

Algebra - Expressions and Formulas

The video covers the following exercises. Please print this sheet and work along!

$$x = 4$$

$$y = -3$$

$$z = 2.5$$

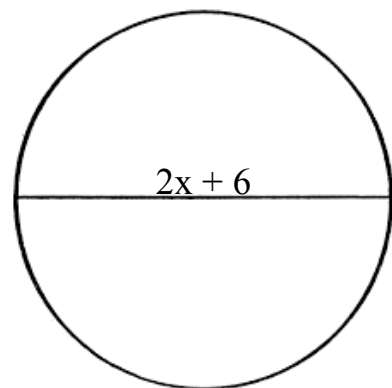
$$x + y - 2z$$

$$2(x + y)$$

$$\frac{x^2 - 4y}{2 - 4z}$$

Please write the appropriate expression for the area of the given circle:

$$A = \pi r^2$$



Algebra 2
Chapter 1 Notes

Name _____

Date _____

EQUATIONS AND INEQUALITIES

1.1: Expressions and Formulas

Order of Operations – PEMDAS

Parenthesis **E**xponents **M**ultiplication/**D**ivision **A**ddition **S**ubtraction

Key Concept Order of Operations

Step 1 Evaluate the expressions inside grouping symbols.

Step 2 Evaluate all powers.

Step 3 Multiply and/or divide from left to right.

Step 4 Add and/or subtract from left to right.

Ex#1: Evaluate the following expressions if $m = 12$ and $q = -1$

a) $m + (3 - q)^2$

b) $m + 2q + 4$

Ex#2: Evaluate the following expressions if $a = 5$ and $b = -3.2$

c) $a + b^2(b - a)$

Ex#3: Evaluate the following expression if $h = 4$, $j = -1$, and $k = 0.5$

$$\frac{j^2 - 3h^2k}{j^3 + 2}$$

Formula – a mathematical “sentence” that creates relationships between certain values

The formula $F = \frac{9}{5}C + 32$ represents the conversion of temperature from Celsius to Fahrenheit.

Ex#4: What is the Fahrenheit equivalent of 40°C ?

Ex#5: What is the Celsius equivalent of 41°F ?

Algebra - Properties of Real Numbers

The video covers the following information. Please print this sheet and work along!

List of number categories:

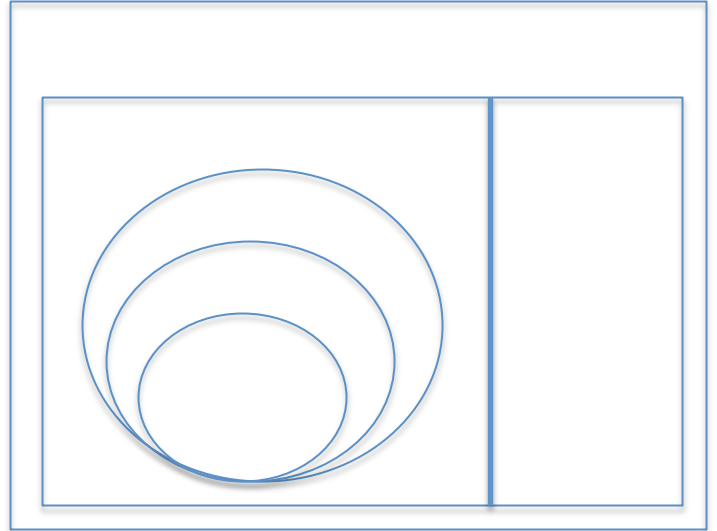
Natural #s –

Whole #s –

Integer #s –

Rational #s –

Irrational #s –



Please list which number categories each of the following are:

5

1.2

$\overline{1.22}$

-3

$\sqrt{36}$

$\sqrt{37}$

1.2: Properties of Real Numbers

Real numbers are classified in a variety of ways.

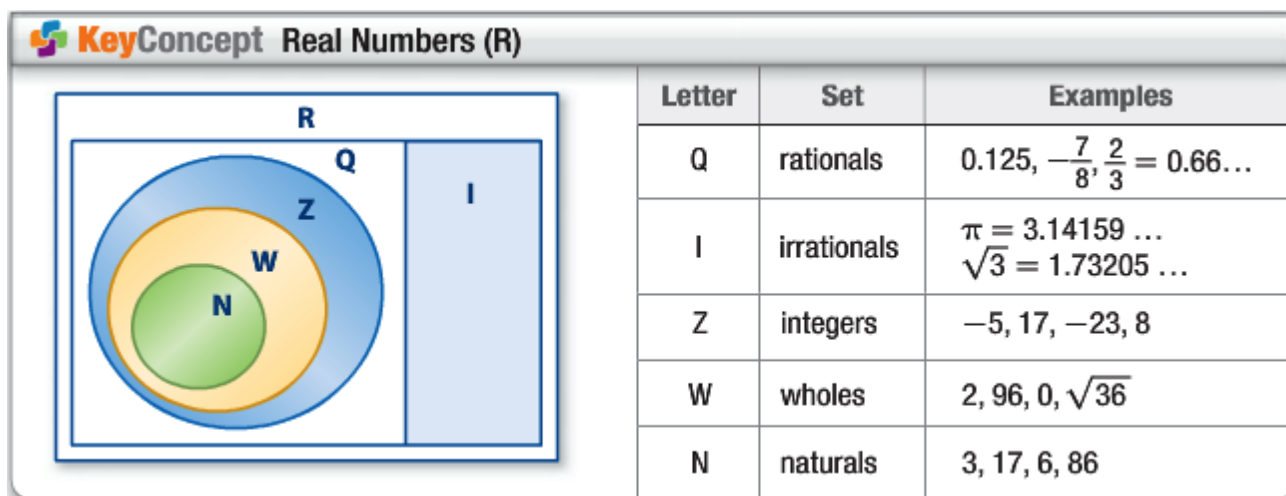
Natural numbers: 1, 2, 3, ...

Whole numbers: all Natural numbers, and 0. So, 0, 1, 2, 3, ...

Integers: all Whole numbers, and the negative countable numbers: ... , -3, -2, -1, 0, 1, 2, 3, ...

Rational numbers: all Integers, and *ratios* of integers, so fractions, ending decimals, and repeating decimals

Irrational numbers: cannot be represented by a ratio of integers. They're decimals that continue on without a pattern. Common examples include $\sqrt{}$ and π .



Ex#1: Name all of the sets of numbers to which each number belongs.

a) -185

b) $\sqrt{49}$

c) $\sqrt{95}$

d) $-\frac{7}{8}$

e) 0

f) $0.5\overline{8}$

Real Number Properties (and Examples)

For any real numbers, a , b , and c		
Property	Addition	Multiplication
Commutative	$a + b = b + a$	$a \cdot b = b \cdot a$
Associative	$(a + b) + c = a + (b + c)$	$(a \cdot b) \cdot c = a \cdot (b \cdot c)$
Identity	$a + 0 = a$	$a \cdot 1 = a$
Inverse	$a + (-a) = 0$	$a \cdot \frac{1}{a}$
Distributive	$\underline{a}(b + c) = \underline{a}b + \underline{a}c$	

Ex:#2: Please name the property illustrated by each of the following.

a) $(6 \cdot 8) \cdot 5 = 6 \cdot (8 \cdot 5)$

b) $84 + 16 = 16 + 84$

c) $(12 + 5)6 = 12 \cdot 6 + 5 \cdot 6$

Ex#3: Please find the additive and multiplicative inverses of each of the following numbers.

a) -7

b) 0.8 (hint: turn into a fraction)

Ex#4: Please simplify the following expressions.

a) $-2a + 4a(8 - 3a)$

b) $3(4x - 2y) - 2(3x + y)$



Algebra - Solving Equations

The video covers the following exercises. Please print this sheet and work along!

Math Property:

Reflexive –

Symmetry –

Transitive –

Substitution –

Addition –

Subtraction –

Multiplication –

Division –

$$2x - 1 = 13$$

$$\frac{2}{3}x = 30$$

if $3x - 3 = 1/4$, then what is $3x + 7$?

$$V = \frac{1}{3}\pi r^2 h$$

Please solve for h .

1.3a: Solving Equations

Translating Verbal Expressions and Algebraic Expressions

Ex#1:

- a) Please translate the verbal expressions into an algebraic expressions.

three times the difference of a number and eight

the cube of a number increased by 4 times the same number

- b) Please translate the algebraic expression into a verbal expression.

$$p^3 + 4p$$

Ex#2: Please write a verbal sentence to represent the equation.

$$2c = c^2 - 4$$

Properties of Equality – common math operations, used to solve equations

For any real numbers, a , b , and c		
Property	Using only symbols	Additional examples
Reflexive	$a = a$	$b + 8 = b + 8$
Symmetric	If $a = b$, then $b = a$	If $2b + c = 20$, Then $20 = 2b + c$
Transitive	If $a = b$, and $b = c$, then $a = c$	If $2a + 12 = 30$, and $30 = 5c - 8$, then $2a + 12 = 5c - 8$
Substitution	If $a = b$, then a can be replaced by b b can be replaced by a	If $(5 + 2)x = 21$, Then $7x = 21$

Ex#3: Please name the property illustrated by the following statement.

$$\text{If } -11a + 2 = -3a, \text{ then } -3a = -11a + 2$$

Additional Properties of Equality

“Whatever operation you do to one side of the equation, you must do to the other.”

For any real number ‘a’	
Property	Example
Addition	if $a = a$ then $a + 8 = a + 8$
Subtraction	if $a = a$ then $a - 4 = a - 4$
Multiplication	if $a = a$ then $a \cdot 3 = a \cdot 3$
Division	if $a = a$ then $a \div 7 = a \div 7$

Ex#4: Please solve the following equations, noting which property of equality is being utilized.

a) $x - 14.29 = 25$

b) $\frac{2}{3}y = -18$

c) $-10x + 3(4x - 2) = 6$

Ex#5: Please solve for h in the following formula for area of a trapezoid. $A = \frac{1}{2}h(b_1 + b_2)$

Please note the property used for each step.



Algebra - Solving Equations (word problem)

If Suzy sells a total of 50 fruits in a day, and sells 8 more apples than plums...

(what will be
the question?)

1.3b: Solving Equations (word problems)

Ex. #1: Suppose that in my coffee shop, one day I sell 12 *more* regular coffees than decaffeinated. The total cups I sold that day were 60. How many of each kind of coffee did I sell?

(Hint: you can either play around with numbers to guess and check, or assign variables, such as D for the number of decaf cups sold.)

Ex. #2: Supplementary angles are defined as 2 angles that sum to 180° . Suppose that one angle is 3 times larger than its supplement. What are the measures of the 2 angles?

(Same hint as above. Maybe start with 100° and 80° . They're supplementary, but 100 is not 3 times as large as 80. So tinker with the numbers until one angle is 3 times larger than the other. Or, you can set variables to represent each of the 2 angles.)

Algebra

Absolute Value Equations

YAY MATH!

The following problems are solved in the video:

$$|x + 6| = 18$$

$$\left| \frac{1}{2}x - 1 \right| = 2$$

$$3|x + 6| = 36$$

$$|3x - 1| = -450$$

$$|3t - 5| = 2t$$

$$|x - 3| + 7 = 2$$

1.4: Solving Absolute Value Equations

The **absolute value** of a number is its *distance from zero* on a number line. Since distance is always non-negative, absolute values are always non-negative.

Symbol: $|x|$

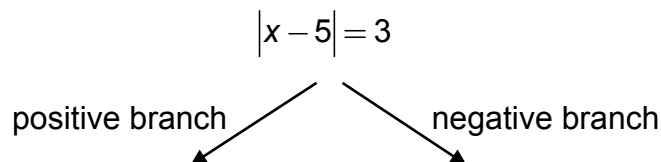
Another way of understanding it is that the absolute value bars are like a “positivity machine.” Any number that enters the positivity machine will come out *positive*. Zero will come out as zero.

Ex #1: Please evaluate the following if $x = -2$.

a. $|4x + 3| - 3\frac{1}{2}$

b. $-2|3 - x| + 8$

Solving Absolute Value Equations – “BIFURCATE” – meaning, dividing into two branches

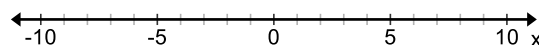
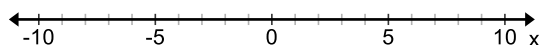


(then solve both branches)

Ex #2: Please solve each equation. Then graph your solution(s) on a number line.

a) $|x + 3| = 6$

b) $|x - 7| = 4$



No solution?

We know that an absolute value is always equal to a positive number.

Thus, whenever an absolute value equation equals a *negative number*, there is **no solution**.

Here are some examples of an equation having “no solution” for the variable, ‘a’.

$$|a| = -8$$

(there is no number that a can be
that would make the equation true)

$$-2|3a| = 8$$

(divide both sides by -2 , to
see that abs. value = neg.)

Ex #3: **Extraneous Solutions** – When an absolute value expression is set equal to an expression containing a variable, **extraneous solutions** may be encountered.

(Hint: first combine like terms. Then isolate the absolute value. Then bifurcate, and solve each.)

$$2|x + 1| - x = 3x - 4$$



Algebra - Solving Inequalities

The video covers the following exercises. Please print this sheet and work along!

Add 3 to both sides
 $2 < 6$

Divide both sides by 2
 $2 < 6$

Multiply both sides by -1
 $2 < 6$

$$3x + 1 > 22$$

$$-3x + 1 > 22$$

$$10 > -2x$$

$$x \leq \frac{3-x}{2}$$

$$\frac{2x-6}{4} > \frac{x-3}{2}$$

(please circle one)

“at least” means:

$<$ \leq \geq $>$

“at most” means:

$<$ \leq \geq $>$

“no more than” means:

$<$ \leq \geq $>$

“no less than” means:

$<$ \leq \geq $>$

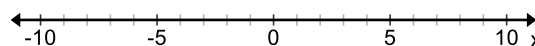
1.5: Solving Inequalities

(circle one)

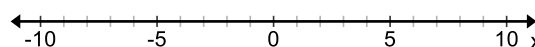
Adding and subtracting the same amount to each side of an inequality **DOES / DOES NOT** reverse the direction of the inequality sign.

Ex#1: Please solve the inequalities. Then graph the solution set.

a) $5x - 3 > 4x + 2$



b) $4x - 15 \leq 21$



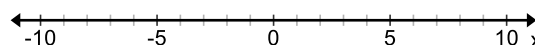
(circle one)

Multiplying or dividing by a **positive number** DOES / DOES NOT reverse the inequality sign.

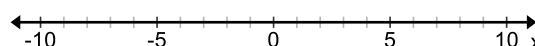
Multiplying or dividing by a **negative number** DOES / DOES NOT reverse the inequality sign.

Ex#2: Please solve and graph on the number line.

a) $-4.2x \leq 29.4$



b) $-3x \leq \frac{-4x + 22}{5}$



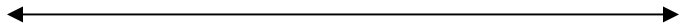
Algebra

Absolute Value Inequalities

YAY MATH!

The following problems are solved in the video:

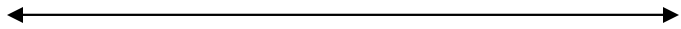
$$3x + 1 < 7 \text{ OR } 7 < 2x - 9$$



$$|x + 2| > 3$$

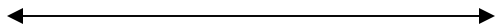
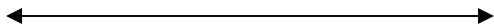
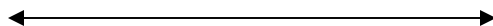
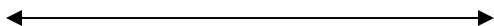


$$|2x - 9| \leq 27$$



$$|5x| + 10 < 3$$

$$|5x| > -7$$

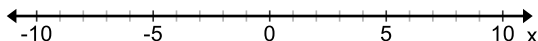


1.6: Solving Compound and Absolute Value Inequalities

A **compound inequality** consists of two inequalities joined by the word “and” or “or.”

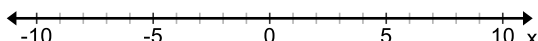
$$x \geq -4 \text{ and } x < 3$$

The compound inequality above involves “and”. This means that BOTH statements need to be true. How would you graph all the numbers that are BOTH ≥ -4 and < 3 ?



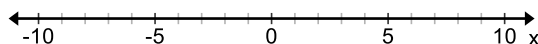
“**And**” inequalities may also be rewritten in the following ways:

$$4x+8 \geq -12 \text{ and } 4x+8 \leq 32 \quad \text{can be condensed to:} \quad -12 \leq 4x+8 \leq 32$$



Ex#1: Please solve and graph.

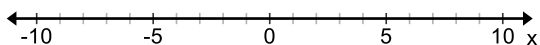
$$-5 \geq 3x-2 > -14$$



“Or” Inequalities is the **union** of the solution sets.

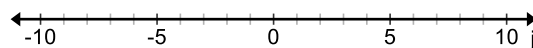
$$x \geq 5 \text{ or } x < -3$$

The compound inequality above involves “or”. This means that ONE or BOTH of the statements need to be true. How would you graph all the numbers that are EITHER ≥ 5 or < -3 ?

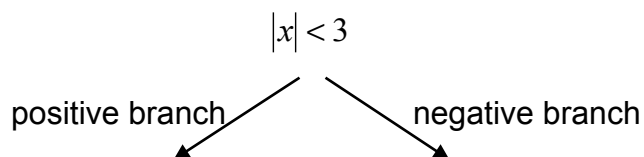


Ex#2: Please solve and graph the inequality.

$$5j \geq 15 \text{ or } -3j \geq 21$$

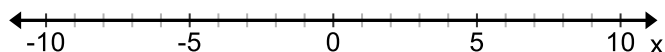


Absolute Value Inequalities – time to BIFURCATE into 2 separate statements

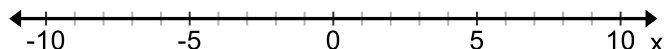


Ex#3: Please solve and graph.

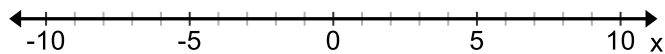
a) $|x| < 6$



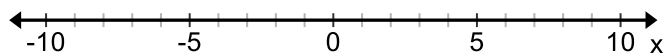
b) $|x| \geq 6$



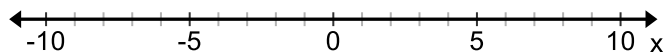
c) $|x-4| \leq 6$



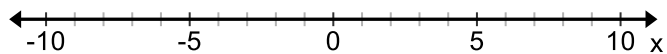
d) $|x+7| > 2$



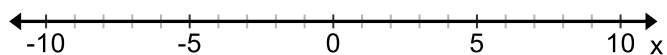
e) $|8x+3| \leq 4$



f) $|x+3| \leq -6$ (Hint: can an absolute value expression ever be less than -6 ?)



g) $|x+3| > -6$ (Hint: how often is an absolute value expression greater than -6 ?)



Remember to look for open circles or closed circles to decide which inequality to use, $<$ vs \leq
 $>$ vs \geq

Let's check for understanding:

When using graphs, *open circles* over the numbers (circle one) DO / DON'T include "or equal to" (as in, \leq)

When using graphs, *closed circles* over the numbers DO / DON'T include "or equal to"

To create an absolute value inequality, use this guide for "AND" problems:

$$|x - \text{middle \#}| \leq \text{distance from middle to each value}$$

And use this for "OR" problems:

$$|x - \text{middle \#}| > \text{distance from middle to each value}$$

Remember this fun guide:

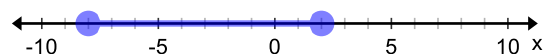
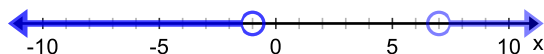
$<, \leq$ less than "less thAND"

$>, \geq$ greater than "greatOR"

(so these abs. val. inequalities involve AND)

(these abs. val. inequalities involve OR)

Ex#4: What is the absolute value inequality represented in each graph below?



a) _____

b) _____

Algebra 2
Chapter 1 Practice Test

Name _____
Date _____

Please evaluate each expression.

1) $\frac{16 - 3 \cdot 2}{1 + 4}$ 1) _____

2) $21 + [6 - 12 \div 3]$ 2) _____

3) $\frac{3}{4}(11 - 7)^2$ 3) _____

Please evaluate each expression if $a = 3$, $b = -4$, and $c = \frac{1}{4}$.

4) $a^2(b - a)$ 4) _____

5) $\frac{8c + ab}{c}$ 5) _____

Please complete the table below by placing a check mark or X to indicate all sets of numbers that apply to the value of each expression.

		R real	I irrational	Q rational	Z integer	W whole	N natural
6)	0.4						
7)	$\sqrt{\frac{1}{4}}$						
8)	$-\sqrt{7}$						
9)	-15						

10) What are the additive and multiplicative inverses of $1\frac{2}{3}$? 10) Additive: _____

Multiplicative: _____

Please name the property illustrated by each equation or statement.

11) If $x - 2 = 5$, then $x = 7$.

11) _____

12) $(3 \cdot 4) \cdot 9 = 3 \cdot (4 \cdot 9)$

12) _____

13) If $a = b$ and $b = -2$, then $a = -2$.

13) _____

Please solve each equation or formula for the specified variable.

14) $y(x + z) - v = 3d$ for y

14) _____

15) $\frac{10z + x}{y} = 4$ for x

15) _____

Please solve each equation.

16) $6m - 4 = -46$

16) _____

17) $\frac{d}{2} + \frac{d}{4} = 3$

17) _____

18) $5 - (2w - 8) = 6w - 9$

18) _____

19) $|x - 3| = 1$

19) _____

20) $2|3e - 2| = 14$

20) _____

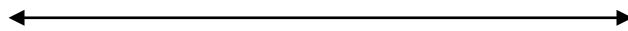
21) $|3x - 8| = -15$

21) _____

Please solve each inequality. Then graph the solution set on a number line.

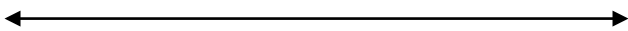
22) $-3y - 4 \geq -7$

22) _____



23) $|2x + 3| \geq 11$

23) _____



24) $|3x - 4| < -7$

24) _____



25) $2a + 12 \leq 6$ or $3a - 1 > -13$

25) _____

