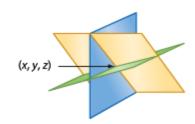
3.4: Systems of Equations in Three Variables

Equations in three variables are graphed as *planes*. As was the case when graphing lines, there may be:

- one solution expressed as an ordered triple, (x, y, z)
- no solution, ø
- an infinite number of solutions

One Solution

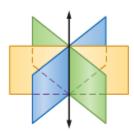
The three individual planes intersect at a specific point.



Infinitely Many Solutions

The planes intersect in a line.

Every coordinate on the line represents a solution of the system.



The planes intersect in the same plane.

Every equation is equivalent. Every coordinate in the plane represents a solution of the system.



No Solution There are no points in common with all three planes.







Steps to Solving Systems with Three Variables

- Pick two equations, and eliminate one variable from them.
 You'll be left with one equation, having 2 variables. Let's call this equation "YAY"
- 2) Pick another pair of equations, and eliminate the same variable you eliminated in step 1. You'll be left with another equation, which we'll call "MATH". "MATH" will have the same 2 variables as "YAY".
- 3) Pair the equations "YAY" and "MATH", to solve for the 2 variables therein.
- 4) Substitute those two values into one of the original equations, to find the third variable.

Ex#1: Please solve the following system.

$$x-3y+z=22$$

$$2x-2y-z=-9$$

$$x + y + 3z = 24$$

Ex#2: Please solve the following system.

$$x + y + z = 1$$

$$x + y - z = 3$$

$$2x+2y+z=3$$

Ex#3: Please solve the following system.

$$x + y + z = 2$$

$$3x+3y+3z=14$$

$$x-2y+z=4$$