

X747/76/12

Mathematics Paper 2

THURSDAY, 12 MAY 10:30 AM – 12:00 NOON

Total marks — 70

Attempt ALL questions.

You may use a calculator.

Full credit will be given only to solutions which contain appropriate working.

State the units for your answer where appropriate.

Answers obtained by readings from scale drawings will not receive any credit.

Write your answers clearly in the spaces provided in the answer booklet. The size of the space provided for an answer should not be taken as an indication of how much to write. It is not necessary to use all the space.

Additional space for answers is provided at the end of the answer booklet. If you use this space you must clearly identify the question number you are attempting.

Use blue or black ink.

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FORMULAE LIST

Circle:

The equation $x^2 + y^2 + 2gx + 2fy + c = 0$ represents a circle centre (-g, -f) and radius $\sqrt{g^2 + f^2 - c}$. The equation $(x - a)^2 + (y - b)^2 = r^2$ represents a circle centre (a, b) and radius r.

Scalar Product: $\mathbf{a}.\mathbf{b} = |\mathbf{a}||\mathbf{b}|\cos\theta$, where θ is the angle between \mathbf{a} and \mathbf{b}

or
$$\mathbf{a.b} = a_1b_1 + a_2b_2 + a_3b_3$$
 where $\mathbf{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$.

Trigonometric formulae: $\sin (A \pm B) = \sin A \cos B \pm \cos A \sin B$

$$cos (A \pm B) = cos A cos B \mp sin A sin B$$

 $sin 2A = 2 sin A cos A$

$$\cos 2A = \cos^2 A - \sin^2 A$$
$$= 2 \cos^2 A - 1$$
$$= 1 - 2 \sin^2 A$$

Table of standard derivatives:

f(x)	f'(x)
sin ax	$a\cos ax$
cos ax	$-a\sin ax$

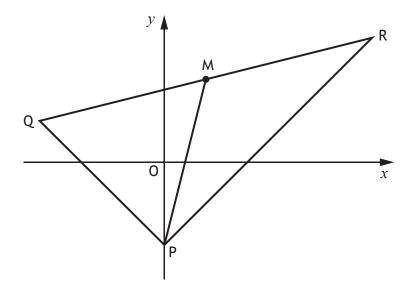
Table of standard integrals:

f(x)	$\int f(x)dx$
sin ax	$-\frac{1}{a}\cos ax + c$
cos ax	$\frac{1}{a}\sin ax + c$

Attempt ALL questions

Total marks — 70

1. PQR is a triangle with vertices P(0,-4), Q(-6,2) and R(10,6).



(a) (i) State the coordinates of M, the midpoint of QR.

1

(ii) Hence find the equation of PM, the median through P.

- 2
- (b) Find the equation of the line, L, passing through M and perpendicular to PR.
- 3

(c) Show that line *L* passes through the midpoint of PR.

3

3

2. Find the range of values for p such that $x^2 - 2x + 3 - p = 0$ has no real roots.

[Turn over

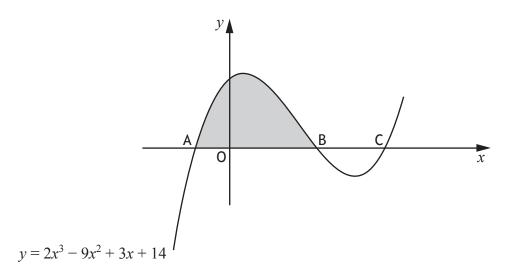
3. (a) (i) Show that (x+1) is a factor of $2x^3 - 9x^2 + 3x + 14$.

2

(ii) Hence solve the equation $2x^3 - 9x^2 + 3x + 14 = 0$.

3

(b) The diagram below shows the graph with equation $y = 2x^3 - 9x^2 + 3x + 14$. The curve cuts the *x*-axis at A, B and C.



- (i) Write down the coordinates of the points A and B.
- (ii) Hence calculate the shaded area in the diagram.

4. Circles C_1 and C_2 have equations $(x+5)^2 + (y-6)^2 = 9$ and $x^2 + y^2 - 6x - 16 = 0$ respectively.

(a) Write down the centres and radii of C_1 and C_2 .

4

(b) Show that C₁ and C₂ do not intersect.

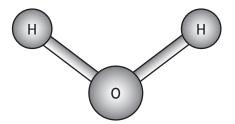
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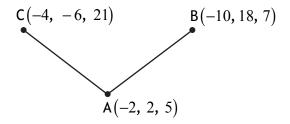
1

5. The picture shows a model of a water molecule.



Relative to suitable coordinate axes, the oxygen atom is positioned at point A(-2, 2, 5).

The two hydrogen atoms are positioned at points B(-10, 18, 7) and C(-4, -6, 21)as shown in the diagram below.



- (a) Express \overrightarrow{AB} and \overrightarrow{AC} in component form.
- (b) Hence, or otherwise, find the size of angle BAC.

6. Scientists are studying the growth of a strain of bacteria. The number of bacteria present is given by the formula

$$B(t) = 200 e^{0.107t}$$
,

where *t* represents the number of hours since the study began.

- (a) State the number of bacteria present at the start of the study.
- (b) Calculate the time taken for the number of bacteria to double.

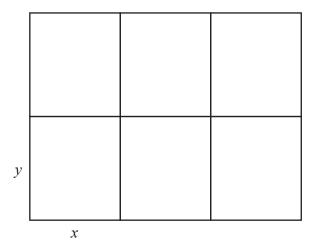
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[Turn over

6

7. A council is setting aside an area of land to create six fenced plots where local residents can grow their own food.

Each plot will be a rectangle measuring \boldsymbol{x} metres by \boldsymbol{y} metres as shown in the diagram.



(a) The area of land being set aside is 108 m^2 .

Show that the total length of fencing, L metres, is given by

$$L(x) = 9x + \frac{144}{x} . \tag{3}$$

(b) Find the value of *x* that minimises the length of fencing required.

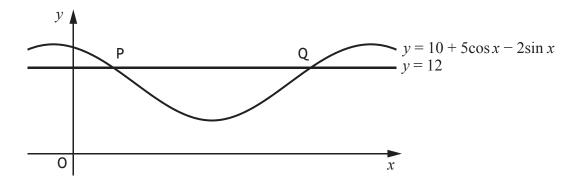
8. (a) Express $5\cos x - 2\sin x$ in the form $k\cos(x+a)$,

where k > 0 and $0 < a < 2\pi$.

4

(b) The diagram shows a sketch of part of the graph of $y = 10 + 5\cos x - 2\sin x$ and the line with equation y = 12.

The line cuts the curve at the points P and Q.



Find the x-coordinates of P and Q.

4

9. For a function f, defined on a suitable domain, it is known that:

$$\bullet \qquad f'(x) = \frac{2x+1}{\sqrt{x}}$$

•
$$f(9) = 40$$

Express f(x) in terms of x.

4

[Turn over for next question

10. (a) Given that $y = (x^2 + 7)^{\frac{1}{2}}$, find $\frac{dy}{dx}$.

2

(b) Hence find $\int \frac{4x}{\sqrt{x^2 + 7}} \, dx.$

1

11. (a) Show that $\sin 2x \tan x = 1 - \cos 2x$, where $\frac{\pi}{2} < x < \frac{3\pi}{2}$.

4

(b) Given that $f(x) = \sin 2x \tan x$, find f'(x).

2

[END OF QUESTION PAPER]

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X747/76/02

Mathematics Paper 2 Answer Booklet

THURSDAY, 12 MAY 10:30 AM – 12:00 NOON



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QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN
1.(a) (i)	MARGIN
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1.(a) (ii)	
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1.(b)	

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QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN	
3.(a) (i)	MARGIN	
3.(a) (ii)		

QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN	
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3.(b) (ii)		

QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN	
4.(a)	MARGIN	

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4.(b)	MARGIN	

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5.(a)	MARGIN	
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QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN	
6.(a)	MARGIN	
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QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN	
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	7.(b)	MARGIN	

QUESTION NUMBER	DO NOT WRITE IN THIS MARGIN	
8.(a)	MARGIN	

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9.	MARGIN	

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10.(a)	MARGIN	
10.(b)		



DO NOT WRITE IN THIS MARGIN QUESTION NUMBER 11.(a)

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11.(b)	MARGIN

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