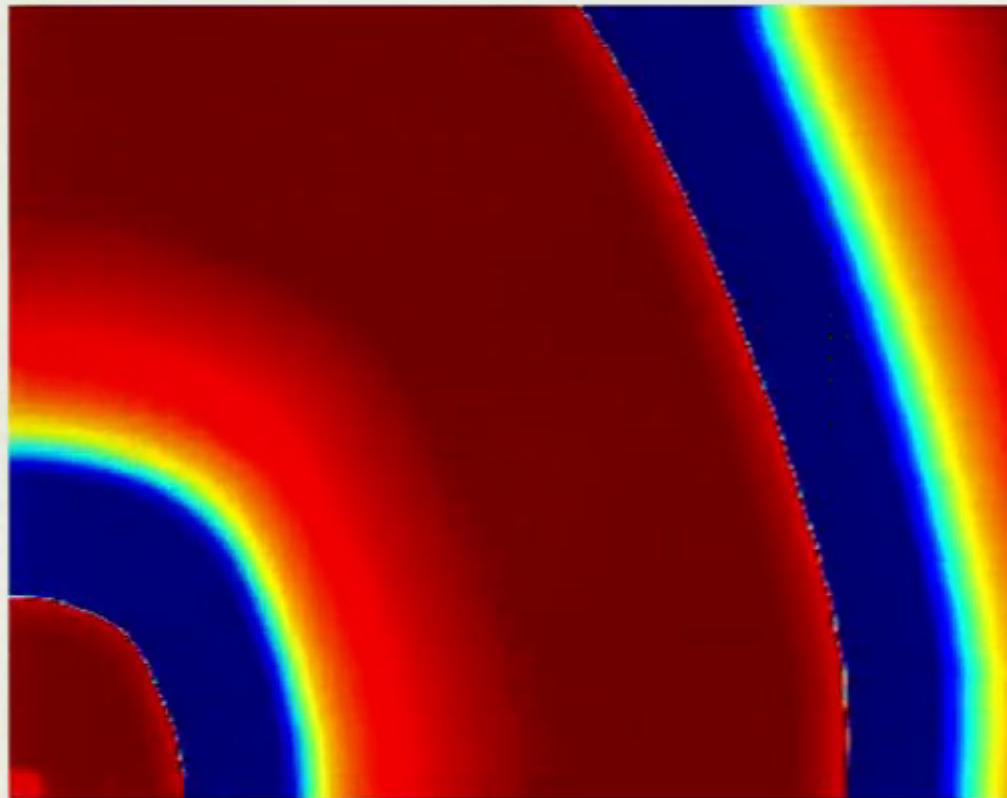
$t = 1130$





# Alternans: Possible Precursor to fibrillation

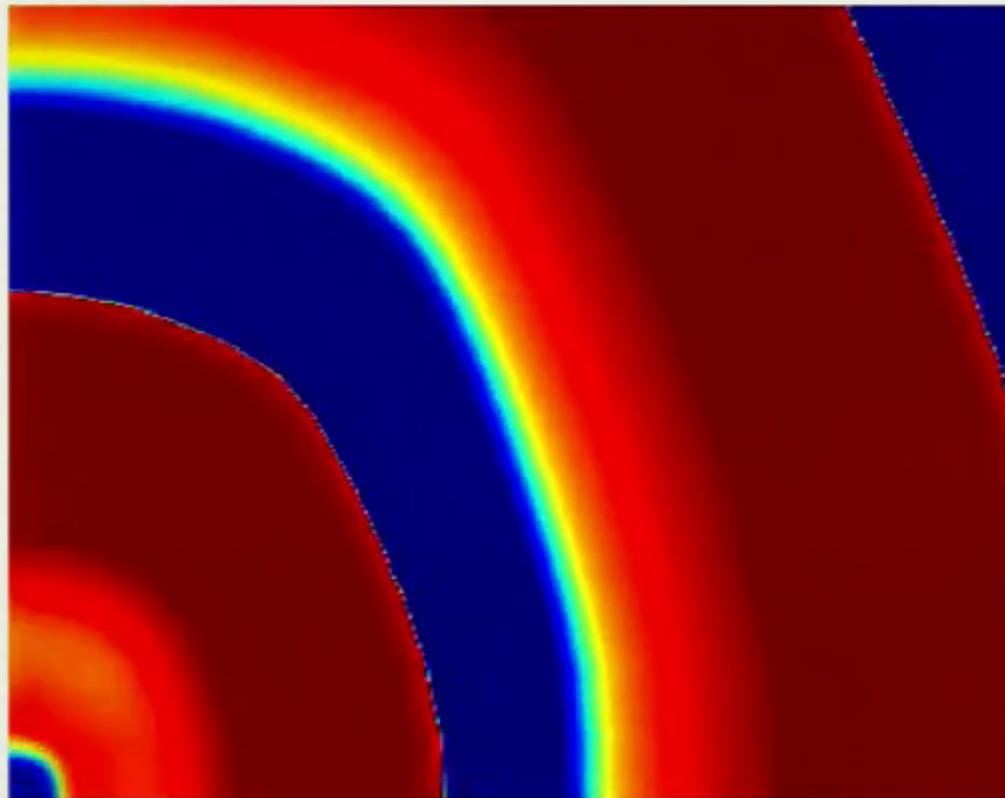
$t = 1138$





# Alternans: Possible Precursor to fibrillation

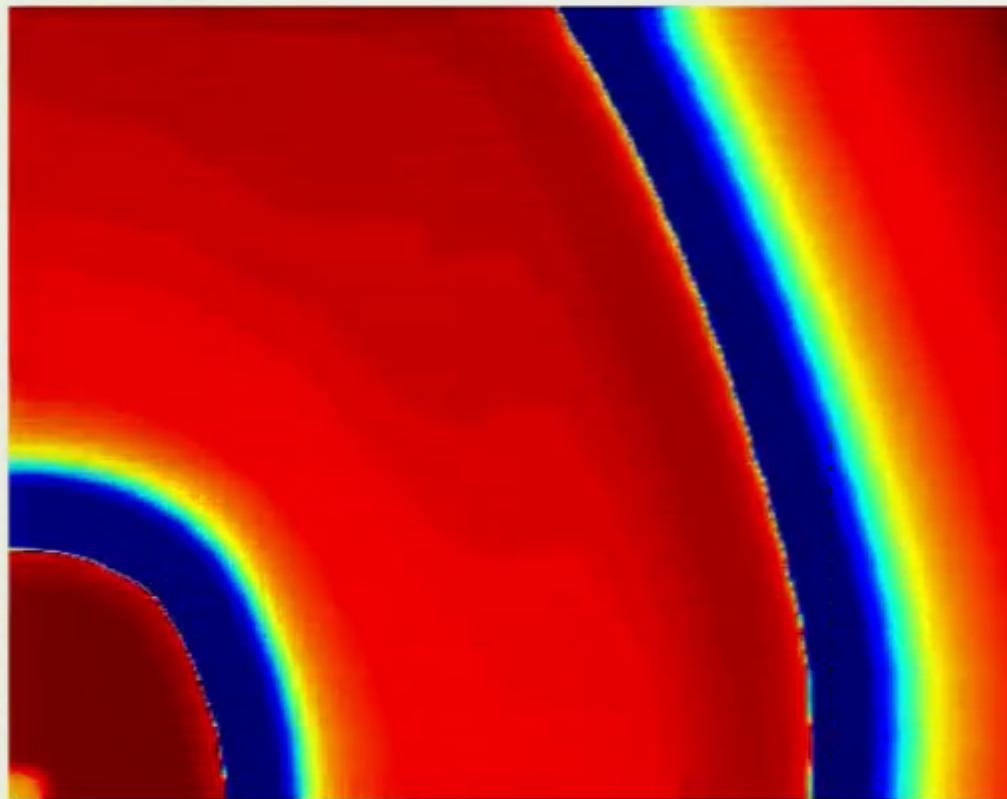
$t = 1518$





# Alternans: Possible Precursor to fibrillation

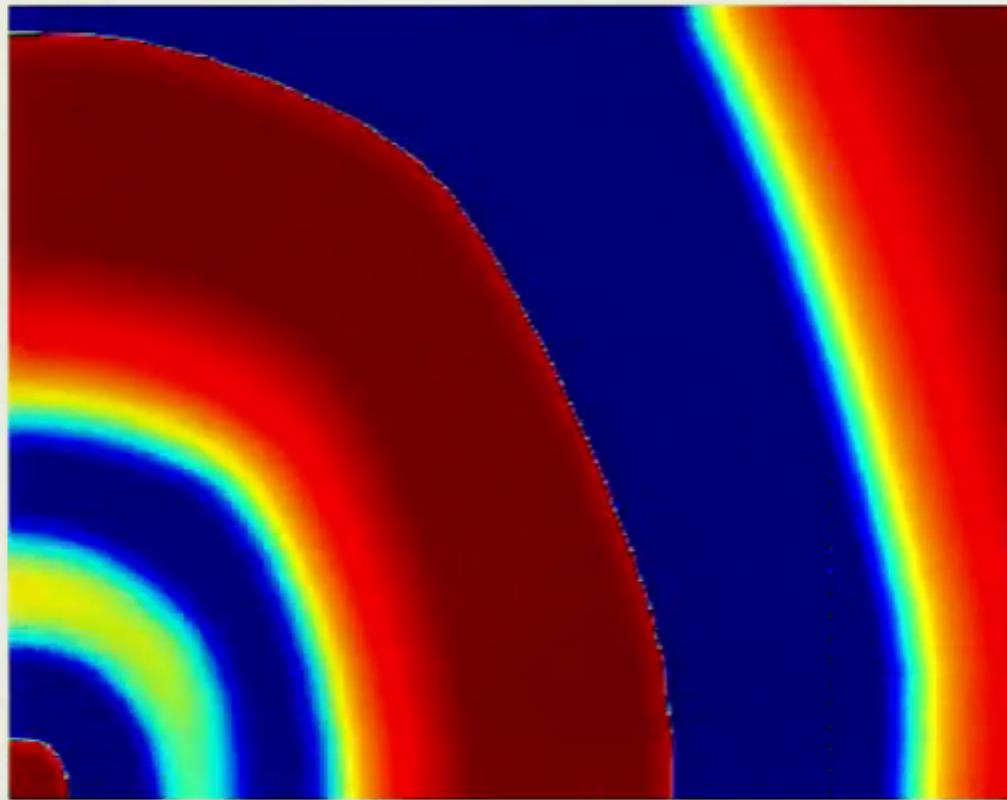
$t = 1694$





# Alternans: Possible Precursor to fibrillation

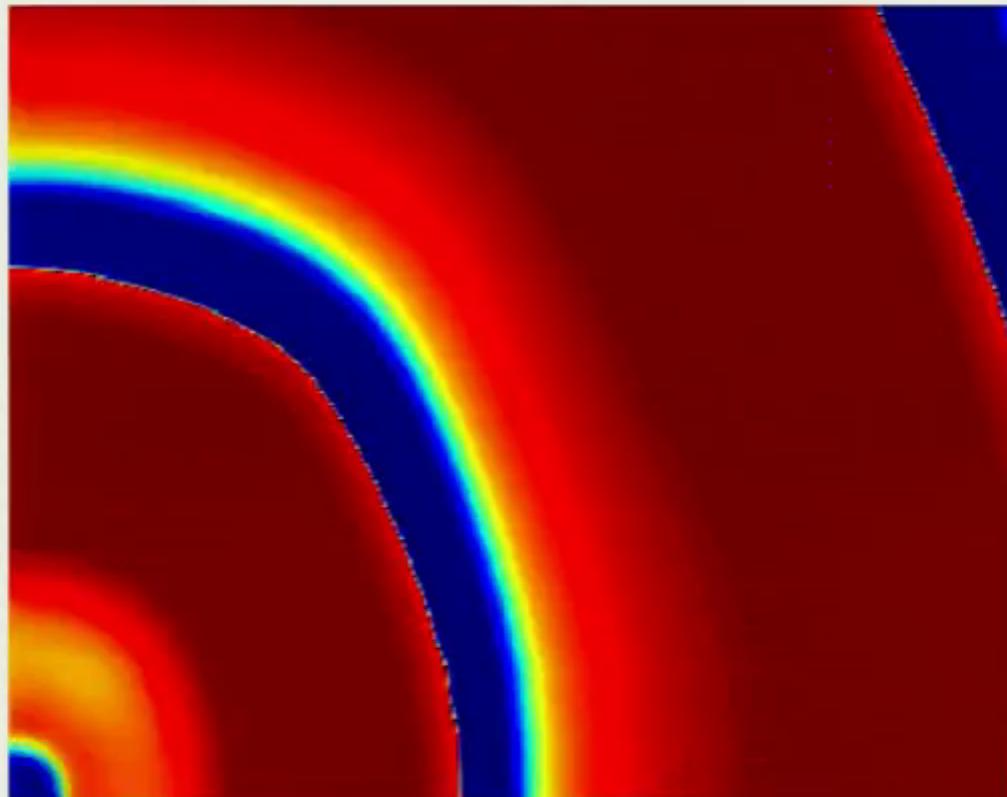
$t = 1902$





# Alternans: Possible Precursor to fibrillation

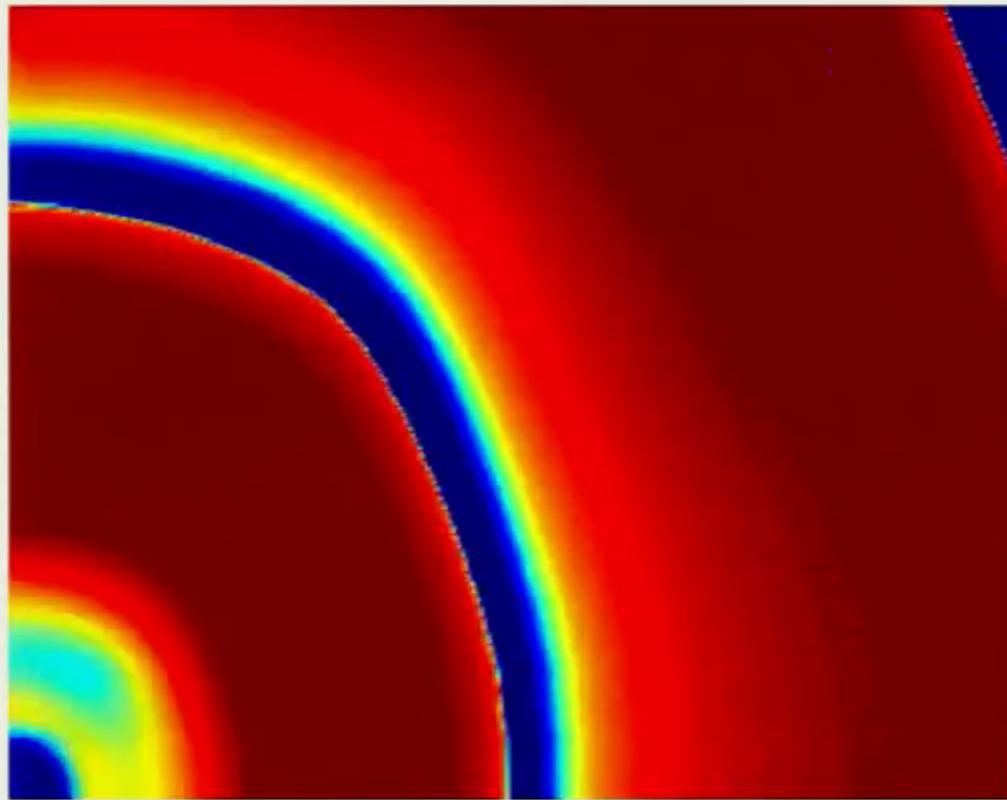
$t = 2066$





# Alternans: Possible Precursor to fibrillation

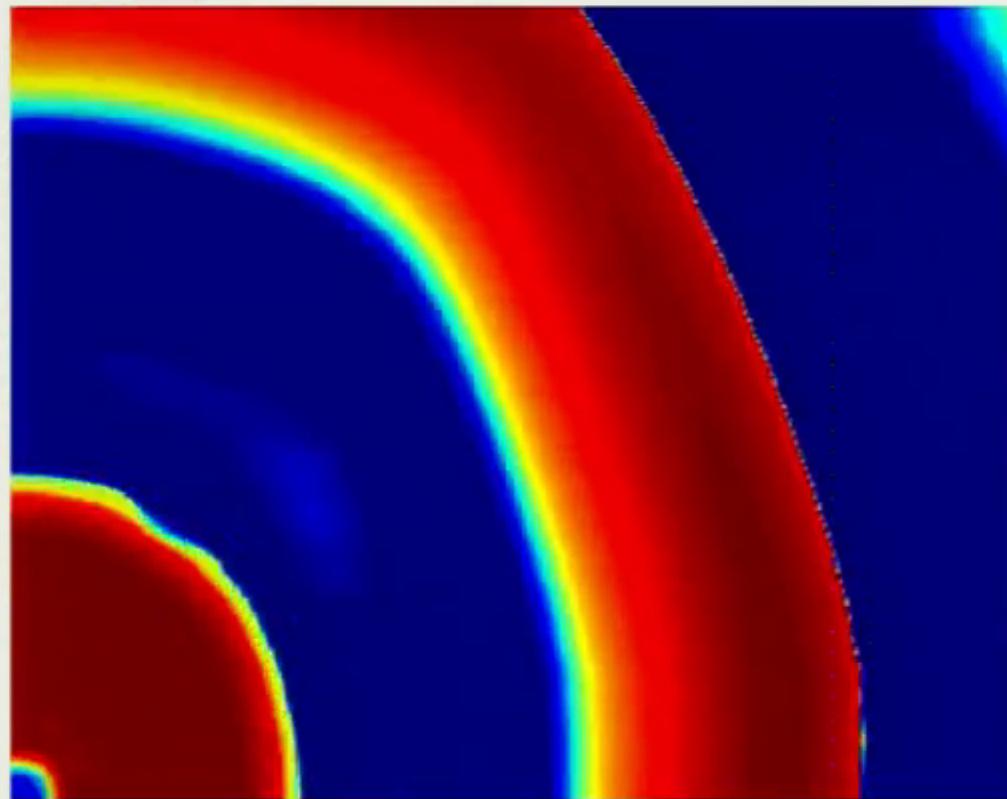
$t = 2090$





# Alternans: Possible Precursor to fibrillation

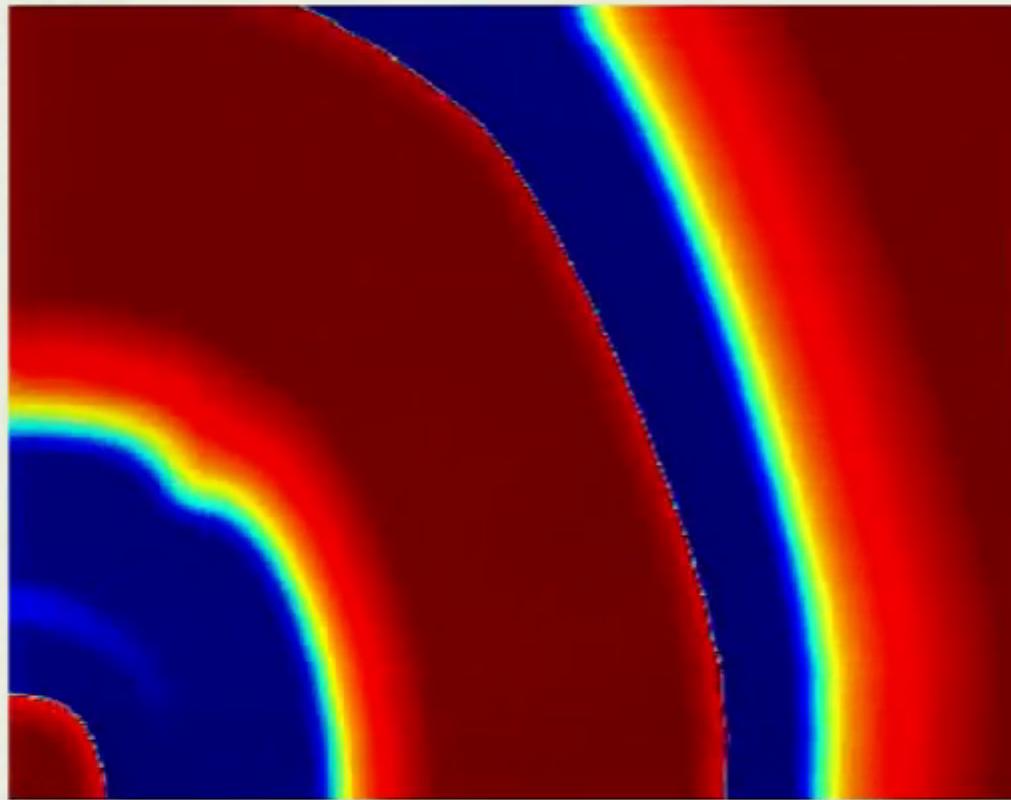
$t = 2282$





# Alternans: Possible Precursor to fibrillation

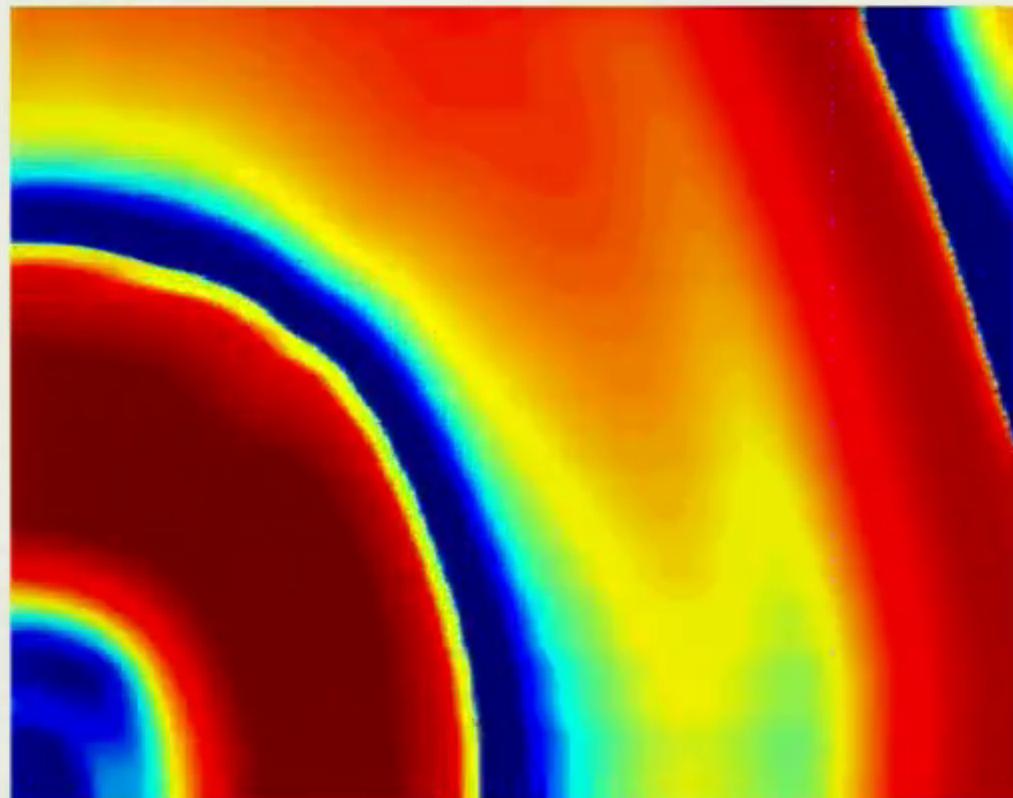
$t = 2458$





# Alternans: Possible Precursor to fibrillation

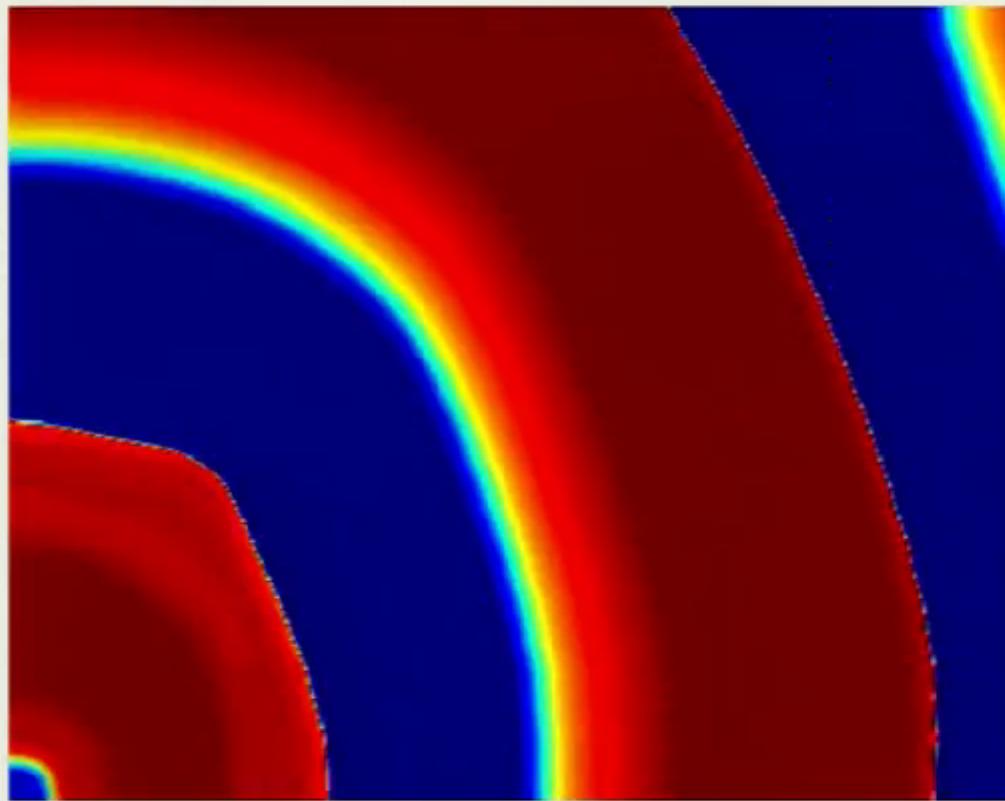
$t = 2646$





# Alternans: Possible Precursor to fibrillation

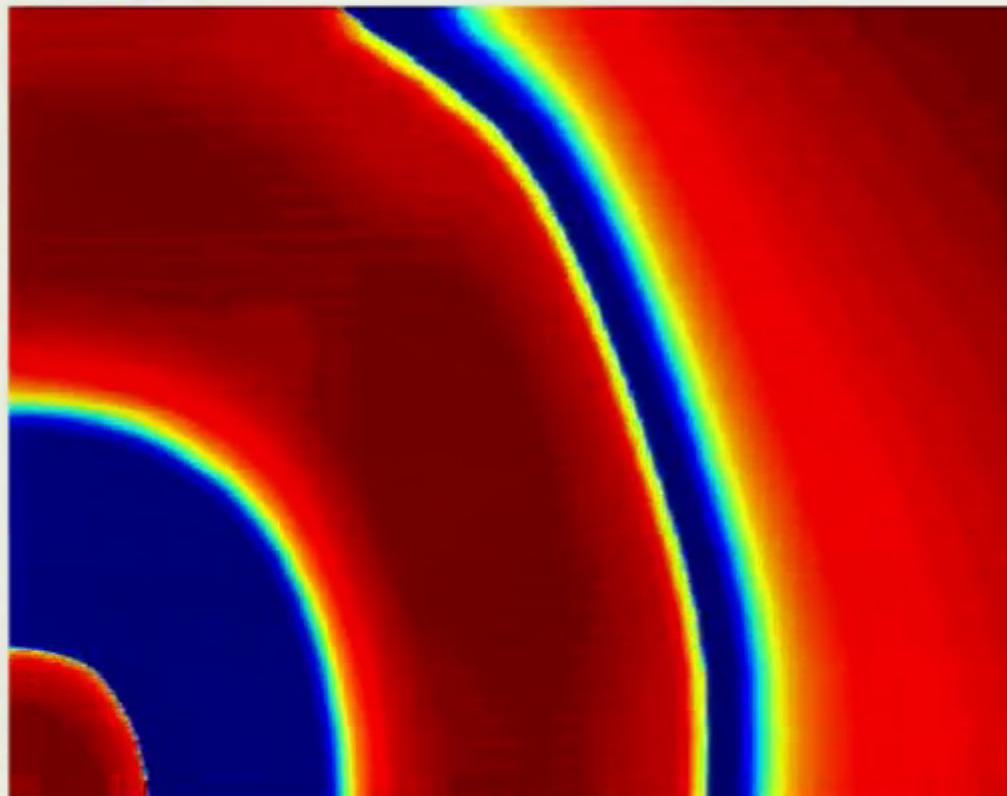
$t = 2838$





# Alternans: Possible Precursor to fibrillation

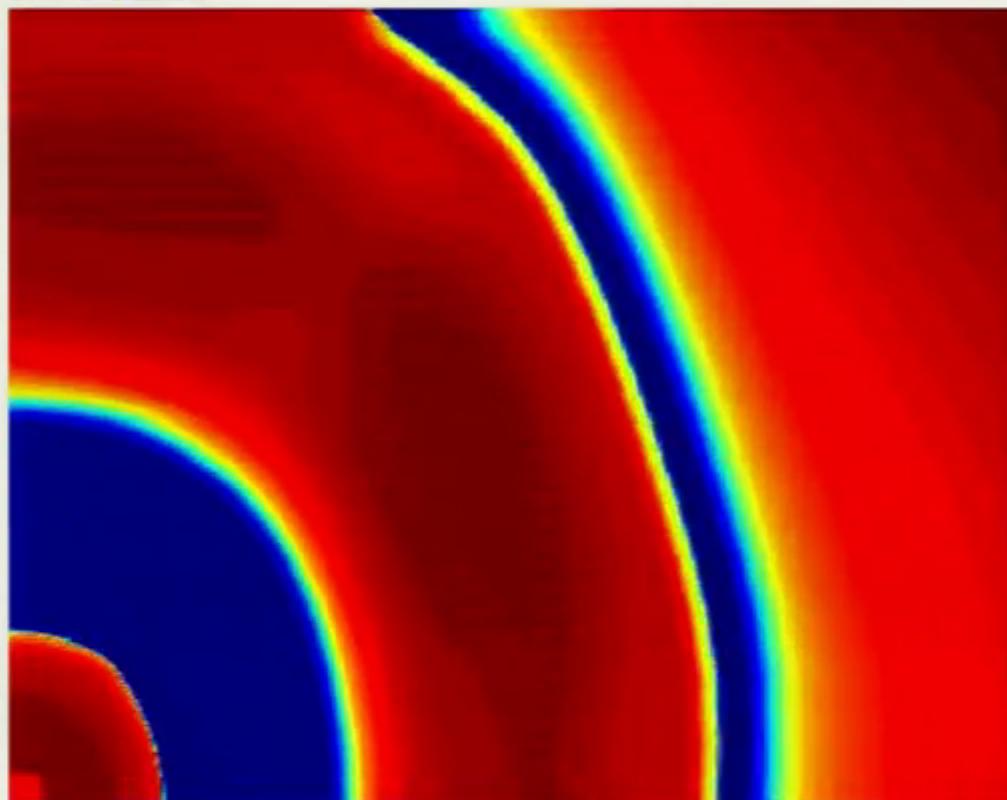
$t = 3018$





# Alternans: Possible Precursor to fibrillation

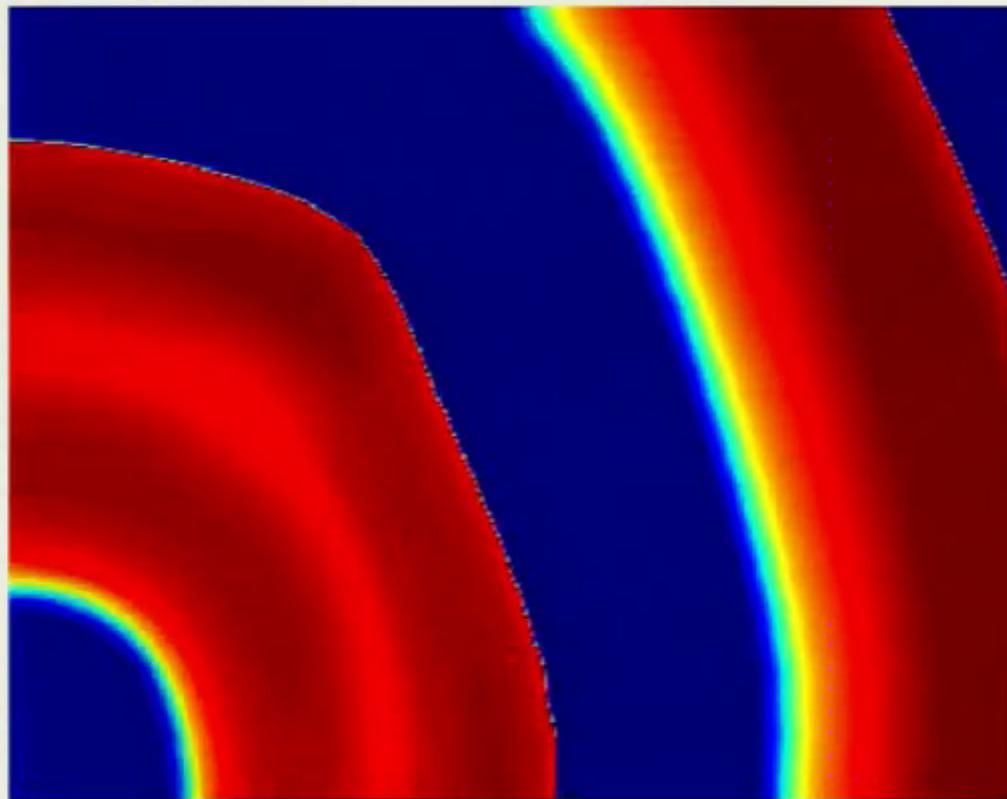
$t = 3026$





# Alternans: Possible Precursor to fibrillation

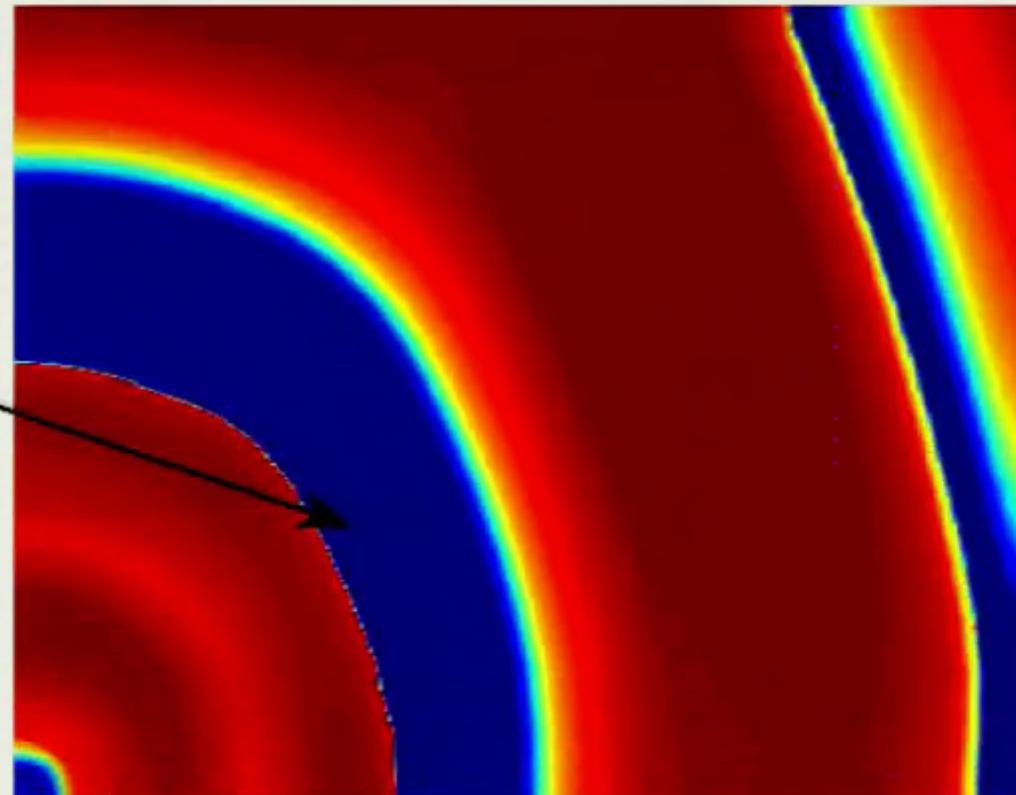
$t = 3218$





# Alternans: Possible Precursor to fibrillation

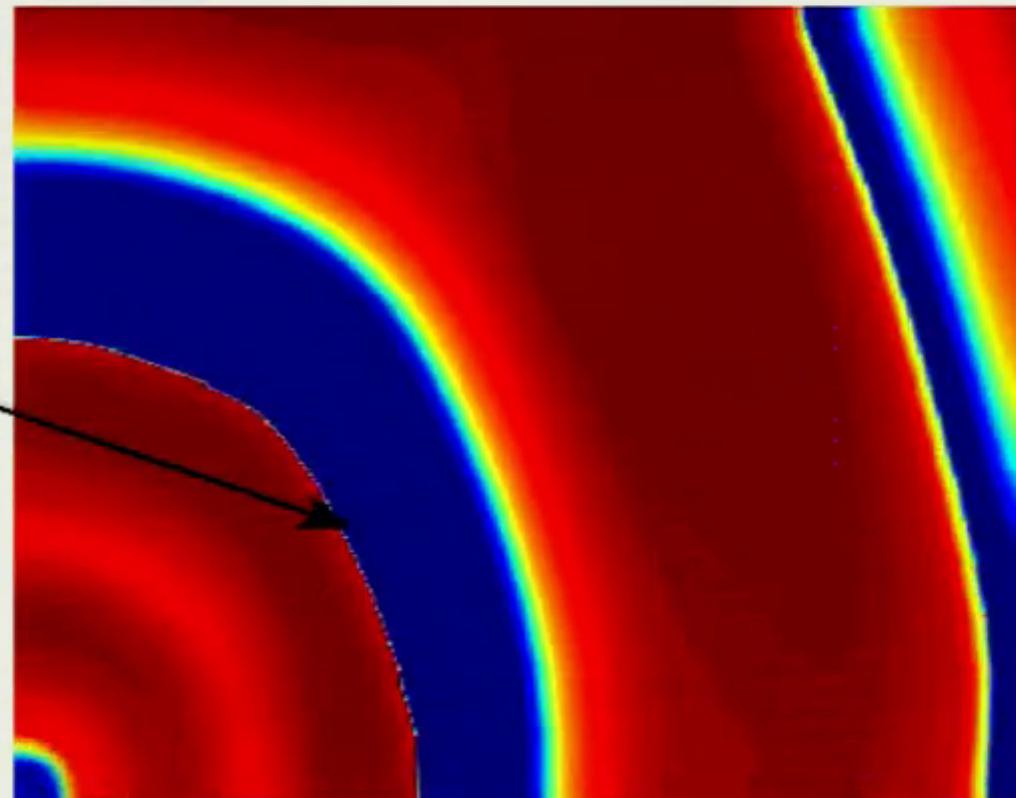
$t = 3402$





# Alternans: Possible Precursor to fibrillation

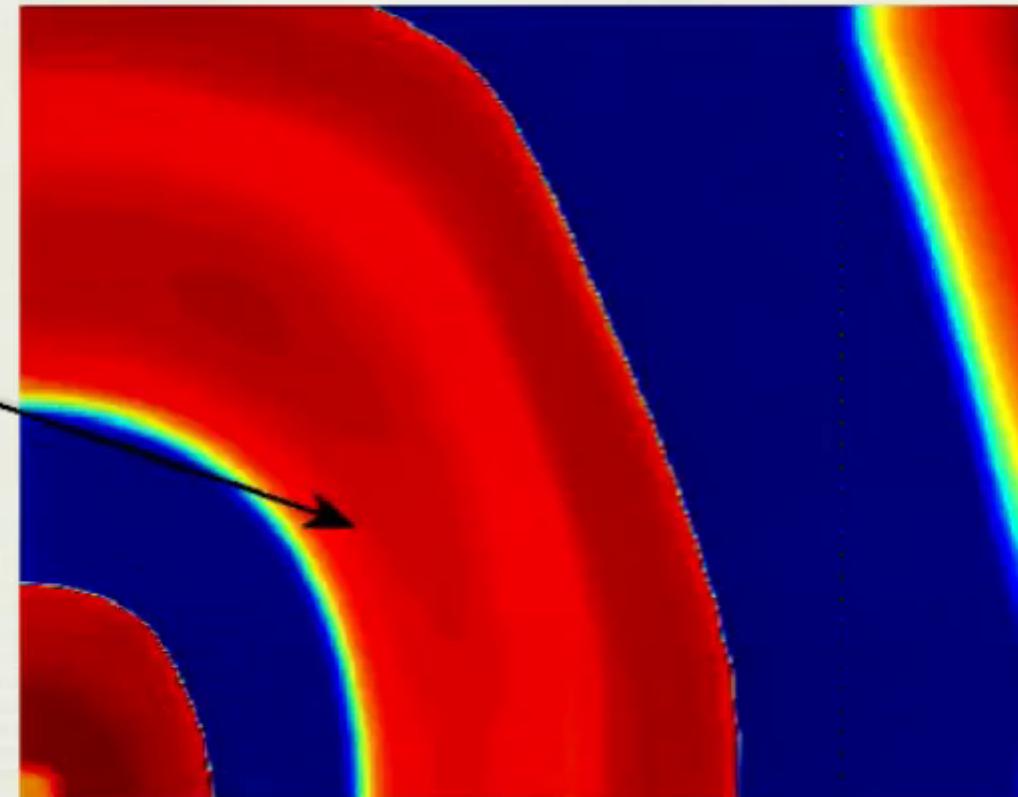
$t = 3410$





# Alternans: Possible Precursor to fibrillation

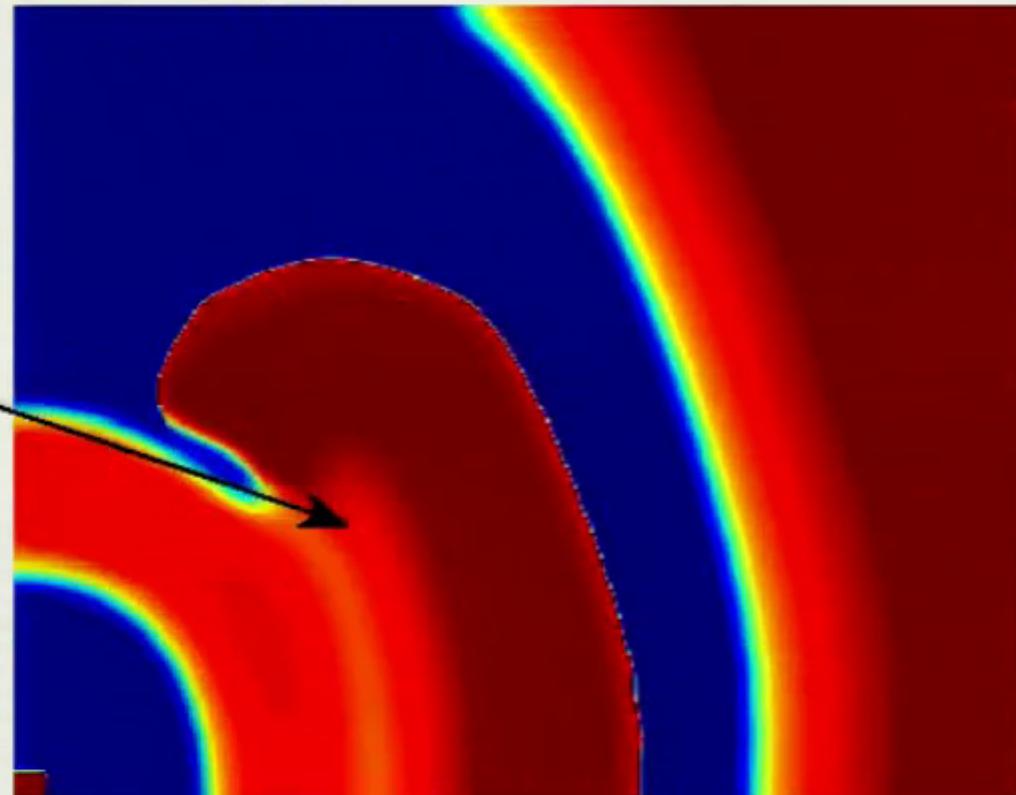
$t = 3582$





# Alternans: Possible Precursor to fibrillation

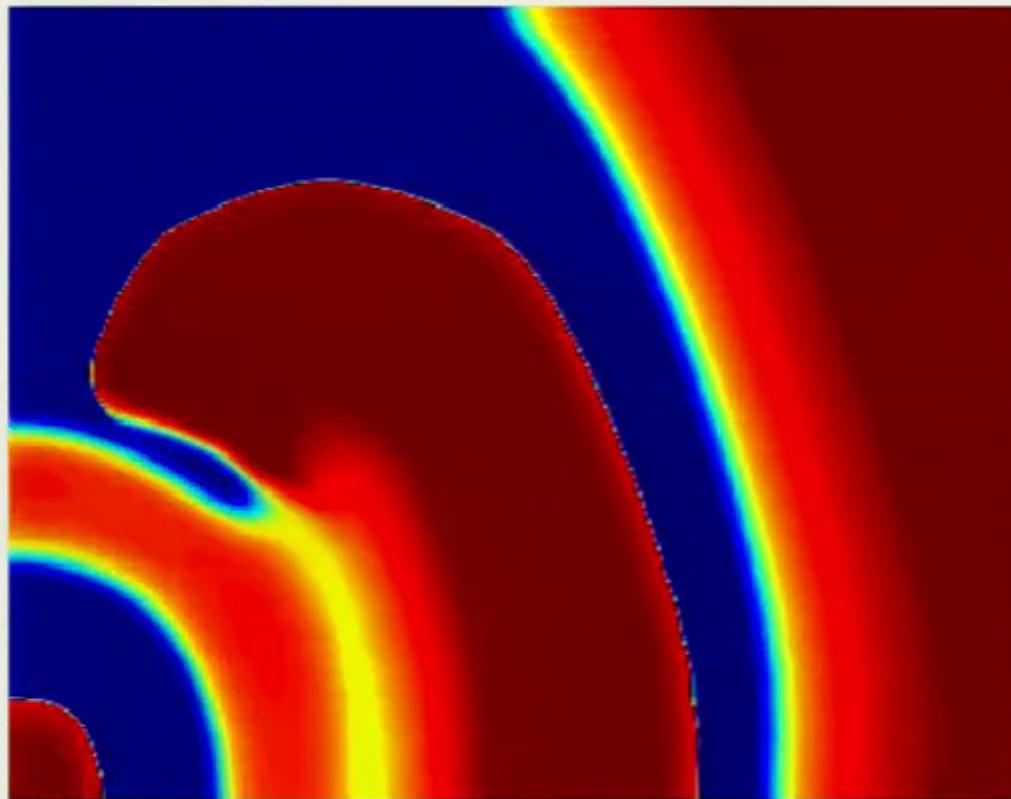
$t = 3782$





# Alternans: Possible Precursor to fibrillation

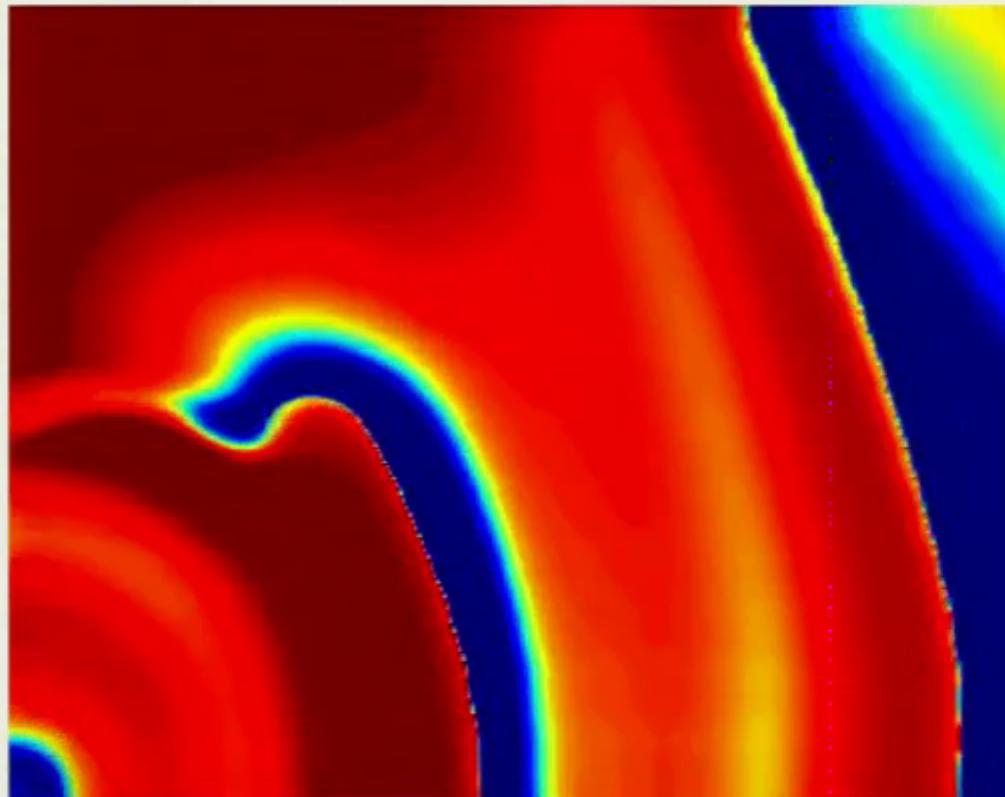
$t = 3806$





# Alternans: Possible Precursor to fibrillation

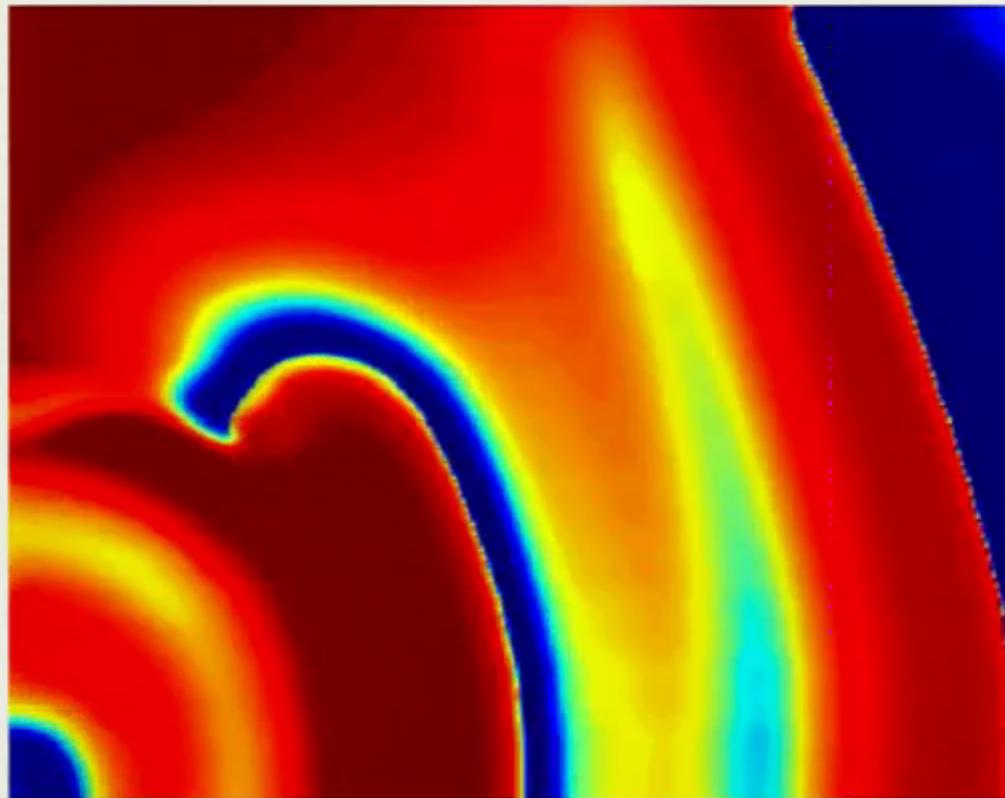
$t = 3974$





# Alternans: Possible Precursor to fibrillation

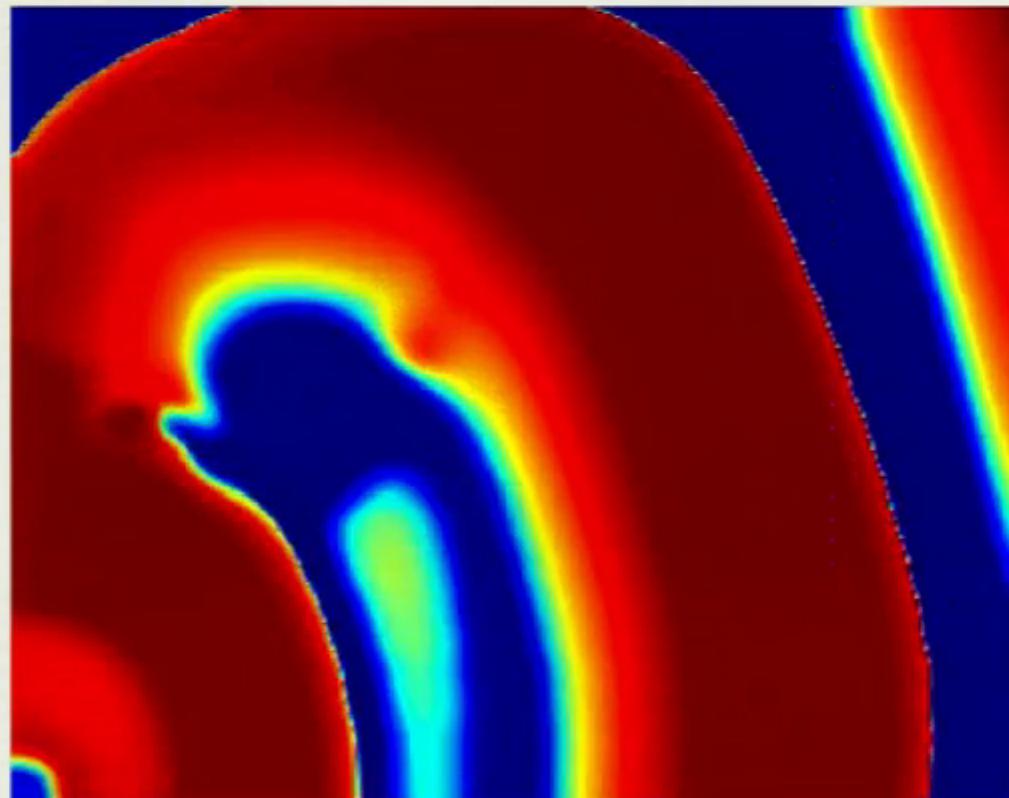
$t = 3998$





# Alternans: Possible Precursor to fibrillation

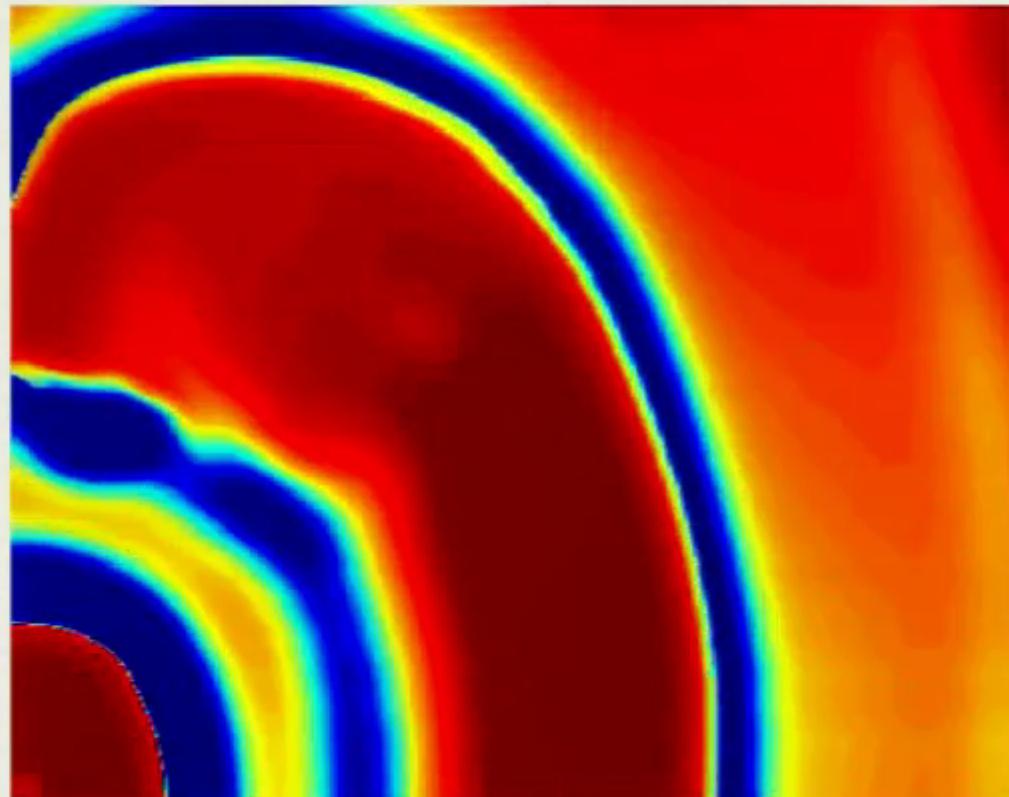
$t = 4186$





# Alternans: Possible Precursor to fibrillation

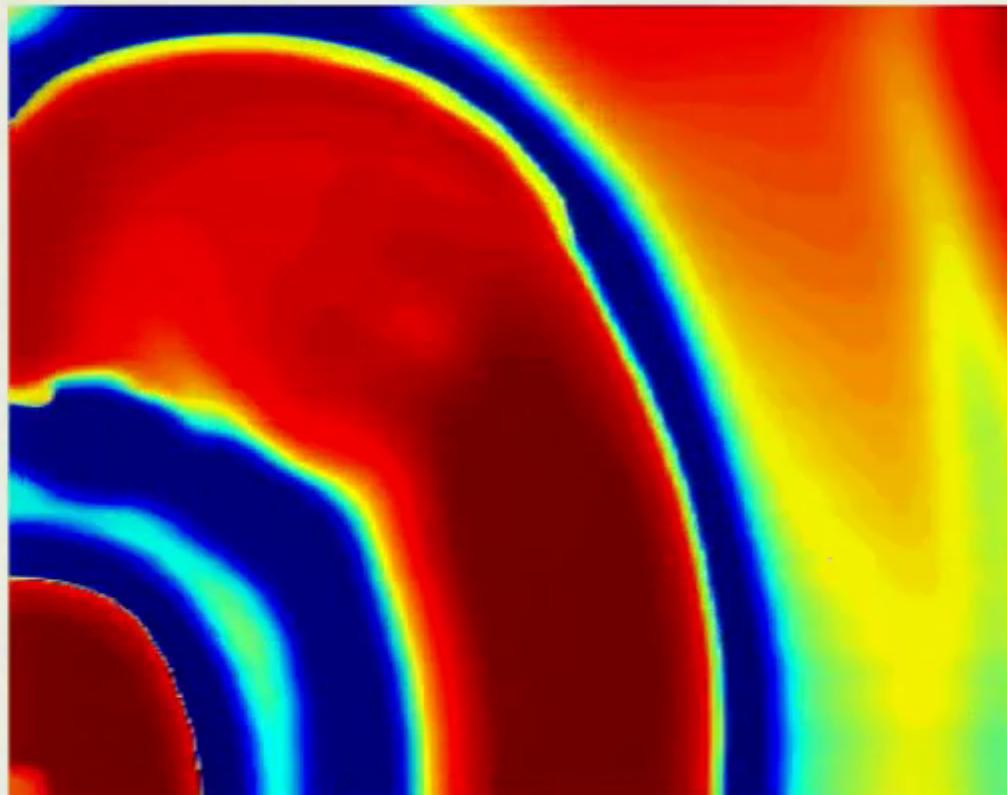
$t = 4370$





# Alternans: Possible Precursor to fibrillation

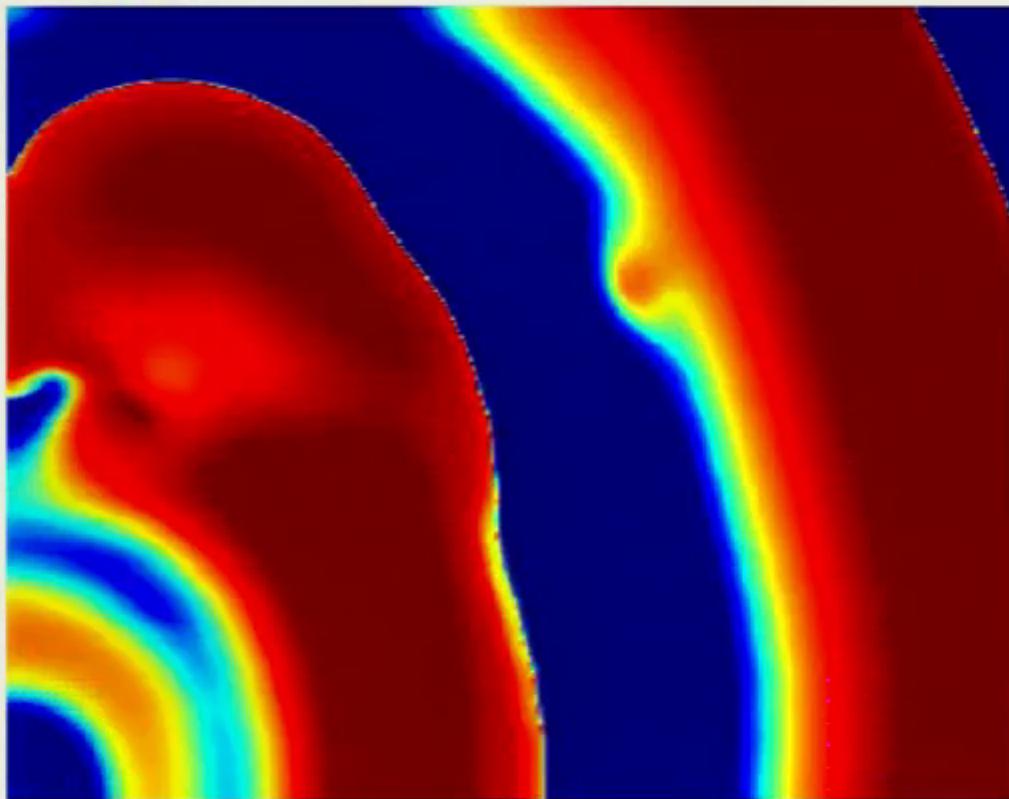
$t = 4386$





# Alternans: Possible Precursor to fibrillation

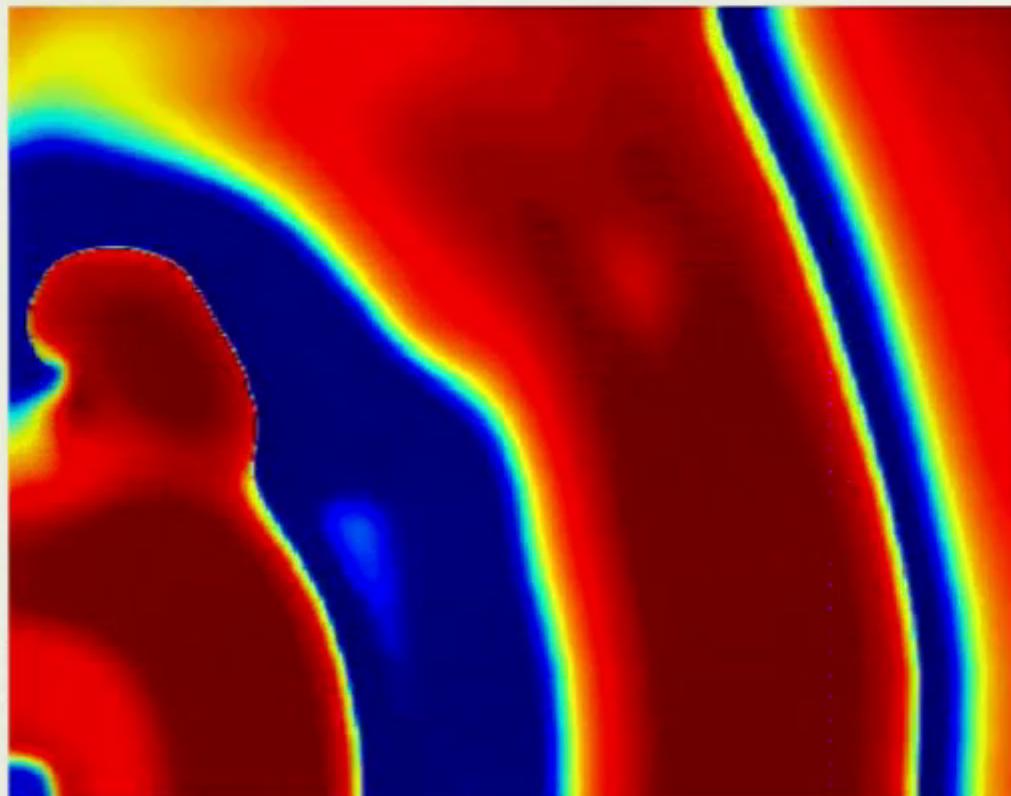
$t = 4566$





# Alternans: Possible Precursor to fibrillation

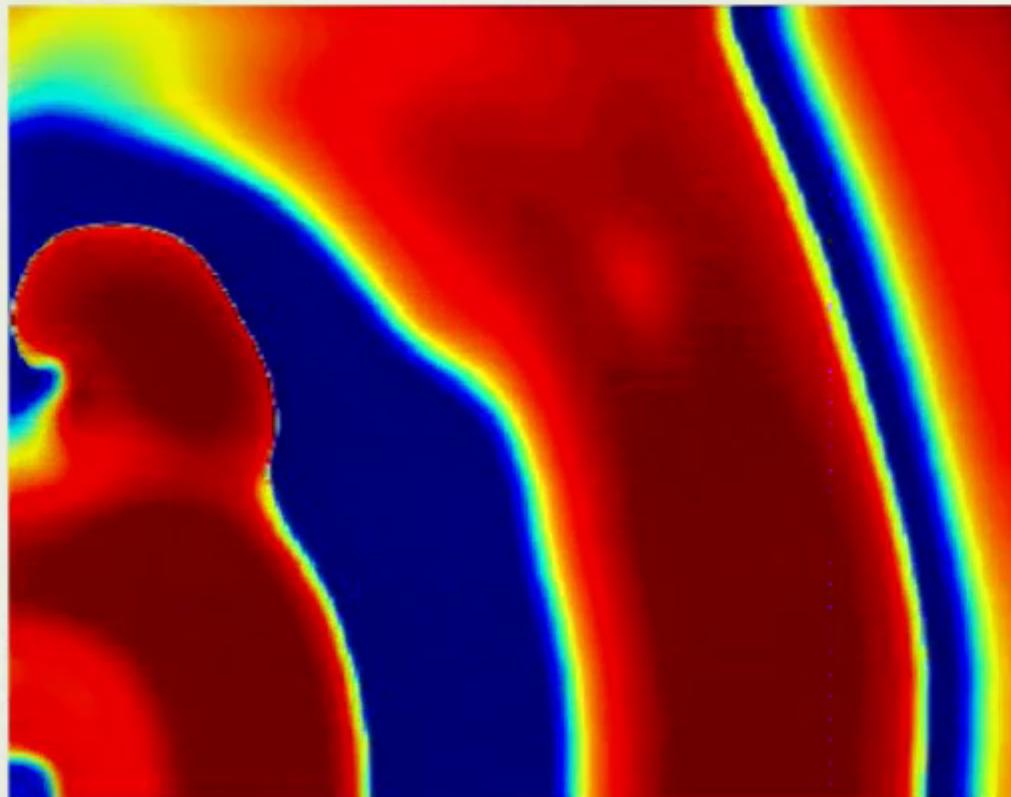
$t = 4734$





# Alternans: Possible Precursor to fibrillation

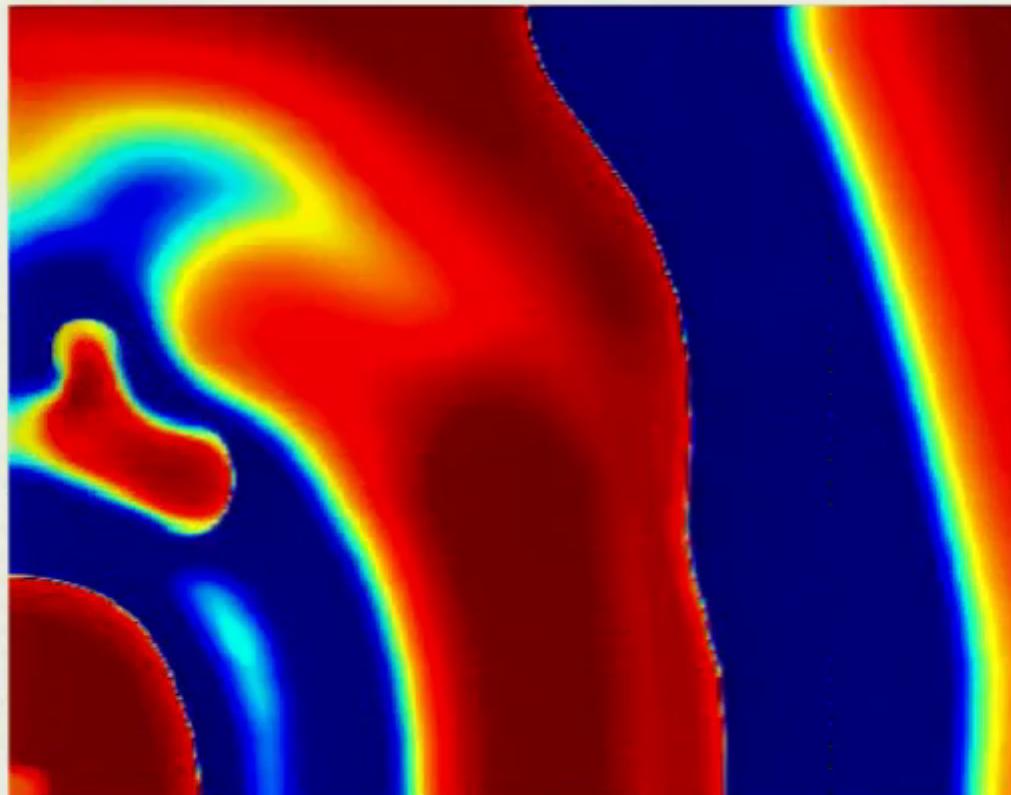
$t = 4742$





# Alternans: Possible Precursor to fibrillation

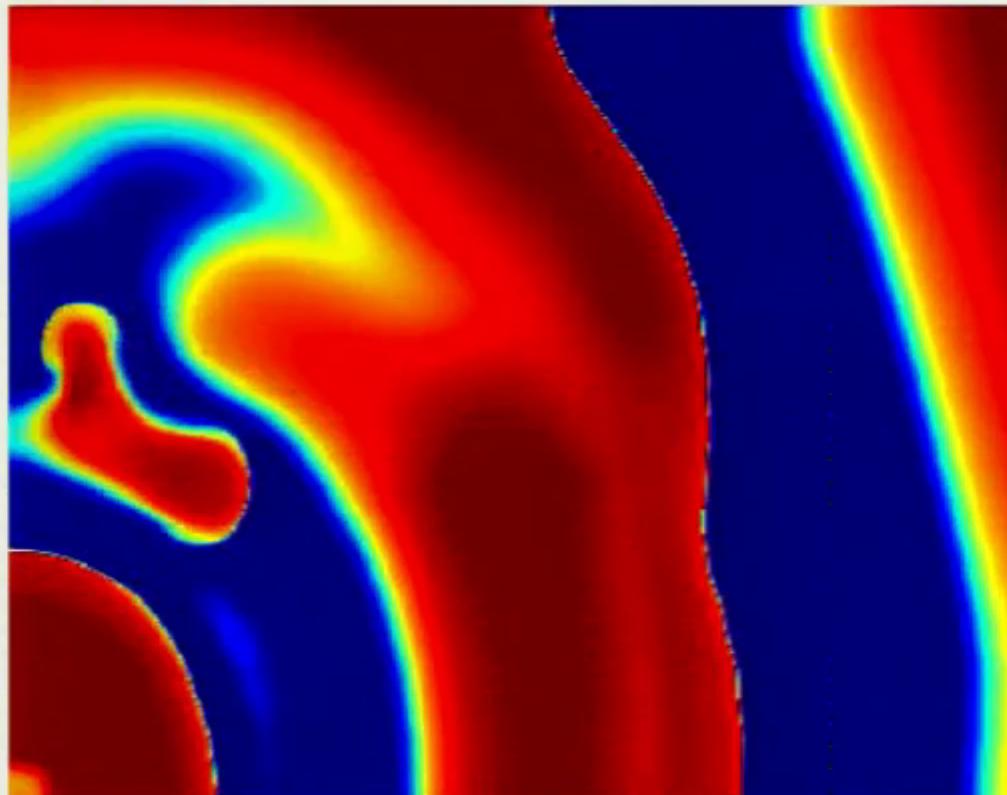
$t = 4926$





# Alternans: Possible Precursor to fibrillation

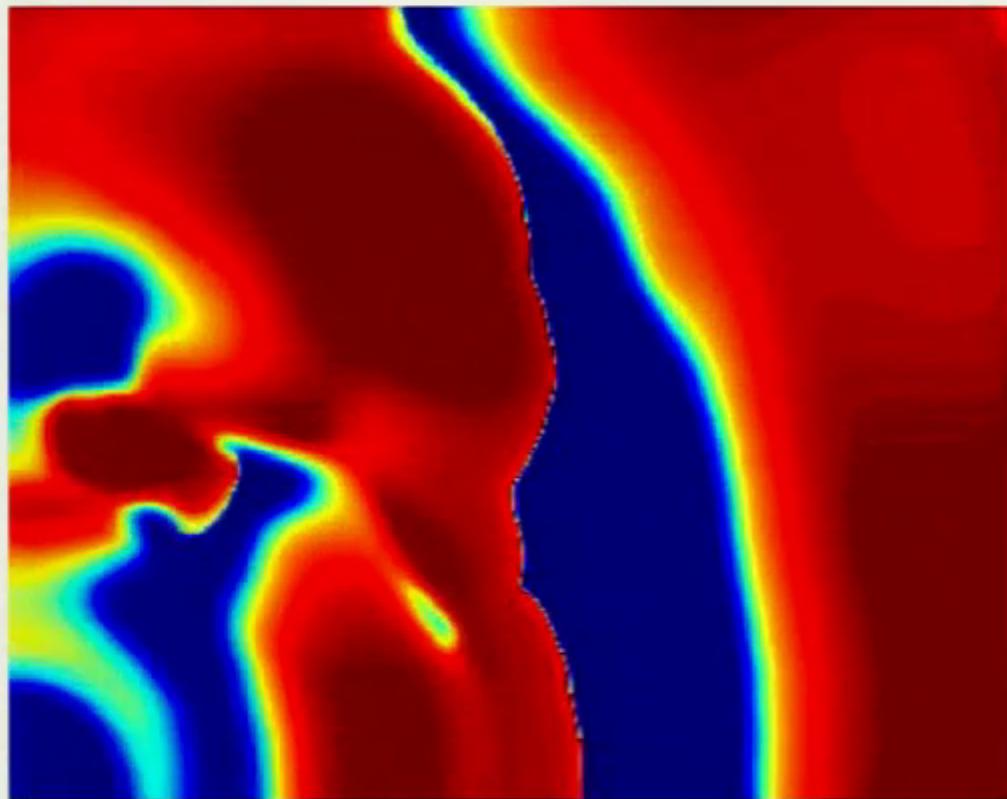
$t = 4934$





# Alternans: Possible Precursor to fibrillation

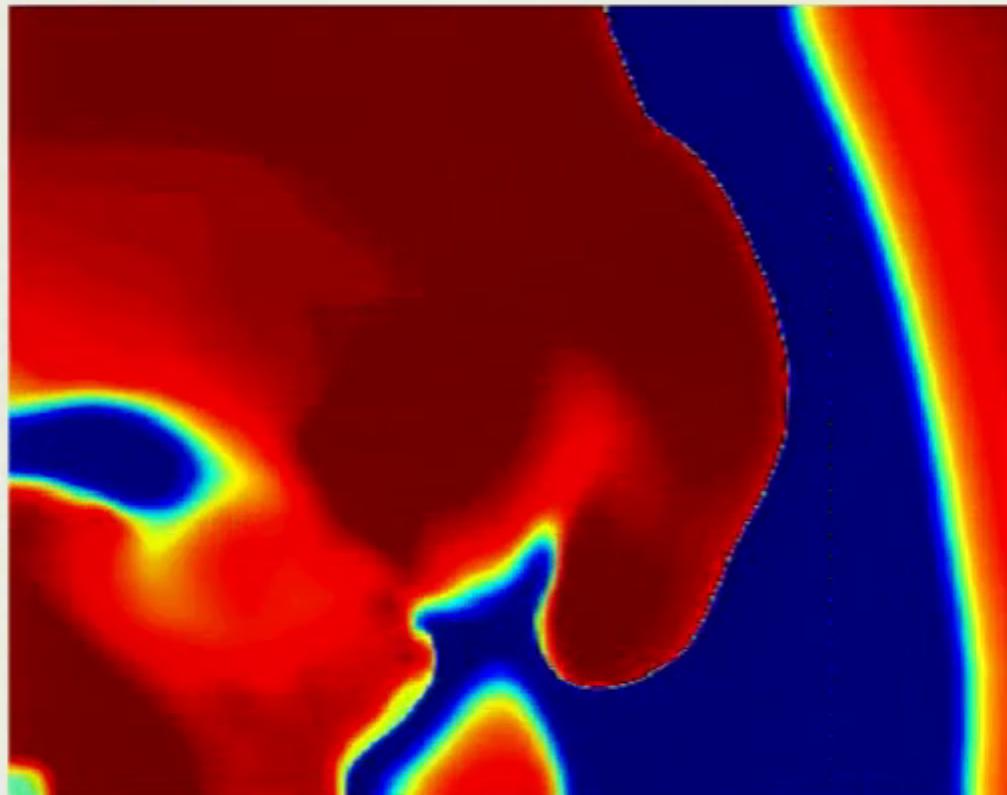
$t = 5122$





# Alternans: Possible Precursor to fibrillation

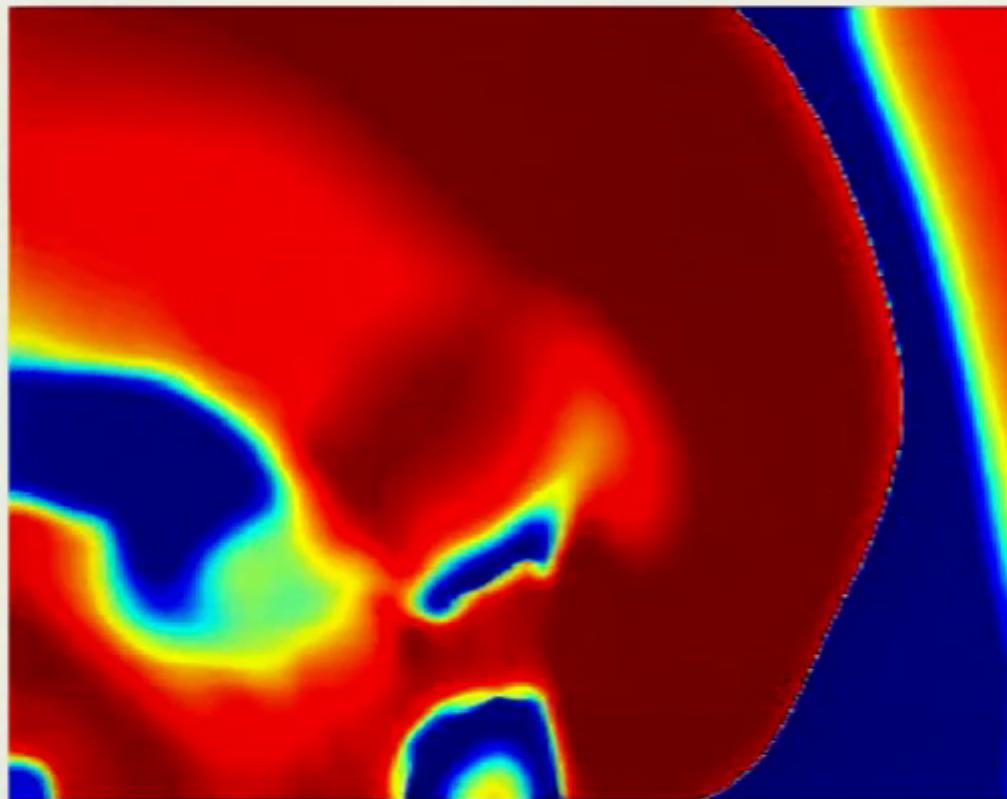
$t = 5498$





# Alternans: Possible Precursor to fibrillation

$t = 5542$





## Alternans Control Objective:

- find electrical stimulus which stabilizes period-1 action potentials using minimal power

# Isostables



$$\frac{d\mathbf{x}}{dt} = \mathbf{F}(\mathbf{x}), \quad \mathbf{x} \in \mathbb{R}^n$$

stable fixed point  $\mathbf{x}^*$

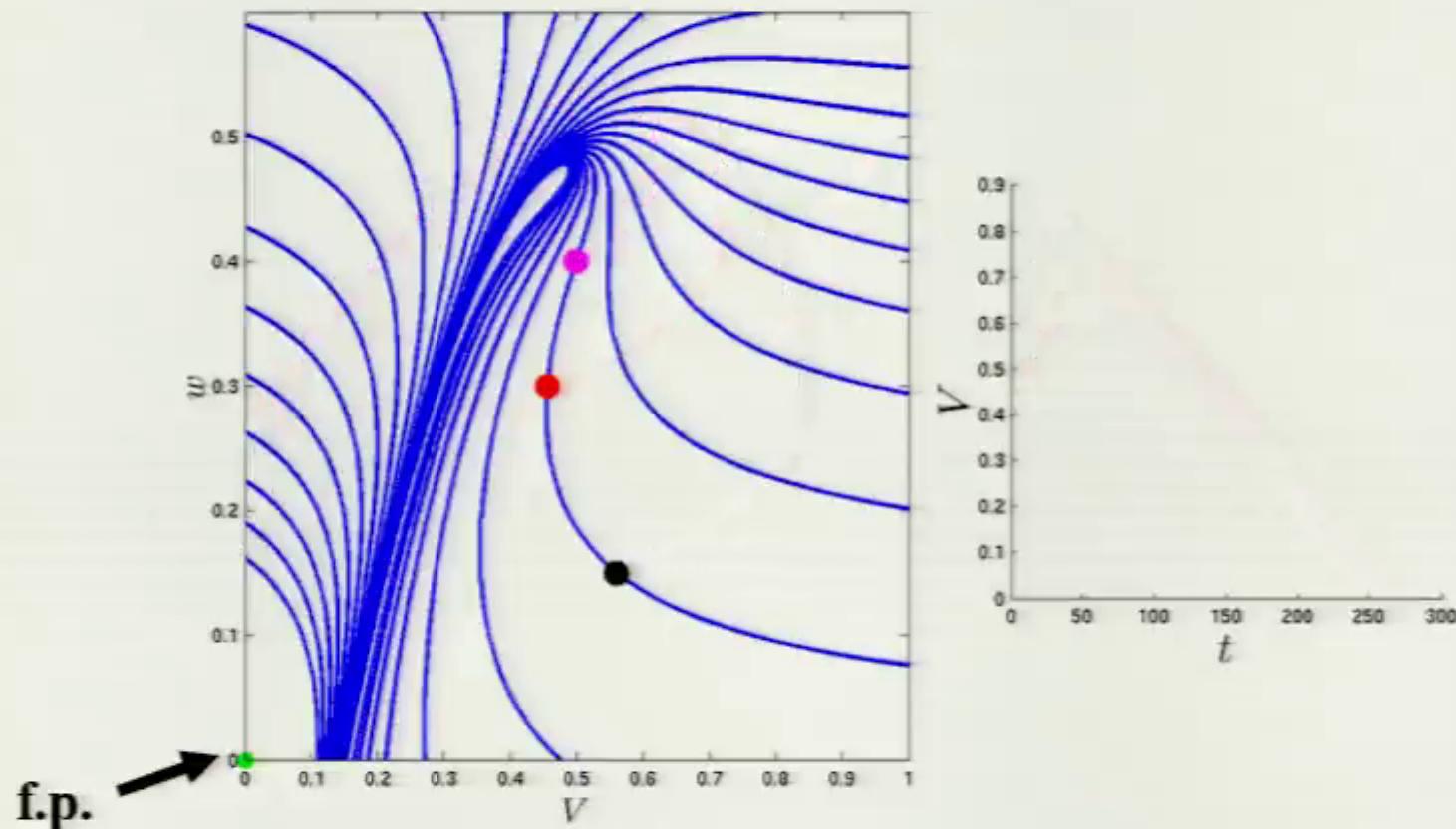
isostable:

- a set of initial conditions that share the same asymptotic convergence to a fixed point
- a level set of phase-like variable  $\psi(\mathbf{x})$

$$\boxed{\frac{d\psi}{dt} = \kappa}$$



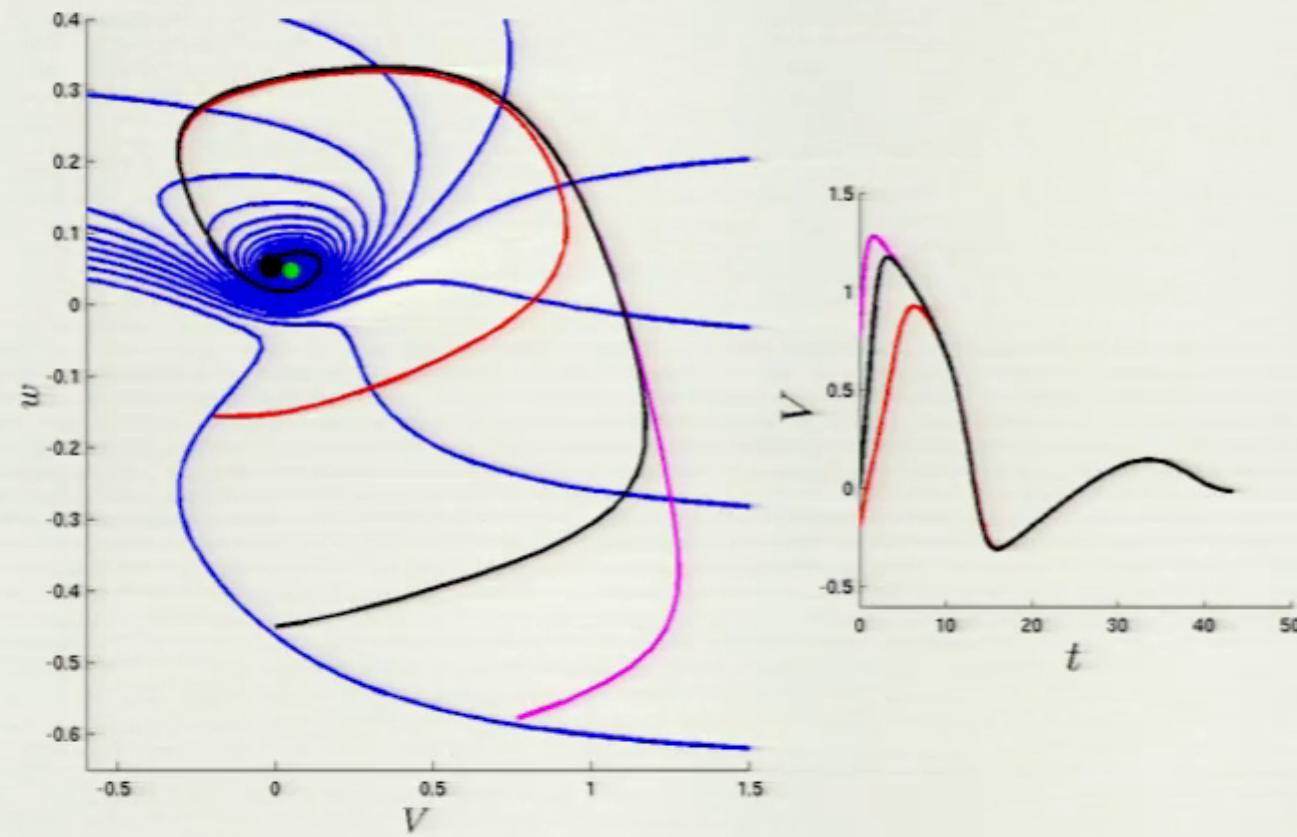
Initial Conditions Same Isostable (Real Evalues)



Mauroy, Mezic, M – *Physica D* 2013



Initial Conditions Same Isostable (Complex Evalues)



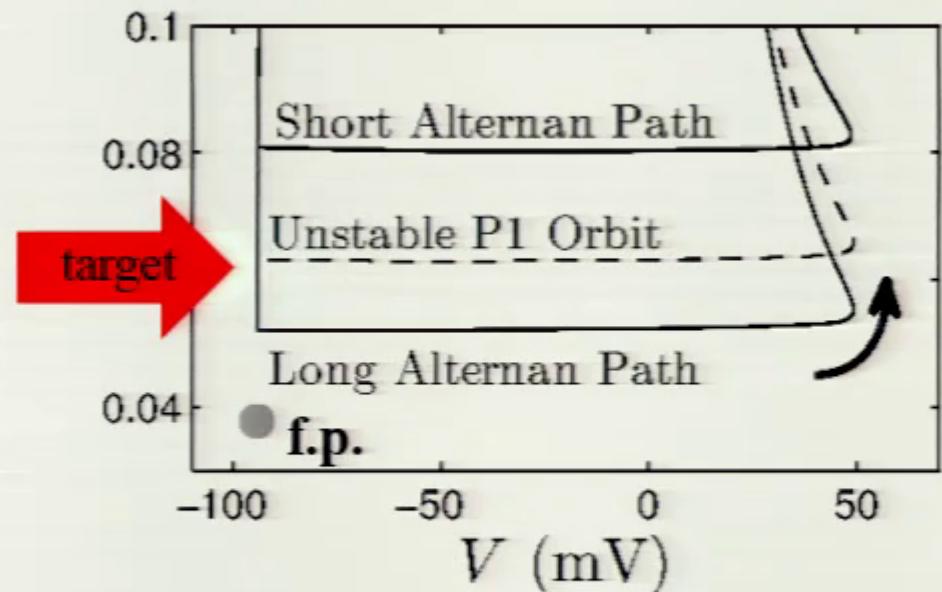
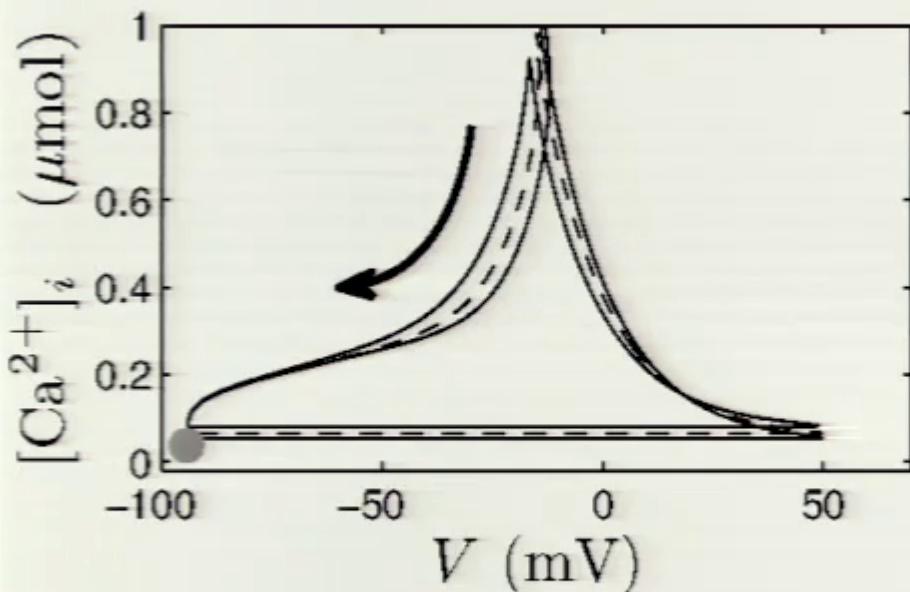
Mauroy, Mezic, M – *Physica D* 2013



# Control based on Isostable Reduction

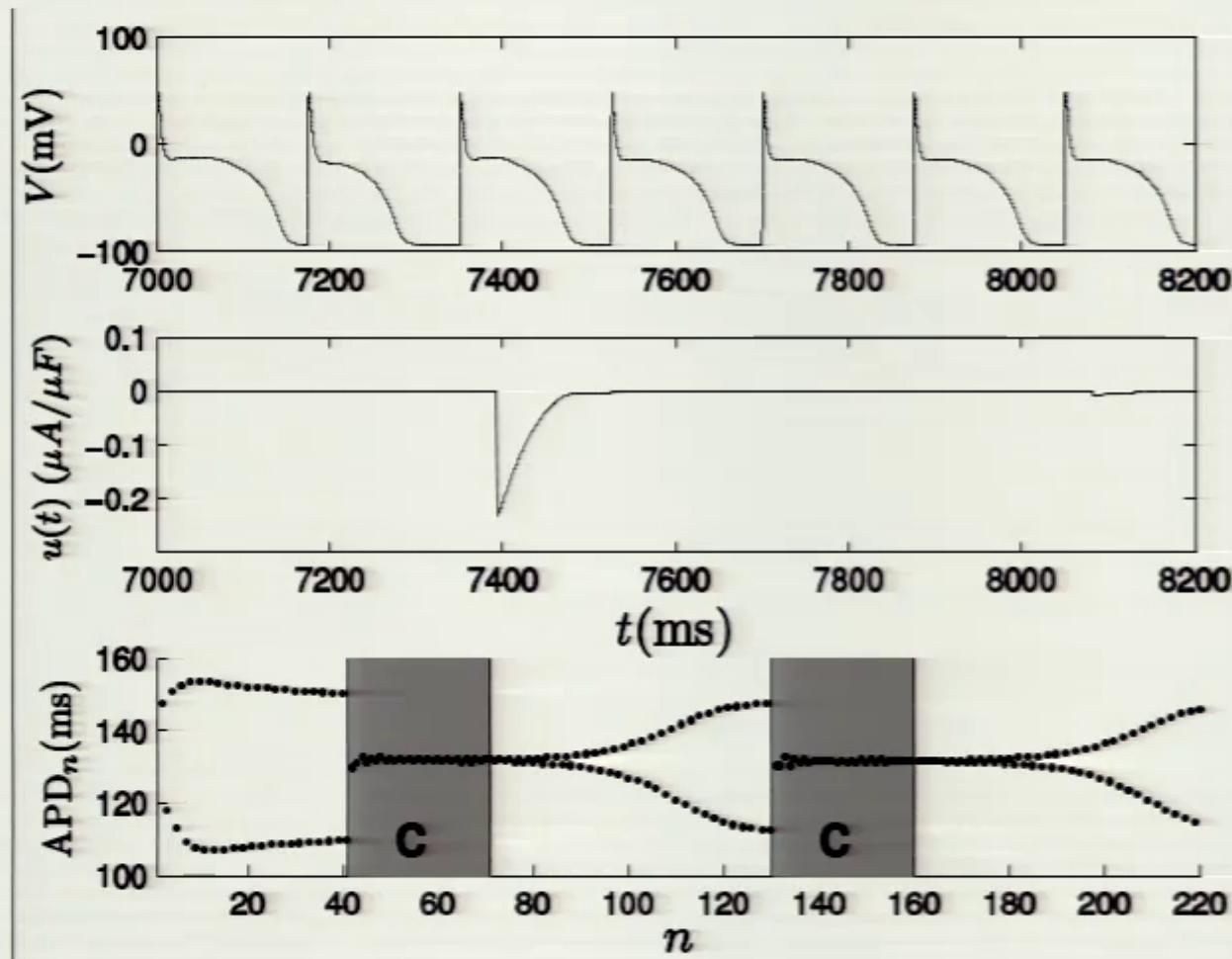
$$\frac{d\psi}{dt} = \kappa + I(\psi)u(t)$$

$u(t)$  is input current,  $I(\psi)$  is isostable response curve





# Control based on Isostable Reduction





## Control based on Isostable Reduction of PDEs

Consider a ring of connected cardiac tissue:

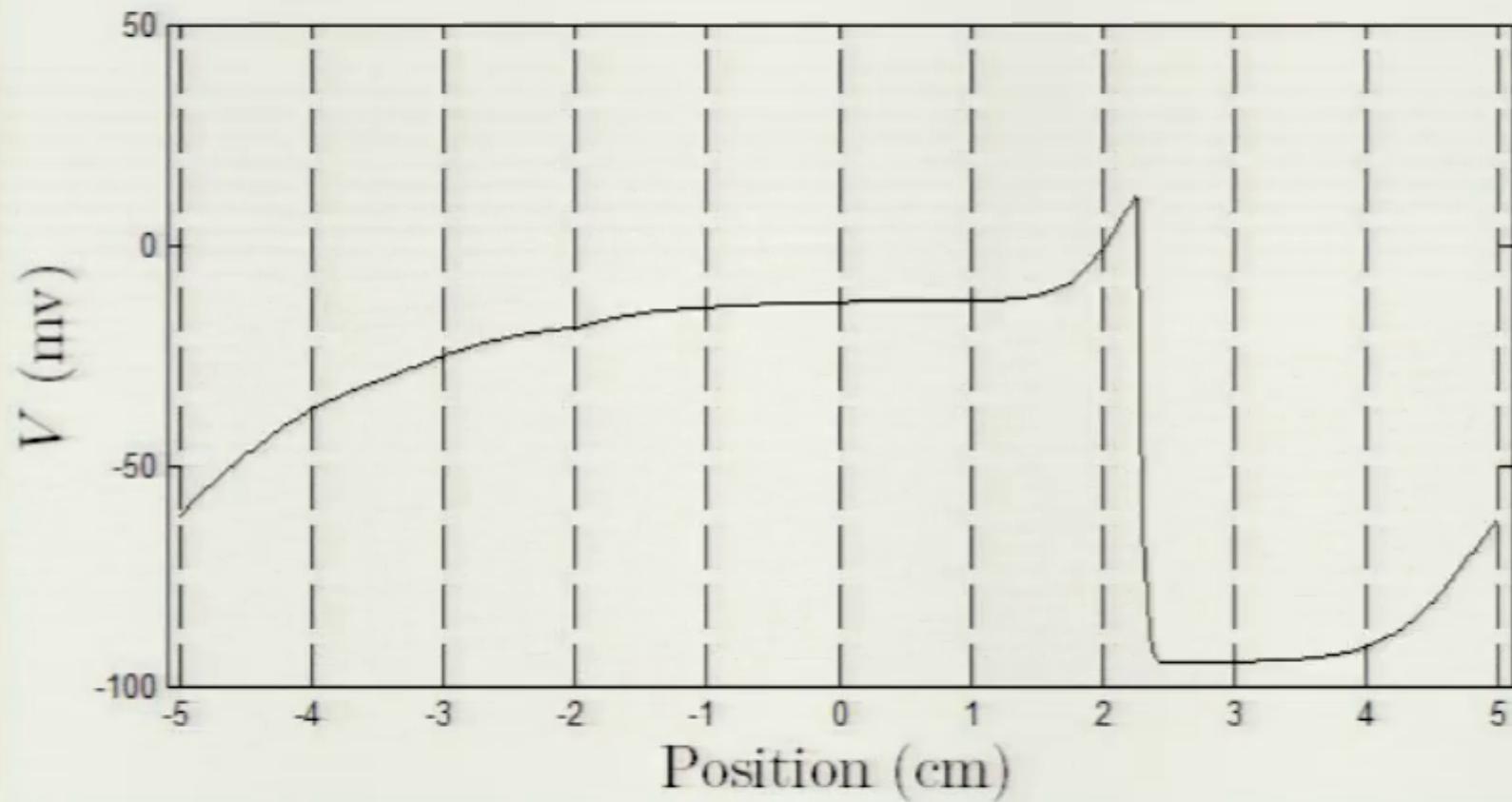
$$C_m \frac{\partial V(r, t)}{\partial t} = D \frac{\partial^2}{\partial r^2} V(r, t) + (-I_{ion} + I_{stim}(r, t)).$$

After isostable reduction:

$$\dot{\psi} = \kappa + \langle \mathcal{I}(r, \psi), I_{stim}(r, \psi) \rangle.$$



# Control based on Isostable Reduction of PDEs



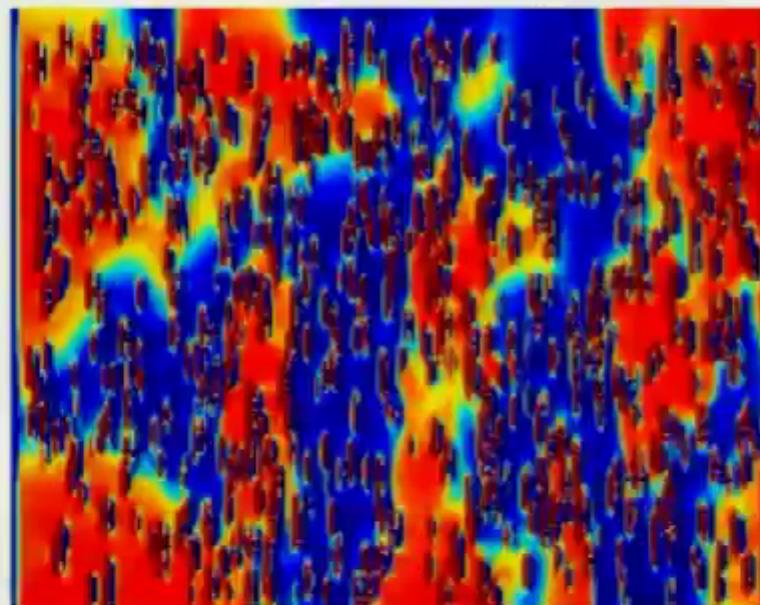


## Fibrillation Control Objective:

- find electrical stimulus which eliminates recurrent spiral waves by synchronizing the cell activity



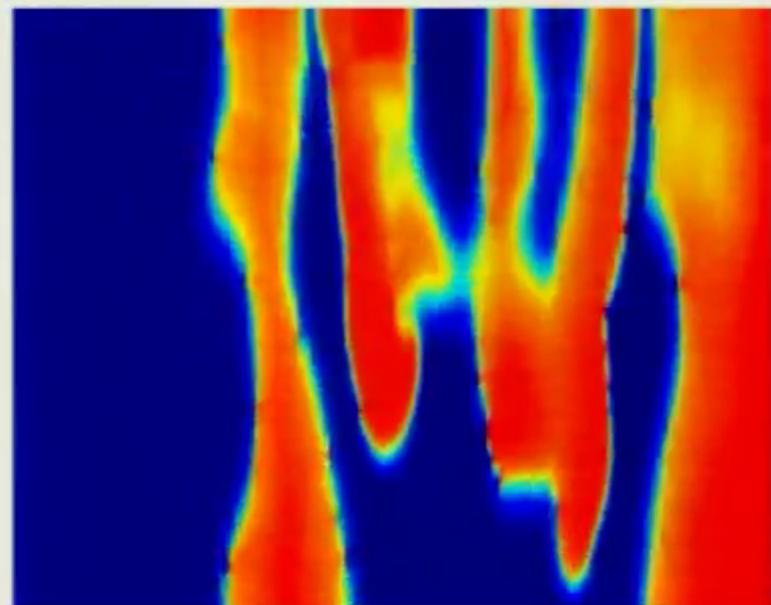
Unsuccessful “Defibrillation”:  
single pulse



Wilson, M – submitted



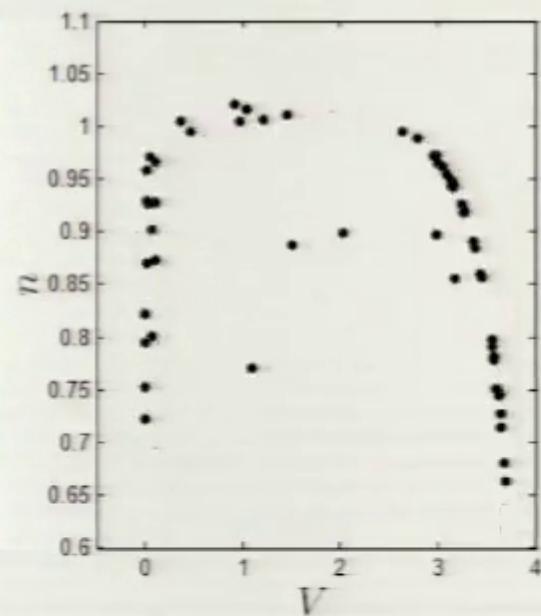
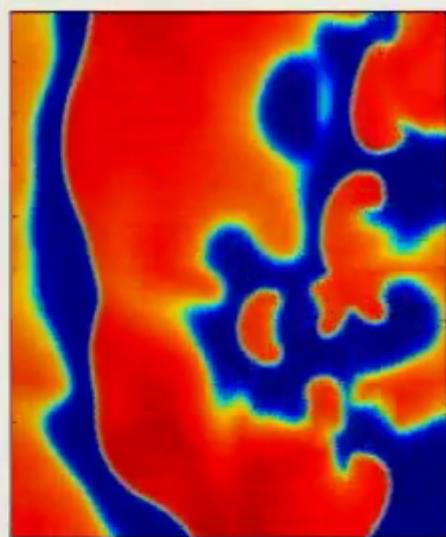
Unsuccessful “Defibrillation”:  
single pulse



Wilson, M – submitted

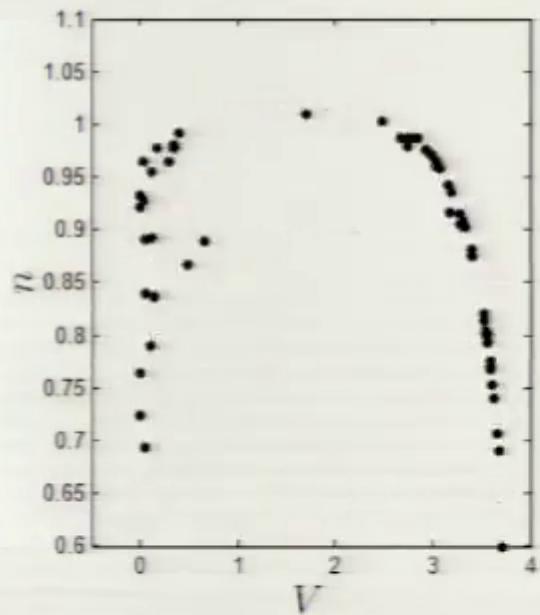
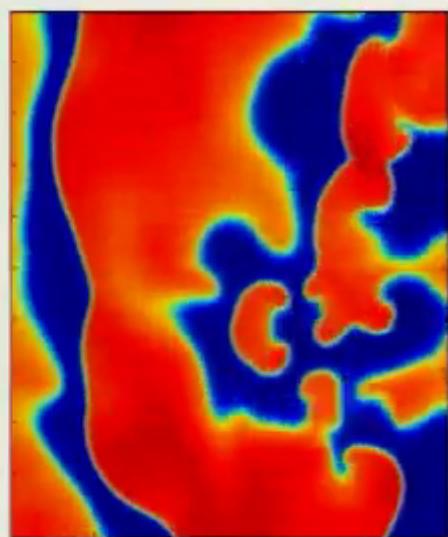


Cell Dynamics Follow Transient Attractor:  
can reduce dimensionality



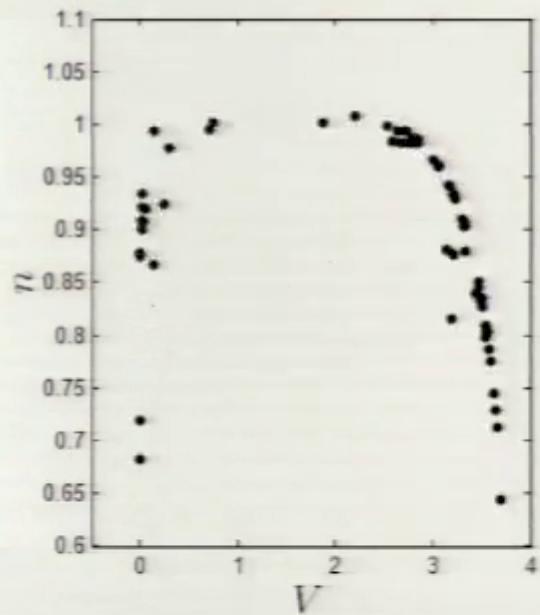
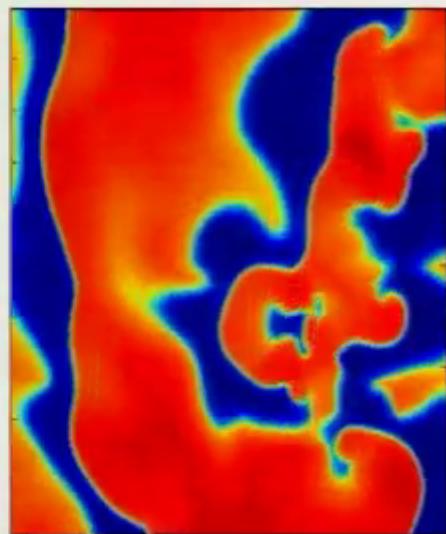


Cell Dynamics Follow Transient Attractor:  
can reduce dimensionality



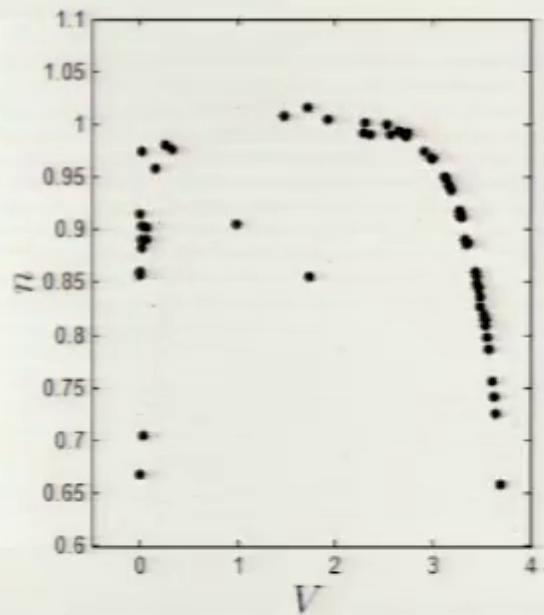
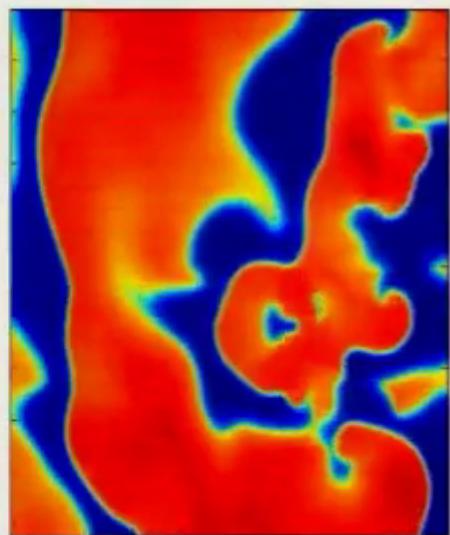


# Cell Dynamics Follow Transient Attractor: can reduce dimensionality



Wilson, M – submitted

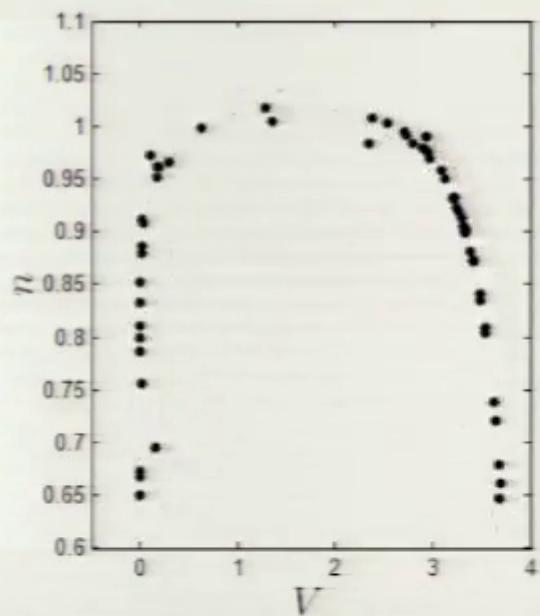
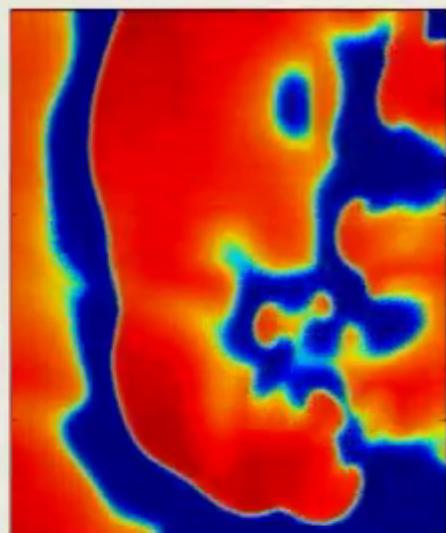
## Cell Dynamics Follow Transient Attractor: can reduce dimensionality



Wilson, M – submitted

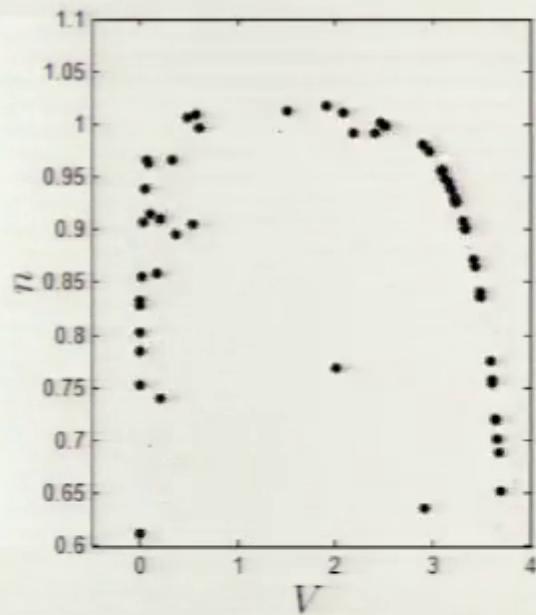
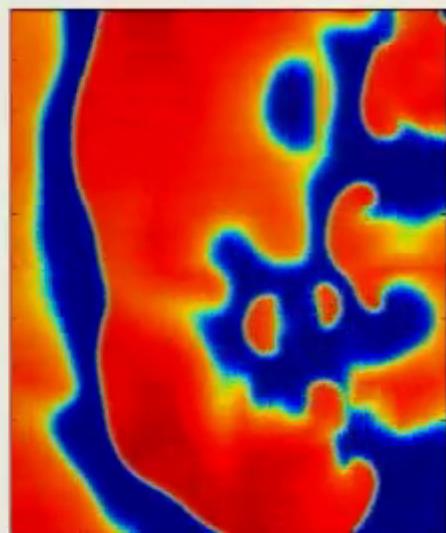


# Cell Dynamics Follow Transient Attractor: can reduce dimensionality





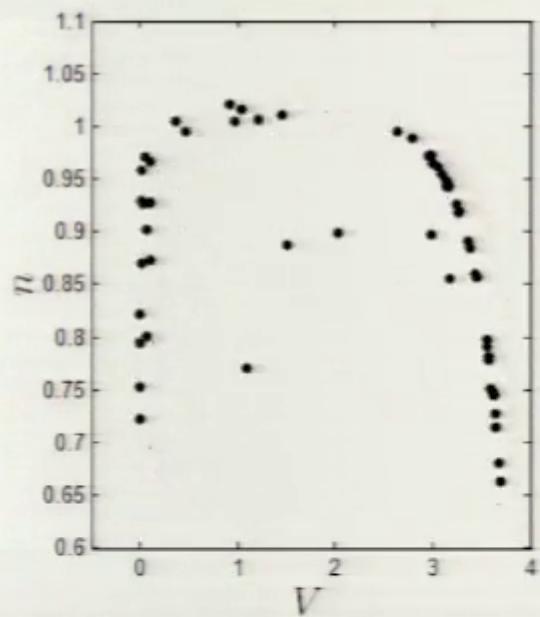
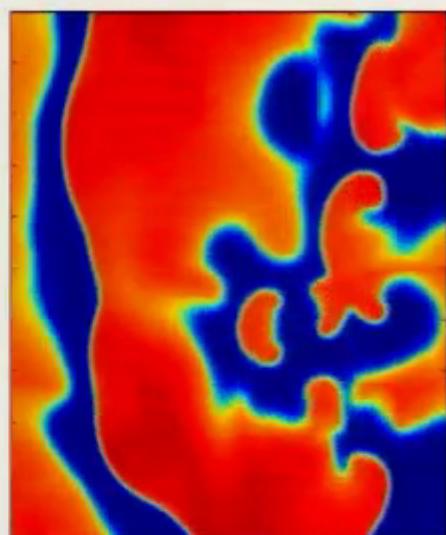
# Cell Dynamics Follow Transient Attractor: can reduce dimensionality



Wilson, M – submitted

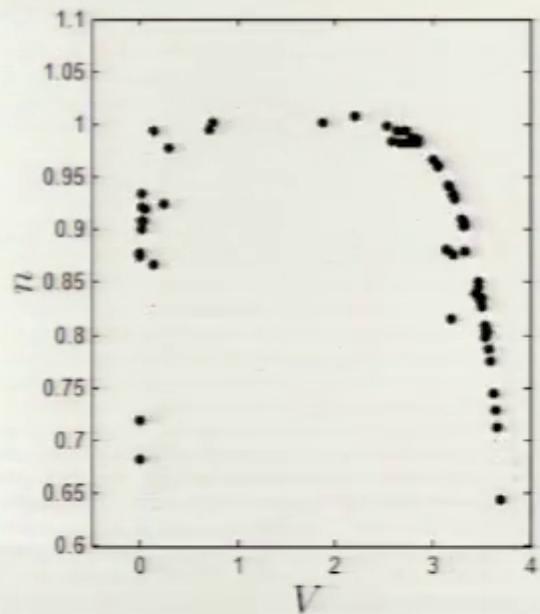
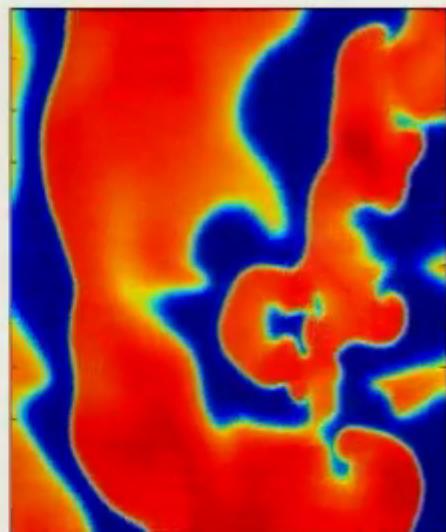


Cell Dynamics Follow Transient Attractor:  
can reduce dimensionality





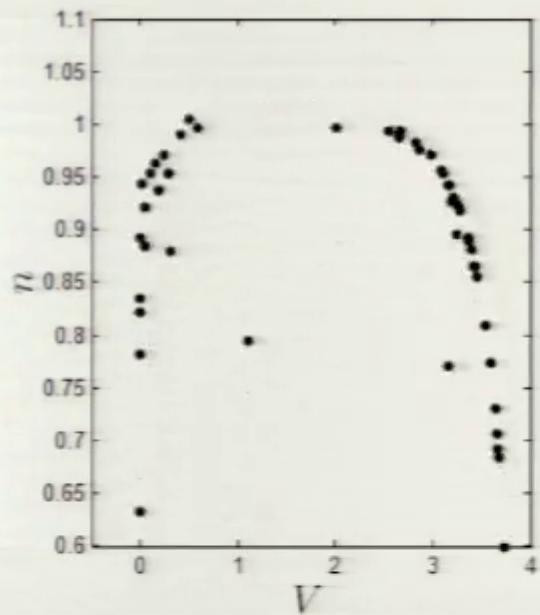
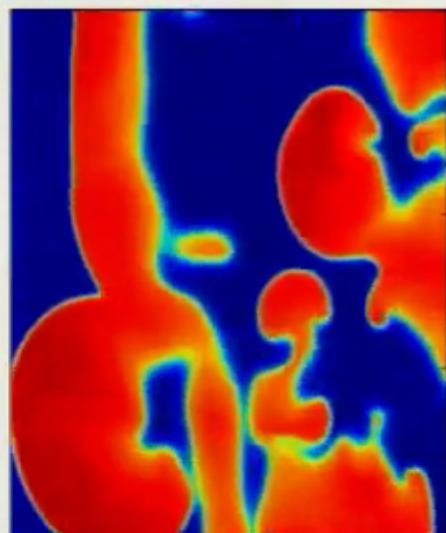
Cell Dynamics Follow Transient Attractor:  
can reduce dimensionality



Wilson, M – submitted



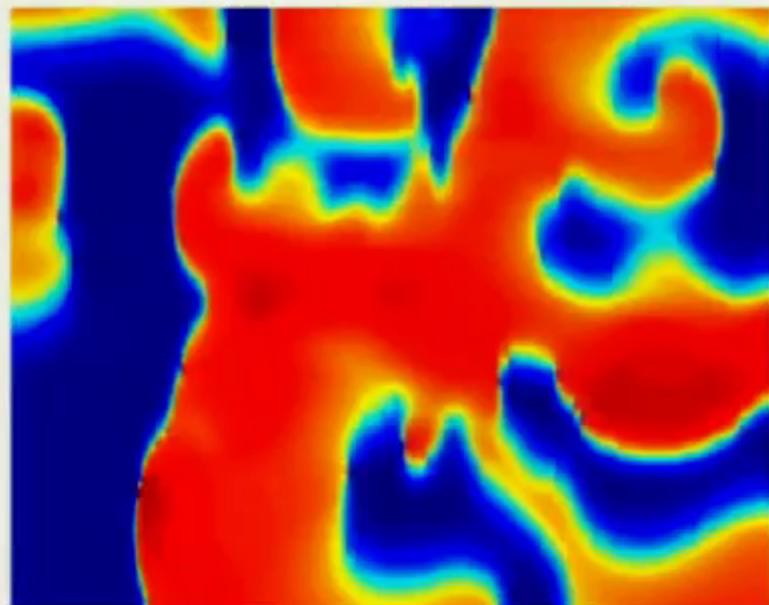
# Cell Dynamics Follow Transient Attractor: can reduce dimensionality



Wilson, M – submitted

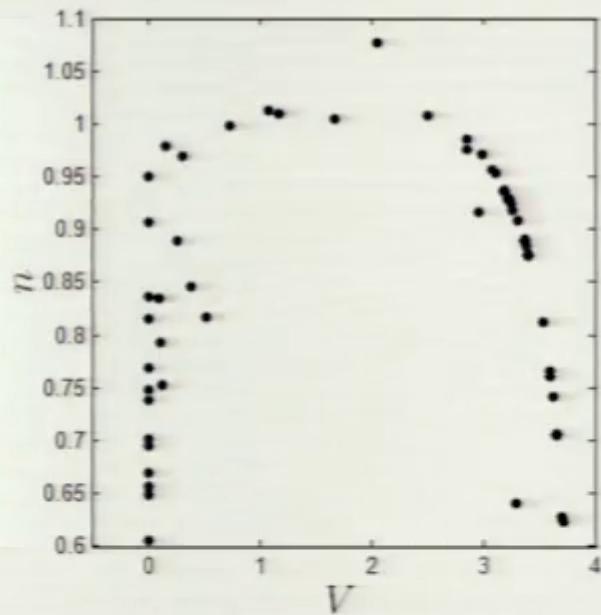
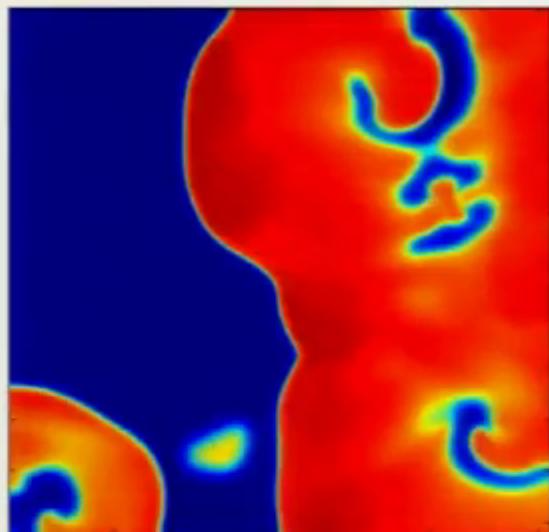
Successful “Defibrillation”:

pulse timing found using dynamic programming  
which optimizes synchronization of cell activity



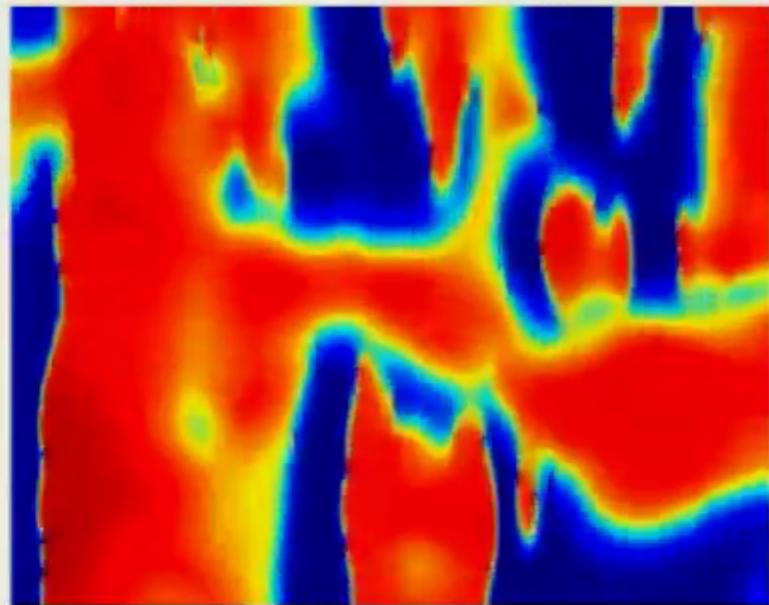


# Cell Dynamics Follow Transient Attractor: can reduce dimensionality

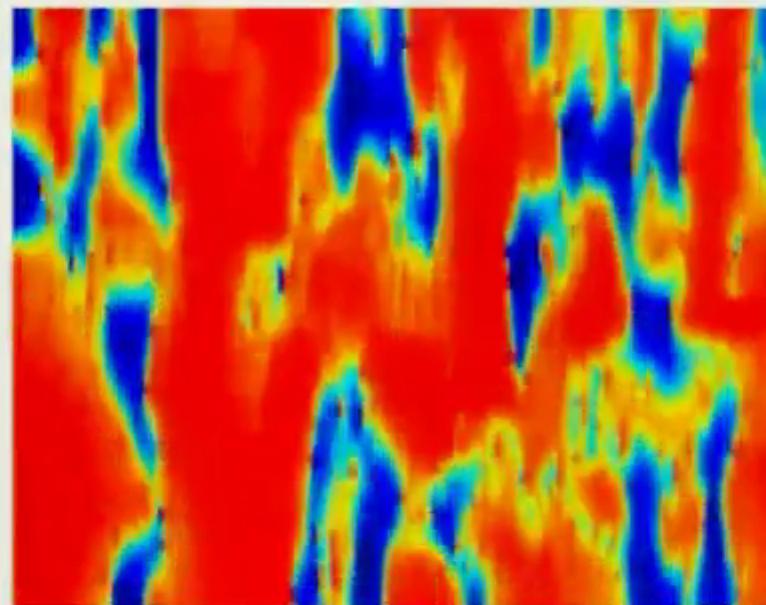


Wilson, M – submitted

Successful “Defibrillation”:  
pulse timing found using dynamic programming  
which optimizes synchronization of cell activity

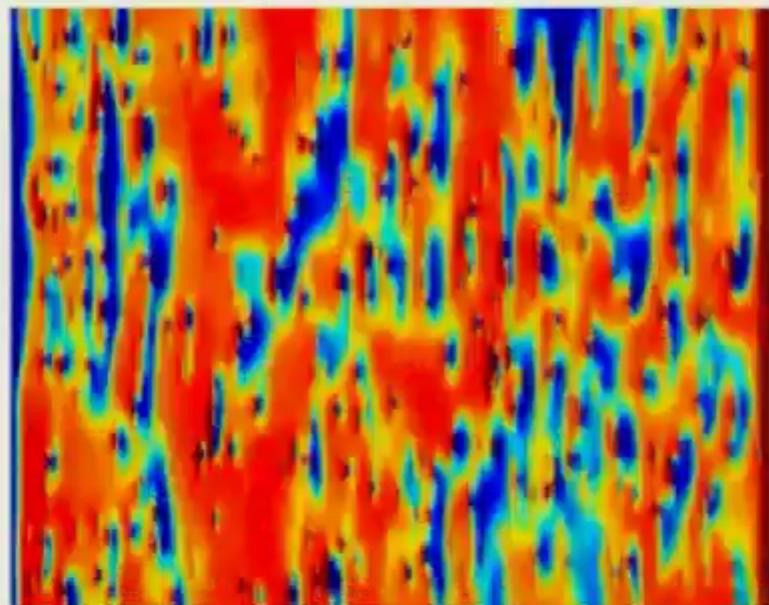


Successful “Defibrillation”:  
pulse timing found using dynamic programming  
which optimizes synchronization of cell activity



Successful “Defibrillation”:

pulse timing found using dynamic programming  
which optimizes synchronization of cell activity



Successful “Defibrillation”:

pulse timing found using dynamic programming  
which optimizes synchronization of cell activity





# Desync from Isostable Reduction of PDEs

**Phase density evolves according to**

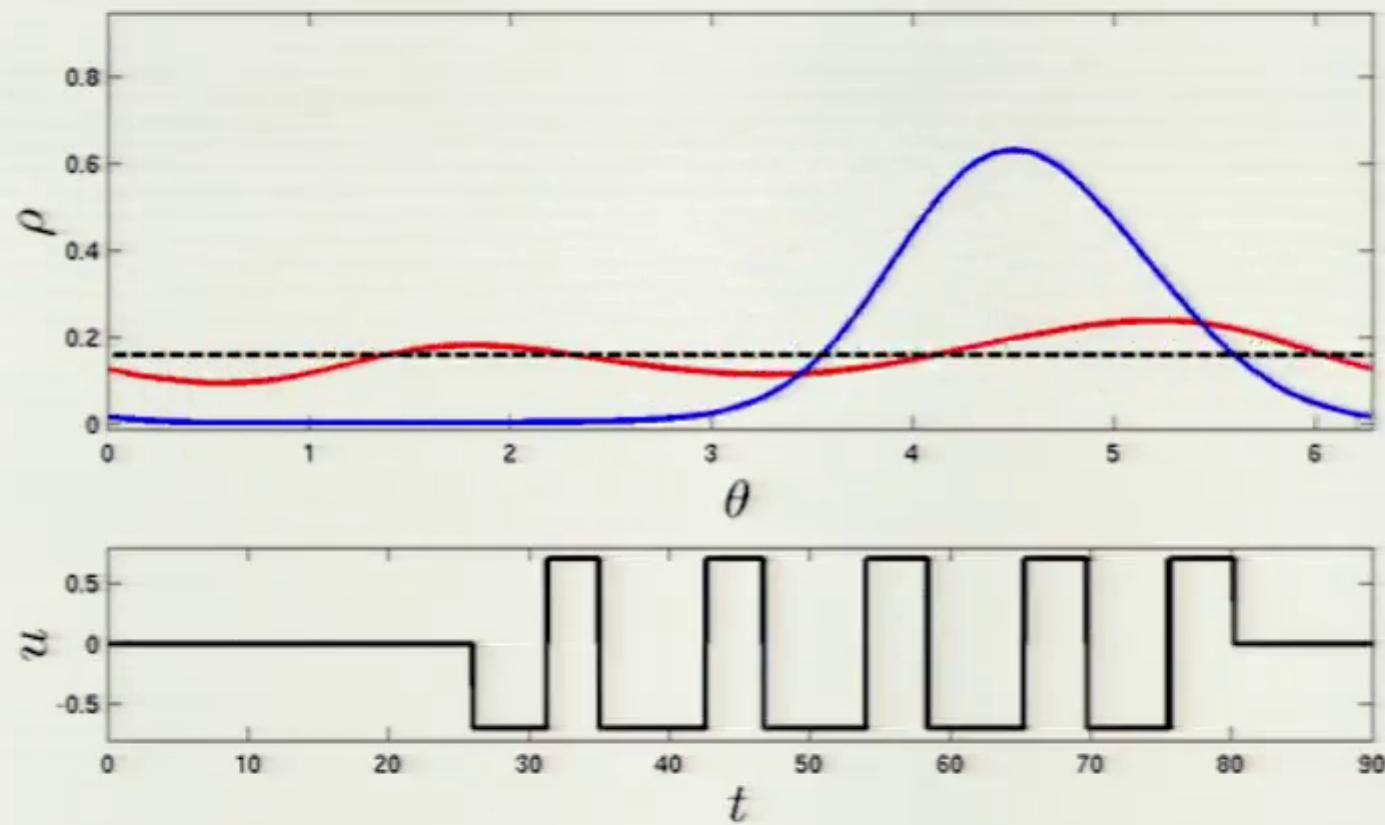
$$\frac{\partial \rho(\theta, t)}{\partial t} = -\omega \frac{\partial \rho}{\partial \theta} + \frac{B^2}{2} \frac{\partial^2 \rho}{\partial \theta^2} + \text{input} + \text{coupling}.$$

**After isostable reduction:**

$$\dot{\psi} = \kappa + \langle \mathcal{I}, \text{input} + \text{coupling} \rangle.$$



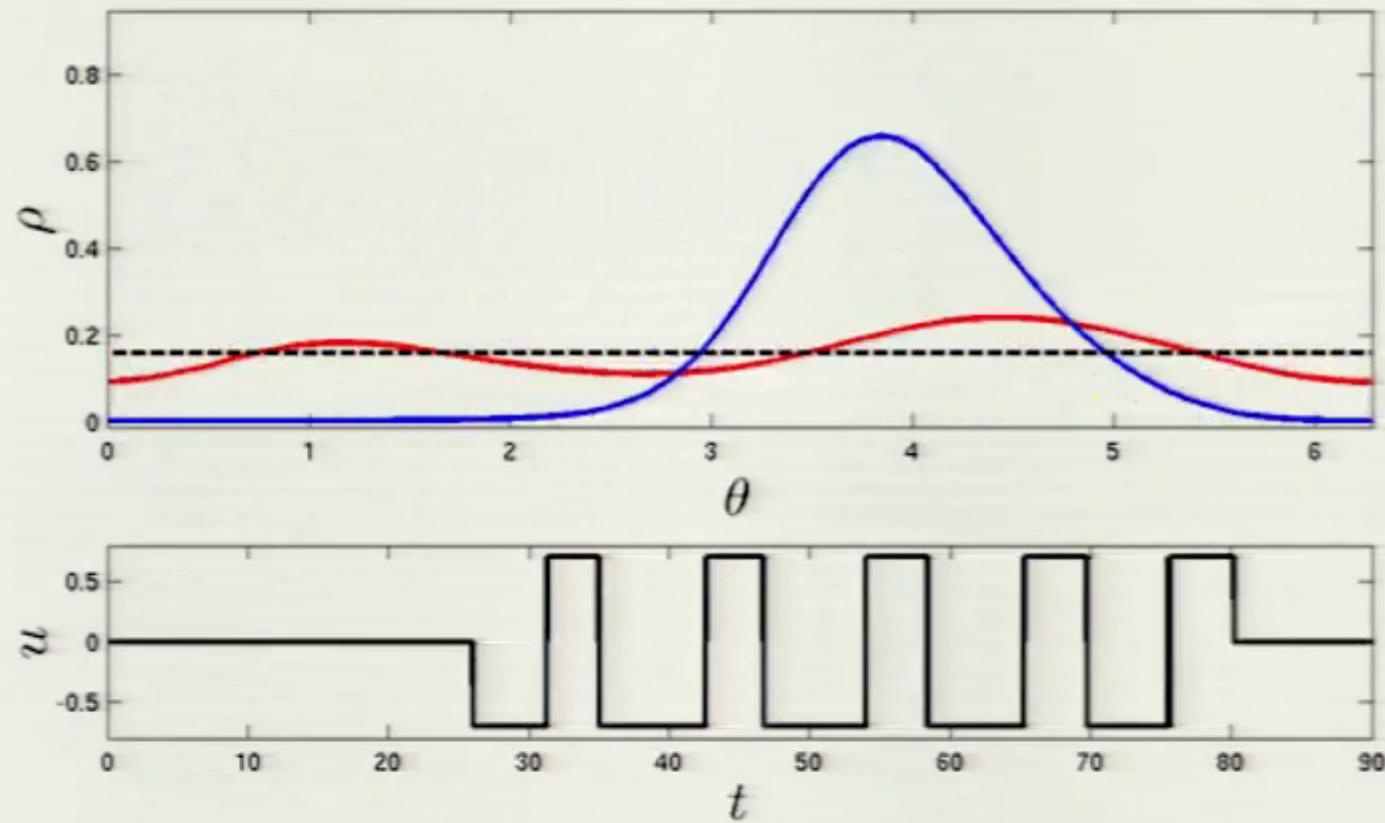
# Desync from Isostable Reduction of PDEs



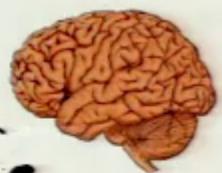
Wilson, M – submitted



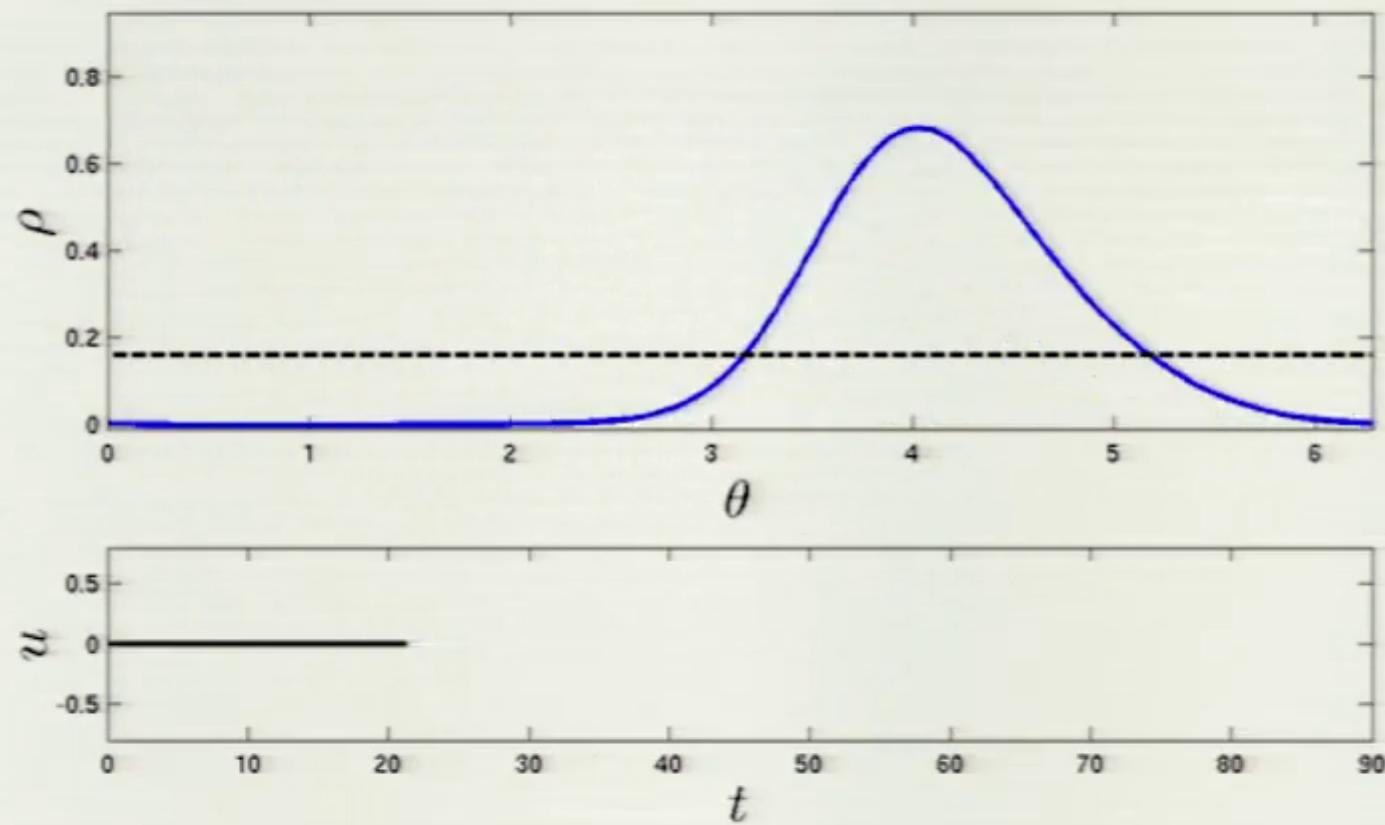
# Desync from Isostable Reduction of PDEs



Wilson, M – submitted



# Desync from Isostable Reduction of PDEs



# Other Related Research

- Chaotic desync for extracellular stimulation
  - Wilson, M - *JCNS* 2014
- Time optimal phase resetting
  - Danzl, Hespanha, M – *Bio Cyb* 2009
- Dynamic programming control of neural populations
  - Nabi, M - *J Neural Engr* 2011
- Control with time-delayed signals
  - Orosz, M, Murray - *Bio Cyb* 2010
- Control of circadian oscillators
  - Wilson, M - *Biophys J* 2014
- Experimental control of neurons
  - Wilson, Holt, Netoff, M – *Front Neuro* 2015
  - Nabi, Stigen, M, Netoff - *J Neural Engr* 2013
  - Stigen, Danzl, M, Netoff - *J Neurophys* 2011
- Experimental control of chemical oscillators
  - w/ Ken Showalter's group, Tay Netoff's group

# Collaborators on the Presented Work

## UCSB

- Dan Wilson
- Miles Detrixhe
- Frederic Gibou
- Igor Mezic

## Former UCSB

- Ali Nabi
- Mohammad Mirzadeh
- Marion Doubeck
- Blane Rhoads
- Alexandre Mauroy (now at U Liege)

## Auckland

- Hinke Osinga

# Other Recent Collaborators on Related Work

## Former and Current UCSB

- Per Danzl
- Tim Matchen
- Joao Hespanha
- Gabor Orosz (now U Mich)
- Gerd Schmidt (visitor from Stuttgart)

## U Minn

- Abbey Holt
- Tyler Stigen
- Tay Netoff

## WVU

- Ken Showalter
- Mark Tinsley

Thanks to the  
NSF for funding!

# Brain + Heart Control

It's not just for Mad Scientists!!

Parkinson's Disease

- chaotic desync
- optimal phase resetting

Cardiac Arrhythmias

- stabilize UPO
- pulse timing for sync

Reduction:

- isochrons
- isostables

Thank you!

BAD BRAINS